Scaleable 3-D Terrain Visualization Through Reversible JPEG2000-Based Blind Data Hiding

Khizar Hayat, William Puech, and Gilles Gesquière

Abstract—In this paper a new method is presented for 3-D terrain visualization via reversible JPEG2000-based blind data hiding with special focus on data synchronization and scalability. Online real-time 3-D terrain visualization involves considerable amount of data. The process is essentially the mapping of the aerial photograph, called texture, onto its corresponding digital elevation model (DEM) implying at least two distinct data inputs. The presence of large disparate data necessitates a compression strategy on one hand and the integration of the DEM and texture into one unit on the other. Whilst the compression must accommodate the scalability requirement originated by the diversity of clients, the unification of data ought to be synchronous. For scalability this paper relies on the multiresolution nature of the DWT-based JPEG2000 standard whereas the synchronized unification of DEM with the texture is realized by the application of a wavelet-based data hiding strategy in the DWT domain. The proposed method is blind in the sense that only a secret key, if any, and the size of the original DEM are needed to extract the data from the texture image. We believe that this is one of the pioneering methods to propose scaleable embedding of DEM in the texture image. The method is cost effective, in terms of memory and bandwidths, which is an advantage, especially, in real-time environments when quicker transfer of data is required. The results of a 3-D visualization simulation effected with our method were encouraging and gave a useful insight to the effectiveness of our method in various bandwidth scenarios.

Index Terms—3-D visualization, data hiding, data synchronization, Digital Elevation Model (DEM), Discrete Wavelet Transform (DWT), Geographic Information System (GIS), JPEG2000.

I. INTRODUCTION

The advent of geo-browsers like Google Earth, World Wind and Virtual Earth has brought the terrain of earth, and even its neighboring planets in the case of World Wind, to one’s desktop. With each passing day the resolution of the aerial photographs and satellite imagery which is being made available to these browsers ameliorates. All this comes at a cost as far as memory requirements are concerned. For example, a 5 meters/pixel resolution aerial photograph of a small district requires well over ten gigabytes of storage, even in the JPEG2000 compressed form. Alongside the storage is the network factor, when it comes to online real-time 3-D visualization, since the data must be transferred from the server towards a client application in a timely way. In such a client/server environment the visualization quality becomes dependent on the payload, bandwidth, distant server and data transfer rate. To cope with the aforementioned challenges, any strategy that would not focus on data compression is unthinkable. But there is more to compression strategy than meets the eye since the clients are diverse in terms of resource capacity and requirements. Thus one client may have a powerful workstation while others may have just a smart-phone. Similarly one client may have a 100 Mbps connection whereas the other may be using a 56 kbps dial up modem. Still one client may want to view a precise location at high accuracy but others may just want to quickly browse through the globe. There is also a possibility that the network path of a client may involve at least one weak link or node. In between these extremes, there may be thousands of clients with varying capabilities and needs. Moreover, the preferences of a client may adapt to his capacity, e.g. a client handicapped by bandwidth may be more interested in real-time visualization without interruption than in high resolution. A synchronized mechanism is needed so that the server is in a better position to cater for each of its client. The wide spectrum of clients thus necessitates the data compression to be ideally scaleable for each hierarchy of clients. The JPEG2000 standard [10] serves this purpose since it is wavelet-oriented and wavelets have the property of multiresolution. The diversity of resolutions, that are resulting from a wavelet decomposition at various levels, is capable of offering the scaleability needed in the situations discussed.

The 3-D visualization information is in general stored in three different files: digital elevation model (DEM), an orthorectified photo and projection system and geo-referencing employed. The process of visualization in three dimensions is, essentially, the linking of the aerial photograph of the terrain, called texture, with the geometry of the terrain, called DEM. Each of the DEM coefficients represents the altitude of a particular square block of texture pixels and the process of visualization is the overlaying of texture over a regular triangle network [17], [23] obtained from the DEM. This linking is possible by geo-referencing the coordinates (longitude/latitude) of these elements depending on the scale and system of projection used. Rather than using two disparate DEM and texture files it is advisable to interleave them...
into a single file. For this purpose one can take a cue from the technique of data hiding and embed the smaller DEM data inside the larger texture image. The underlying assumption of our method is that the texture image must have at least 16 times more pixels than the total number of coefficients in the corresponding DEM.

