



**HAL**  
open science

# Matching in the presence of don't cares and redundant sequential elements for sequential equivalence checking

Solaiman Rahim, Bruno Rouzeyre, Lionel Torres, Jerome Rampon

► **To cite this version:**

Solaiman Rahim, Bruno Rouzeyre, Lionel Torres, Jerome Rampon. Matching in the presence of don't cares and redundant sequential elements for sequential equivalence checking. HLDVT 2003 - 8th IEEE International High-Level Design Validation and Test Workshop, Nov 2003, San Francisco, United States. pp.129-135, 10.1109/HLDVT.2003.1252486 . lirmm-00269707

**HAL Id: lirmm-00269707**

**<https://hal-lirmm.ccsd.cnrs.fr/lirmm-00269707>**

Submitted on 7 Sep 2022

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# Matching in the presence of don't cares and redundant sequential elements for sequential equivalence checking

Solaiman Rahim  
[rahim@synplicity.com](mailto:rahim@synplicity.com)  
LIRMM – Synplicity  
Montpellier, FR

Bruno Rouzeyre  
[rouzeyre@lirmm.fr](mailto:rouzeyre@lirmm.fr)  
LIRMM  
Montpellier, FR

Lionel Torres  
[torres@lirmm.fr](mailto:torres@lirmm.fr)  
LIRMM  
Montpellier, FR

Jerome Rampon  
[jerome@synplicity.com](mailto:jerome@synplicity.com)  
Synplicity  
Montpellier, FR

## Abstract:

Full sequential equivalence checking by state space traversal has been shown to be unpractical for large designs [10]. To address state space explosion new approaches have been proposed that exploit structural characteristics of a design and make use of multiple analysis engines (e.g. BDDs, Simulation, SAT) to transform the sequential equivalence checking problem into a combinational equivalence checking problem [1][8]. While these approaches, based on induction techniques [1][2][3], have been successful in general, they are not able to reach proof of equivalence in presence of complex transformations between the reference design and its implementation. One of these transformations is redundant Flip-Flops (FFs) removal. FFs may be removed by redundancy removal, or don't care optimization techniques applied by synthesis tools. Consequently, some FFs in the reference design may have no equivalent FFs in the implementation net-list. Latest researches in this area have proposed specific solutions for particular cases. In [5], matching in the presence of redundant constant input FFs has been addressed and in [11] identification of sequential redundancy is performed. This paper presents an in-depth study of some possible causes of unmatched FFs due to redundancy removal, and proposes a generic approach to achieve prove of equivalence in presence of redundant FFs. Our approach is independent from specific synthesis transformations. It is able to achieve matching in presence of complex redundancies, and is able to perform formal equivalence checking in presence of don't cares. The experimental results show a significant improvement in the matching rates of FFs when compared to industrial equivalence checking tools. This higher matching is directly translated to a higher success rate in proving equivalency.

## 1. Introduction

Generic equivalence checking methods of two sequential circuits require a state space traversal of the product machine. This method has the capacity to handle sequential optimizations (such as retiming, pruning, state machine re-encoding...), which are performed during synthesis. However, due to computational complexity, those methods cannot be applied to large circuits. Other approaches have been investigated which try to map the sequential equivalence problem of circuits

into a combinational equivalence checking problem [8]. They rely on identifying some potential equivalent FFs or nets in the two circuits under verification through a matching/mapping step, and checking the equivalence of those FFs and nets by using combinational verification. The powerful existing matching methods [1][2][3] are functional based method using induction proof. They are applied to try to handle some sequential optimizations done during synthesis as merge, replication, sequential redundancy removal and retiming. These methods consist to find functional equivalent FFs in the two designs. But they cannot handle efficiently all type of sequential optimizations done during synthesis, particularly the optimizations which removed sequential elements such as redundancy removal or don't care optimizations (only method for constant input FFs was proposed in [5] and [6]). Furthermore, they do not handle unspecified values (which is called don't care) derived from the circuit (one method was proposed in [2] which consists to do the matching for each possible value of the don't care, but can not be applied for circuits with large number of don't care). In this paper, optimizations that remove sequential elements are presented. The problems, they may introduce for the existing matching methods, are illustrated on a set of circuits with redundant FFs. Then a synthesis independent method to complete the existing matching to handle those optimizations is proposed. We demonstrate that it completes the existing matching method efficiency. In section 6, a set of industrial circuits is used to compare our algorithm with some industrial tools

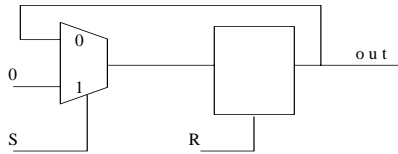
## 2. Preliminaries

Here we introduce the notion of redundant FFs and don't care functions which are used in the following sections.

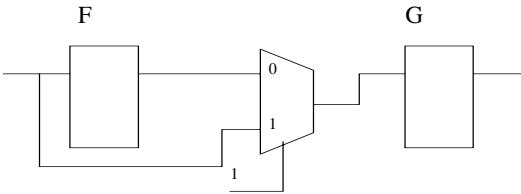
### 2.1 Redundant FFs

**Definition 1:** A FF  $R$  of a circuit  $C$  is called *redundant FF*, if the observable input-output behavior of  $C$  is invariant after removing  $R$  from the circuit.

**Definition 2:** A *constant input FF* is an FF with a constant input function (0 or 1) at any clock cycle.



**Figure 1: Example of stuck at 0 FF**



**Figure 2: F is a non-observable FF**

**Definition 3:** If  $F(t)$  is the input function of an FF  $R$  and  $v$  its output variable,  $R$  is *stuck at 0* (resp *1*) (An example is given in figure 1) iff:

- 1)  $\exists t \mid \forall T \geq t, F(t) = 0$  (resp 1)
- 2)  $F(t)$  is a function of  $v$ .

**Definition 4:** An FF  $R$  of a circuit  $C$  is called a *non-observable FF*, if the observable output behavior of  $C$  is independent of the value of  $R$ , for all possible states and all possible input combinations of  $C$ . An example is given in Figure 2.

Constant input FF, stuck at FF and non-observable FF are all redundant FFs and can be removed by the synthesis tools.

## 2.2 Don't care definitions

**Definition 5:** A *don't care variable* (noted dc-var) is a Boolean function which can be substituted by any Boolean function, in particular by 0 or 1. Figure 3 described the use of don't care variables to express the output function of a multiple driver net.

	$(V1, E1, V2, E2)$	Out
	$(0, 0, 0, 0)$	Dc1
	$(0, 0, 1, 0)$	Dc1
	$(0, 1, 1, 1)$	Dc2
	$(1, 0, 0, 0)$	Dc1
	$(1, 0, 1, 0)$	Dc1
	$(1, 1, 0, 1)$	Dc2
	$(1, 1, 1, 1)$	$V1=V2=1$

**Figure 3: A circuit with don't care** **Incomplete Truth Table of function Out**

**Dc1** comes from the condition that  $E1$  and  $E2$  can both be inactive.

**Dc2** comes from the condition that  $E1$  and  $E2$  can be active simultaneously and  $v1 \neq v2$ .

**Definition 6:** A *don't care function* (noted dc-full-func) is a Boolean function with only don't care variables in its support set. Note that dc-full-func is always reduced to 0 or 1 by affecting don't care variables to a constant values. (Figure 5)

Let  $Fct$  be the set of all Boolean functions.

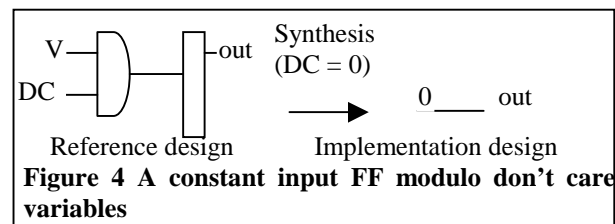
Let  $X = \{Dc1, Dc2, \dots\}$  be the set of dc-var of a Boolean function  $F$ .