It is to be noted that the context of this data hiding would be unconventional unlike steganography or watermarking as neither we are exchanging secret messages nor is copyrighting our goal. The embedding scheme must address the issue of correspondence between the texture and its DEM. In other words the integration of texture and its DEM into a single file must be synchronous. As far as JPEG2000 is concerned there are solutions like GeoJP2 [6] and GMLJP2 [15] but these serve the purpose partially since the data is not synchronized and there is an increase in the original size of the JPEG2000 file. It would be expedient to follow a different course, to have the advantage of synchronization without any change in the JPEG2000 file size and form, by applying a scalable data hiding algorithm. This approach would neither be XML-based, like GMLJP2, nor would it introduce some kind of Universally Unique IDentifier (UUID) boxes, like GeoJP2.

This work is a continuation of our previous efforts [7], [8] for the synchronized unification of the DEM and texture wherein lossless DWT decomposition level of both the message (transformed DEM) and the carrier (transformed Y plane of the texture) are the same before embedding. Moreover, in the current paper, the method is more detailed and the results have been improved. The crux of our argument is to realize a 3-D visualization system that will cater for the two desirable requirements, i.e., scalability and synchronized unification of 3-D data, without developing any new proprietary file format and maintaining compression performances. For scalability the DWT-based JPEG2000 standard can be relied upon for its multiresolution characteristic due to wavelets. In addition JPEG2000 is the standard that is fast establishing itself. The synchronized integration of the disparate 3-D data into one whole is achievable through the application of a perceptually transparent data hiding technique in the transform domain. All this crystallizes to the proposal of an LSB-based strategy that would embed the lossless transformed DEM in the corresponding transformed luminance component of texture of the lossless JPEG2000 coding pipeline. For the extraction step, the proposed method is blind and only the size of the original DEM is needed for extraction.

The rest of the paper is arranged as follows. Section II presents the essential concepts and previous work relevant to our approach. Our method is explained in Section III while the results which we obtained are elaborated in Section IV. Section V concludes the paper.

II. 3-D TERRAIN VISUALIZATION, JPEG2000, AND DATA HIDING

This work relies on a JPEG2000-based data hiding technique in order to achieve synchronous and scalable 3-D terrain visualization. In this context it would be worthwhile to present the notions of 3-D terrain visualization (Section II-A) and JPEG2000 (Section II-B). Alongside, related work on data hiding in the wavelet domain is highlighted in Section II-C whereas Section II-D is dedicated to a description on the integration of geographical data into a JPEG2000 format file.

A. 3-D Terrain Visualization

For years the geospatial professionals thought of mapmaking as inventing ways to flatten Earth’s 3-D surface onto a 2-D map. The various methods and projection systems which were developed are still far from reality. With the advent of 3-D computer graphics it became easier to create 3-D computer models to view different 3-D objects from various angles as well as rotate, zoom in and out, fly through and manipulate them. However, the chronic challenge persisted because the viewer just observed a snapshot of the 3-D models projected to a 2-D computer screen. The recent years’ technological developments have now made it possible to create realistic 3-D terrain models from scanned contour maps and other data sources.4 The popularity and importance of 3-D terrain visualization is increasing day by day in many areas, for example decision making, 3-D urban models, flight and driving simulations, and more generally, multiplayer applications.

Geographic data can be broadly classified into four fundamental classes: raster images, vector data, elevations and spatial databases. Images include aerial photos, scanned maps, satellite imagery and the like. Aerial photographs are the starting point for many mapping projects. By vector data is meant the traditional geometric structures like polylines, points, and polygons that have been used to represent roads, streams, power lines, lakes, county boundaries and topographic lines, on a particular scale. In digital form (e.g. digital line graphs) this representation has the advantage of having files much less heavier than images. Moreover such a data can be resized without any loss of clarity. Elevations are usually in the form of grid of terrain heights recorded at regularly spaced horizontal intervals: the result being a DEM. DEMs are used to create 3-D images of a landscape when overlaid by the corresponding 2-D aerial photos or satellite images thus producing, for example, lighting effects to reveal hills and valleys. The repositories of information like census data, resource inventory data and spatial event data constitute spatial databases that are helpful to a mapmaker in special cases, e.g. highlighting regions in the map or forecasting changes in the terrain.