**Definition 7:** A *dc-var-interpretation* is a map  $X \rightarrow \{0, 1\}$  which associates a Boolean value to each dc-var.

**Definition 8:** A *dc-func-interpretation* of the function  $F$  is a map  $I: \{0, 1\}^X \rightarrow Fct$  which associates a Boolean function to each dc-var interpretation.

Note that all dc-func-interpretations of the function  $F$  are included to it and there are  $2^{|X|}$  dc-func interpretations of the function  $F$  possible.

**Definition 9:**  $R$  is a constant input FFs "*modulo don't care variables*" iff  $\exists$  a dc-func-interpretation of  $R / R = 0$  or  $R = 1$ . (Example in Figure 4)



**Figure 4 A constant input FF modulo don't care variables**

**Definition 10:** A *zero* (resp *one*) *don't care* (noted 0-dc-func) is a function equal to zero (resp one) out of the don't care set, i.e  $\exists$  a dc-func-interpretation of  $F / F = 0$  (resp 1). (Example in figure 7). Notice that the example in figure 6 is a 0-dc-func and a 1-dc-func.

**Definition 11:** A function  $Impl$  is *contained* to a function  $Ref$  iff  $\exists$  a dc-func-interpretation  $I$  of  $Ref$  such as  $I = A$ .

**Theorem:** A FF  $R$  is a *constant input FF modulo don't care variable* iff the input function of  $R$  (noted  $F$ ) is a dc-all-func, 0-dc-func or a 1-dc-func.

If the input function of an FF  $R$  is a constant input FF modulo don't care variable, it may become a redundant FF and may be removed by the synthesis tool depending on which dc-func-interpretation of  $R$  is chosen.

$$F = (DC1 \vee DC2) \wedge DC3$$

Reference design

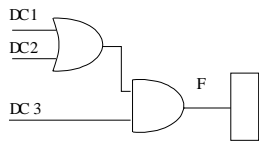
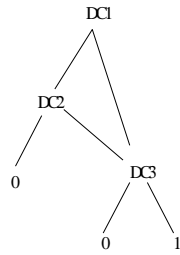


Figure 5: dc-all-func

BDD representation



$$F = (v \vee DC1) \wedge DC2$$

Reference design

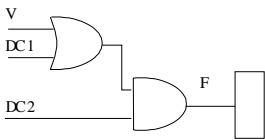
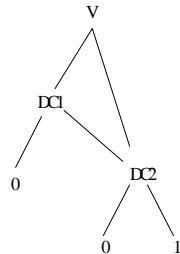


Figure 6: 0 and 1 - dc-func

BDD representation



$$F = \neg v \wedge DC2$$

Reference design

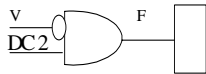
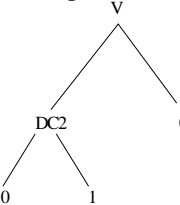


Figure 7: 0-dc-func

BDD representation



### 3. Redundancy removal problems in existing matching methods [1,2,3]

#### 3.1 Constant input FFs problems

Let's consider the example below (Figure 8 (a),(b)). In figure 8a, constant propagation is not performed which leads to  $Out1 \neq Out2$  (false negative). In figure 8b, constant propagation through FFs was performed and the proof concludes  $Out1 = Out2$ .

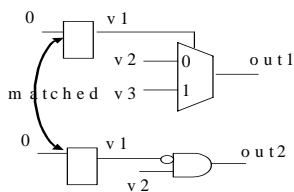


Figure8(a):Constant input FF

$$Out1 = (V2 \wedge \neg V1) \vee (V3 \wedge V1)$$

$$Out2 = (V2 \wedge \neg V1)$$

$$\Rightarrow Out1 \neq Out2 \text{ (False negative)}$$

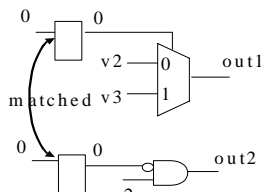


Figure8(b):Constant input propagation

$$\Rightarrow Out1 = Out2$$

#### 3.2 Stuck at FFs problems

The matching process identifies the redundant FFs in the reference design as unmatched FFs because there are no equivalent FFs in the implementation and its input function is not a constant. Sequential equivalence checking often considers unmatched FFs as retimed, and methods similar to [1] or [4] are applied.

The method proposed in [1] consists of finding equivalent nets. This method fails in figure 9 because there are no equivalent nets.

In [4], the method consists of injecting the input function of the unmatched FFs to its output at the next clock cycle. This method fails in figure9 because their method of transforming the circuit with a feedback loop into a loop free circuit requires a positive unate function (otherwise an infinite loop can be created which is the case in figure 9). This is why we are proposing a method to extend the coverage in such cases.

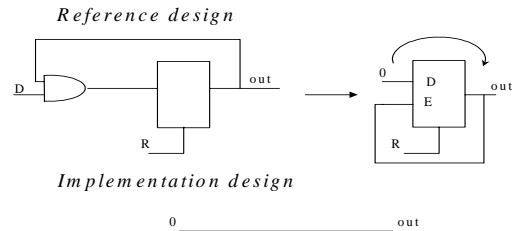


Figure 9: Example of stuck at 0 FF that cannot be handled in [4]

### 4. Our redundancy removal engine for matching step

We introduce here our redundancy removal engine and the process of our engine is illustrated in Figure 10, 11, 12, 13.

#### 4.1 Constant input FFs

To handle constant input FFs, the input function of some candidate FFs is computed using BDD representation. Then the constant propagation through the FFs with BDD equal to 0 and 1 is done and the FFs are removed. The candidate FFs come from a random simulation. This reduces the number of BDD computed.

#### 4.2 Stuck at FFs

We propose here to extend the method proposed in [1]. Indeed, an induction technique is used here to find stuck at FFs.

Let F be the input function of a FF R.

- If R is a FF with a reset line, it can be removed if  $F(t) = 0 \Rightarrow F(t+1) = 0$ .

- If R is a FF with a set line, it can be removed if  $F(t) = 1 \Rightarrow F(t+1) = 1$ .

#### 4.3 Non observable FFs

The method is based on the DTPG algorithm proposed in [7] which consists of identifying redundant nodes by searching for undetectable stuck-at-fault. We apply the algorithm to the FFs instead of the circuit nodes. The

FF is removed if no pattern is found to make the output of the FF observable.

One way to implement the DTPG algorithm is to check if the output variable of a candidate FF is present in the function of all FFs in its transitive fan out (using Bdds for example). This can be very time consuming because of the Bdds complexity. But the use of simulation techniques on the Bdds shows that the time can be considerably decreased (a average gain of 80% has been noticed)

The final flow is the following:

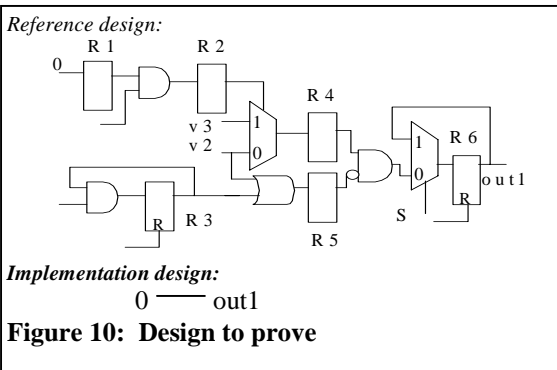
```
Void RemoveRedFFs(Netlist *nl){
  while (fixpoint1)
  {
    removeConstFFs(nl);
    removeStuckAtFFs(nl);
  }

  while (fixpoint 2)
    removeNonObsFFs(nl);}

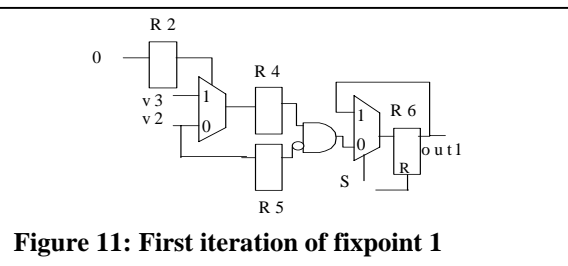
```