Essentially, 3-D terrain representation implies to use two kinds of data combined for the visualization [19].

- Height field data which corresponds to the elevation of terrain [Fig. 1(a)]. It is defined by a grid of points separated by a given step. These points are used to generate the geometry and are connected by triangles [Fig. 1(b)].
- Aerial photographs can be acquired in various spectral domains such as visible or infrared. Theses are used to map 3-D triangles previously computed [Fig. 1(c)].

In order to get the DEM, the simplest solution consists of using a uniform discretization of the terrain. This gives a good

accuracy but leads to a quite large number of triangles, thus implying a considerable memory cost for the 3-D visualization of a large area. Many methods have been proposed to reduce the number of triangles provided by the uniform discretization, while preserving a good approximation of the original surface. One of the main approaches consists of obtaining an irregular set of triangles: Triangulated Irregular Network (TIN). A great deal of work has been done in order to create the TIN starting from a height field by using, for example, a Delaunay triangulation [5] or a progressive mesh representation [9]. Hierarchical representations of these triangulations have been proposed, thus making it possible to introduce the concept of level of detail [4]. Consequently one can obtain various levels of surfaces with an accuracy which is similar to a uniform grid but with a lower number of triangles.

To obtain a three dimensional visualization, one has to bind the texture to the terrain DEM. This bond is allowed by georeferencing coordinates (longitude and latitude) depending on the projection system used. The information is usually stored in three different files; one for the DEM, one for the texture and one for the geo-referenced coordinates. By mapping the satellite or aerial image on the corresponding 3-D terrain model. Thus, a realistic 3-D model can be created with the elevations and the surface texture.

In our work we have relied on the data provided by IGN\(^5\) France which consists of vectorial data in the form carto, raster images in the form BD Ortho or BD Scan and DEM usually at 50 m resolution. We seek to put in place the correspondence between the texture and its DEM. Using a uniform grid would allow this mapping since one would be able to do the similar thing for the ground and the images. The proposed method is about the interleaving of the above data to get a single file.

**B. Discrete Wavelet Transform and JPEG2000**

In standard image compression techniques, one of the essential steps is the domain transformation. The transform results in the decorrelation of the pixels. Pixel energy is thus compacted into a small number of coefficients. The idea is to enable the quantization step to trim the samples selectively, i.e., irrelevant samples must be quantized more heavily than the relevant ones [28]. One aspect of the success of JPEG [24] is in the efficiency of its transform, i.e., discrete cosine transformation (DCT) applied to each image block of $8 \times 8$. But the use of block-based transforms rests on the unrealistic assumption of the independence of blocks.

Of the alternatives available to the block-based transforms the one that got the approval of JPEG2000 [10] proponents is the discrete wavelet transform (DWT). The key being its multiresolution nature resulting in subbands containing some level of detail derived from the whole image or at least a considerably large tile, if the image is of very large size. The quality in such a situation is incremental as the lowest subband has the most important and relevant information and the higher subbands have finer details. Most of the energy is thus compacted into a few large transform coefficients—an entropy coder easily locates these coefficients and encodes them. DWT offers better energy compaction than the DCT without any blocking artifact after coding. In addition the DWT decomposes the image into an L-level dyadic wavelet pyramid. The resultant wavelet coefficient can be easily scaled in resolution as one can discard the wavelet coefficients at levels finer to a given threshold and thus reconstruct an image with less detail.

The multiresolution nature of DWT, therefore, makes it ideal for scalable image coding. After the color transformation, the DWT decomposes each component (luminance Y and chrominance Cr and Cb) into numerous frequency bands called subbands. For each level, DWT is applied twice, once row-wise and hence four subbands result: 1) horizontally lowpass $(L)\$, 2) horizontally lowpass and vertically lowpass $(HL)$, 3) horizontally highpass and vertically lowpass $(HL)$ and 4) horizontally and vertically highpass $(HH)$. Let us consider the input image signal (or tile-component signal if image is large) as the $L_0$ band. A $(R-1)$-level wavelet decomposition is associated with $R$ resolution levels. Each subband of the decomposition is identified by its orientation (i.e., $LH$, $HL$, $HH$, and $HH$) and its corresponding decomposition level $(0,1,\ldots,R-1)$. At each resolution level (except the lowest) the $LL$ band is further decomposed. Thus the $L_0$ band is decomposed to yield the $L_1$, $LH_1$, $HL_1$, and $HH_1$ bands. Then, at the next level, as illustrated in Fig. 2(a), the $L_1$ band is decomposed. This process is repeated until the $L_{R-1}$ band is obtained. If no transform is applied $(R = 1)$ then there

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\(^5\)http://www.ign.fr/.
is only one subband: the $LL_0$ subband. A level-2 wavelet decomposition of the image Lena, given in Fig. 2(b), is illustrated in Fig. 2(c).