Note that our engine is a fixpoint algorithm because every time a FF is removed from the design, new FFs can become redundant. Two fixpoints is needed because removing constant input or stuck at FFs does not imply new non-observable FFs and removing non-observable FFs does not imply new constant or stuck at FFs.

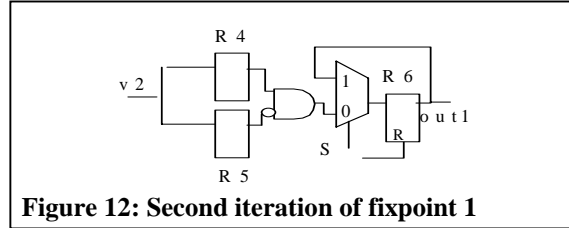
The process of the algorithm is illustrated on the reference and implementation designs in Figure 10.



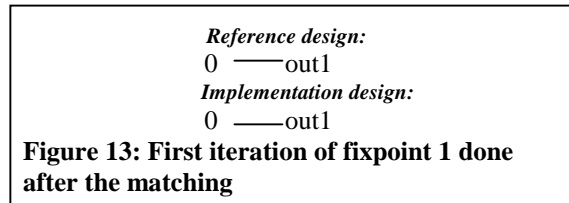
After first iteration of fixpoint 1, R1 is removed because it is a constant input 0 FF, R3 is removed because it is a stuck-at-0 FF, then the reference design is transformed into the equivalent circuit in figure 11.



After second iteration of fixpoint1, R2 is removed because it is a 0 constant input FF and the circuit in figure 11 is transformed to the equivalent circuit in Figure 12.



After first iteration of fixpoint1 done after the matching, R6 is removed because it became a stuck at 0 FF after that R4 and R5 have been matched together. Then the circuit in Figure 12 is transformed to the equivalent circuit in Figure 13 and can be proved easily with the implementation design

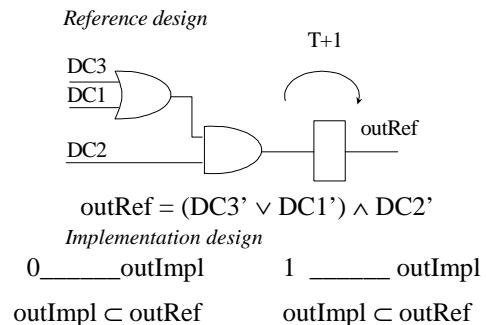


## 5. How to handle Don't care ?

**Notation:** In the following, a function F at next clock cycle (defined as the CBF function in [4]) is noted F'.

### 5.1 How to handle dc-full-func

To handle dc-full-functions, we reintroduce the don't care input function of the FFs to its output at the next clock cycle (note that a dc-full-func at time t remains a dc-full-func at time t+1). This works because dc-full-function is always reduced to 0 or 1 after don't care assignment, and 0 and 1 are contained to the new dc-full-func created at time t+1. This technique is illustrated in figure 14.



**Figure 14: Different implementations of a dc-full-func**

## 5.2 A simulation and assertion method to handle 0-dc-func (resp 1-dc-func).

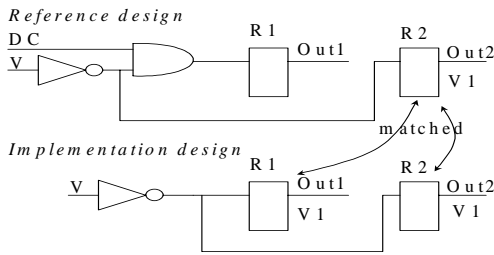
Let's consider Figure 15 and 16 that are the results of a different interpretation of the don't care variables from the same reference design.

The method proposed in section 5.1 can not handle the interpretation of figure 15. Indeed the functional matching can result in the following: {R2(ref), R1(impl), R2(impl)} are matched, and R1{ref} is unmatched as its input function contains don't care. Reintroducing the input function of FF R1(ref) to its output results in the following:

$$\text{Out1ref} = (\text{DC}' \wedge (\neg V'))$$

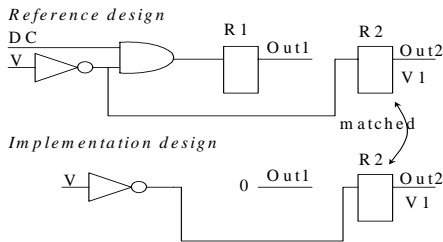
$$\text{Out1impl} = V1$$

$$\Rightarrow \text{Out1impl} \not\subset \text{Out1ref} \text{ (false negative)}$$



**Figure 15: Unknown interpretation of don't care (DC = 1)**

The method proposed in [2] which is based on "inclusion matching" can not handle the interpretation of figure 16. Indeed, functional matching using "inclusion checking" can match {R1(impl), R2(ref), R2(impl)} because R2(impl) is included in R1(Ref). In this case the proof result is  $\text{Out1(ref)} \neq \text{Out1(impl)}$  (false negative)



**Figure 16: Unknown interpretation of don't care (DC = 0)**

To handle 0-dc-func (1-dc-func), our method combines "inclusion matching" [2] with method presented in section 5.1 to extract assertions for prove of equivalence.

The algorithm is as follow:

- 1) Reintroduce the input function  $F(t)$  of FFs with don't care variables to its output at next clock cycle.
- 2) Do the inclusion check.
- 3) Set all assertion given by inclusion checking (i.e if R is a matched FF with output variable  $v$  and it has been checked being included into FF  $R'$  with input function  $F(t)$ , then the assertion  $v \subset F(t)$  is set).

The algorithm is applied after functional matching which, is done without any consideration of don't cares.

Applying this method on Figure 15 gives:

$$1) \text{Out1ref} = (\text{DC}' \wedge (\neg V'))$$

$$2) \text{Inclusion check gives } R1(\text{impl}) \subset R1(\text{ref}), R2(\text{impl}) \subset R1(\text{ref})$$

$$3) \text{Set the assertion } V1 \subset (\text{DC}' \wedge (\neg V'))$$

$$\Rightarrow \text{Out1impl} \subset \text{Out1ref} \text{ as we made the assertion that } V1 \text{ is contained in } (\text{DC}' \wedge (\neg V'))$$

Applying this method on Figure 16 gives:

$$1) \text{Out1ref} = (\text{DC}' \wedge (\neg V'))$$

$$2) \text{Inclusion check gives } R2(\text{impl}) \subset R1(\text{ref})$$

$$3) \text{Set the assertion } V1 \subset (\text{DC}' \wedge (\neg V'))$$

$$\Rightarrow \text{Out1impl} \subset \text{Out1ref} \text{ as we have } 0 \text{ contained in function } (\text{DC}' \wedge (\neg V'))$$

## 5.3. Improvements and Limitations

The method presented in section 5.2 needs to reintroduce the input function of FFs with don't care variables to its output at next clock cycle. If the FFs have a feedback loop, the method cannot work because of the loop. In this case, methods to transform circuit with feedback loop into loop free circuit can be used as presented in [4]. But this method cannot handle all kind of circuits; this is why we are working to settle a general method in this case.

In this paper, a set of potential optimizations, which removed redundant FFs, have been presented. This set is not exhaustive and new algorithm can be added to our engine to handle more optimizations.