Right from the beginning, JPEG2000 has been supporting two kinds of transforms: the reversible integer-to-integer Daubechies (5/3) and the irreversible real-to-real Daubechies (9/7) [3], [27] with the former being lossless and the latter being lossy. The $2-D$ transformation can then be carried out by separately applying the $1-D$ version horizontally and vertically one after the other. Let the $1-D$ (pixel row or pixel column) input signal be $S_1, S_2, S_3, \ldots, S_n$ then for the reversible 5/3 wavelet transform the lowpass subband signal $L_1, L_2, L_3, \ldots, L_n/2$ and highpass subband signal $H_1, H_2, H_3, \ldots, H_n/2$ are given by

$$
\begin{align*}
H_i &= S_{2i+1} - \frac{3}{4}(S_{2i+2} + 2S_{2i}) \\
L_i &= S_{2i} + \frac{1}{2}(H_i + H_{i-1}) + \frac{1}{2}
\end{align*}
$$

In a simplified way, a typical JPEG2000 encoder\footnote{http://www.ece.uvic.ca/~mdadams/jasper/;} consists of the following steps [28] which are illustrated in Fig. 3.

1) Preprocessing such as tiling and shifting the origin of the pixel values to 0 by subtracting 128.
2) Intercomponent transform in the form of irreversible or reversible color transform to pass from RGB space to YCrCb space.
3) Intracomponent transform that may be lossy or lossless.
4) Quantization which decreases the size of the large coefficients and nullifies the small ones.
5) Tier 1 coding when the quantized coefficients are partitioned into rectangular code blocks and each is subjected independently to three coding passes. This step involves entropy coding too.
6) Tier 2 coding which is the packetization step whereby the code pass data is converted to packets—these packets are combined to get the final image in the JPEG2000 format.

It must be noted that in a JPEG2000 coding pipeline there are two primary sources of data loss. One is obviously quantization and the other is the stage in tier-1 coding when a decision is made about the exclusion of certain coding passes from the final JPEG2000 file. For the method proposed in this paper, the scalability prospects offered by JPEG2000 in the form of multisresolution is to our advantage, especially in the client/server environment.

\subsection*{C. Data Hiding in the Wavelet Domain}

Data hiding is an established field and that is why a lot has been written about it \[2\], especially for the last two decades. We, therefore, focus on the literature about wavelet-based data hiding which is again very extensive and one is compelled to be brief. Data hiding deals with embedding an information, called message, inside some host signal, like image, sound or video, called cover. The message may be small and robust as in the case of copyright protection in the form of watermarking or it may be large, critical and statistically invisible as in steganography. Four factors \[1\] characterize the effectiveness of a data hiding method, namely hiding capacity, perceptual transparency, robustness and tamper resistance. Hiding capacity refers to the maximum payload that can be held by the cover. Perceptual transparency ensures the retention of visual quality of the cover after data embedding. Robustness is the ability of the cover to withstand various signal operations, transformations and noise whereas tamper resistance means to remain intact in the face of malicious attacks. The relative importance of these four factors depends on the particular data hiding application. For example,
for visually sensitive applications perceptual transparency becomes very important. Domain-wise, embedding can be carried out in the spatial domain or the transform domain. Pixel or coefficient allocation for data embedding may be regular (e.g. every $k^{th}$ pixel) or irregularly distributed (e.g. pseudo-random). Probably the most preferred pixel allocation is by running a pseudo-random number generator (PRNG) using some secret key as a seed. Finally, an embedding method is blind if data extraction by the recipient does not require the original cover.