## 6. Experimental results & Conclusion

We have synthesized a set of industrial designs using Synplify Pro 7.0 ([www.synplicity.com](http://www.synplicity.com)) synthesis tool with "prune redundant FFs option" enabled. For constant input and non-observable FFs, both our method and those of industrial tools have the same results. However, for all designs with stuck at and constant FFs, our method is better and is able to complete the proof successfully compared to the industrial tools (the designs T7 which is snippet of the circuit on figure10 in section 4 is proved correct with our method and not with the industrial tools). For circuits with don't care function, our method is able to perform the proof in all cases. The industrial tools can prove some of them. Our belief is that it randomly assigns a value to the don't care variables, and thus, this assignment can chose the same value as the synthesis tools (see T10 Figure15 section 5). This is confirmed by the fact that design T11 (Figure16 section 5), a different interpretation of the don't care variables of the same reference design of T10, is proved different.

Finally, we also notice an increase in run-time with our method. This is due to the "inclusion checking," which is needed for each possible pair. Our future work is to

use simulation to reduce the number of possible pairs and thus decrease the run-time.. (Note: DC case 1: dc-full-func; DC case 2: 0-dc-func or 1-dc-func, SAt0: stuck-at-0 FF, NObs: Non observable FF)

Design Automation Conference Proceedings 1996, 33rd, 3-7 June 1996

Test	Size(K)	Pruning type	Industrial tools		[1] + our method	
			Pass	T(s)	Pass	T (s)
T1	18	NObs	Yes	1.10	Yes	1.32
T2	33	SAt0 +const	No	1.89	Yes	4.73
T3	40	Const+NObs	Yes	2.12	Yes	1.21
T4	36	Const+NObs	Yes	1.79	Yes	3.40
T5	15	Const	Yes	1.46	Yes	2.03
T6	45	No red	Yes	24.8	Yes	35.26
T7	90	SAt0 +const	No	57.7	Yes	78.68
T8	102	DC case 1	Yes	12.3	Yes	15.59
T9	200	Const+ DC case1	No	32.3	Yes	36.23
T10	200	DC case 2	Yes	35.2	Yes	54.56
T11	200	DC case 2	No	40.1	Yes	58.23

**Table 1: Results on industrial designs**

## References

- [1] C. van Eijk, "Sequential equivalence checking without state traversal", *DATE*, 98, pp. 618-623.
- [2] Anastasakis, Damiano, Tony Ma, Stanion, "A Practical and Efficient Method for Compare-point Matching" *DAC 2002*, pp 305-310.
- [3] J.R Burch and V. Singhal "Robust Latch Mapping for Combinational Equivalence checking" in *ICCAD, 1998*, pp563-569.
- [4] Ranjan, Singhal, Somenzi, Brayton, "Using Combinational Verification for Sequential Circuits" (*DATE '99*) p. 138
- [5] C.vanEijk: Formal Methods for the Verification of Digital Circuits, *Ph.D. Thesis of the Eindhoven University of Technology, Eindhoven, The Netherlands, September 1997*
- [6] Shi-Yu Huang, Kwang-Ting Cheng, Kuang-chien Chen, Uwe Glaeser, "An ATPG-based Framework for Verifying Sequential Equivalence" *IEEE ITC 1996*, pp. 145 - 157
- [7] Stefan Hendriex, luc Claesen, "Formally Verified Redundancy Removal", *DATE 99*, p. 150
- [8] R.K.Brayton "sequential equivalence checking" Logic synthesis and verification. Kluwer Academic Publishers. Chap12
- [9] Jerry R. Burch, Vigyan Singhal "Tight integration of Combinational Verification Methods", *ICCAD98*, San Jose p570-576.
- [10] O.Coudert, C.Berthet, J-C Madre, "Verification of synchronous Sequential Machines based on symbolic execution", in "Automatic Verification Methods For Finite State Systems" J.Sifakis, LNCS n407, pp3658-373, Springer Verlag 89
- [11] Iyer, M.A.; Long, D.E.; Abramovici, M.; "Identifying sequential redundancies without search" in