Many methods have been proposed in the literature for wavelet-based data hiding but few of these are compatible with the JPEG2000 scheme. According to [21], data hiding methods for JPEG2000 images must process the code blocks independently and that is why methods like inter-subband embedding [12] and those based on hierarchical multiresolution relationship [14] have not been recommended. In the same breath the authors of [21] rejects the correlation-based method [29] as well as non-blind methods. The reason for this is the limited number of coefficients in a JPEG2000 code-block that are likely to fail in reliably detecting the hidden information in a single independent block. There are methods [13], [30] for embedding invisible watermarks by adding pseudo-random codes to large coefficients of the high and middle frequency bands of DWT but the methods have the disadvantage of being non-blind. The blind scheme proposed in [26] is to integrate data hiding with the Embedded Block Coding with Optimized Truncation (EBCOT) and embed data during the formation of compressed bit stream. The scheme is claimed to have robustness and good perceptual transparency. One particular technique [20] embeds the watermark in the JPEG2000 pipeline after the stages of quantization and region of interest (ROI) scaling but before the entropy coding. For reliability purposes the finest resolution subbands are avoided. A window sliding approach is adopted for embedding with the lowest frequencies having higher payload. Piva et al. have proposed an authentication scheme that embeds an image digest in a subset of the subbands from the DWT domain [25]. The image digest is derived from the DCT of the level 1 DWT LL subband of the image. The resultant DCT coefficients are scaled down by quantization and ordered from most to least significant through a zig-zag scan. A most significant subset, after discarding the DC coefficient, is quadruplicated for redundancy and then rescaled and scrambled by using two different keys. This gives the message which is substituted to the subbands selected from a set obtained by the further wavelet decomposition of the level 1 HL and LH subbands of the original image. One blind method [16] transforms the original image by one-level wavelet transform and sets the three higher subbands to zero before inverse transforming it to get the modified image. The difference values between the original image and the modified image are used to ascertain the potential embedding locations of which a subset is selected pseudo-randomly for embedding. The method of Kong et al. embeds watermark in the weighted mean of the wavelets blocks, rather than in the individual coefficient, to make it robust and perceptually transparent [11].

While explaining their method of embedding biometric data in fingerprint images, Noore et al. argue against the modification of the lowest subband to avoid degradation of the reconstructed image as most of the energy is concentrated in this band [22]. Instead they propose to redundantly embed information in all the higher frequency subbands.

### D. Geographical Metadata Integration into the JPEG2000 Codestream

As far as the insertion of GIS information, as metadata, into a JPEG2000 coding pipeline is concerned there have been limited efforts to date. There are already efforts like GeoJP2 [6] and GMLJP2 [15] for the integration of geographical data with the related aerial photographs. The GeoJP2 is a GeoTIFF-inspired method for adding geospatial metadata to a JPEG2000 file. The GeoTIFF specification\(^7\) defines a set of TIFF tags provided to describe all cartographic information associated with TIFF imagery that originates from satellite imaging systems, scanned aerial photography, scanned maps and DEM. Its aim is to allow for tying a raster image to a known model space or map projection, and to describe those projections. GeoTIFF does not intend to become a replacement for existing geographic data interchange standards. GeoTIFF uses a small set of reserved TIFF tags to store a broad range of georeferencing information, catering to geographic as well as projected coordinate systems needs. It uses numerical codes to describe projection types, coordinate systems, datums and ellipsoids.

The additions made to the box-based JPEG2000 format are two UUID boxes, namely, the GeoTIFF box and the optional world file box. The former contains a degenerate GeoTIFF file and the resultant JPEG2000 file have the same level of geospatial metadata as is provided by the GeoTIFF standard. The mechanism is simple using the widely supported GeoTIFF implementations but the introduction of new UUID boxes have the disadvantage that there is an increase in the original JPEG2000 file size. The GMLJP2 envisages the use of the Geography Markup Language (GML) within the XML boxes of the JPEG 2000 data format in the context of geographic imagery. A minimally required GML definition is specified for geo-referencing images while also giving guidelines for encoding of meta-data, features, annotations, styles, coordinate reference systems, and units of measure as well as packaging mechanisms for both single and multiple geographic images. DEMs are treated the same way as other image use cases whereas coordinate reference system definitions are employed using a dictionary file. Thus DEM is either provided as TIFF file and its name is inserted between proper GML tags or its points are directly inserted into the GMLJP2 file. In the former case, there is no reduction in the number of files whereas in the latter case the amount of data is increased.

### III. THE PROPOSED METHOD

As described in Section II-A, the 3-D visualization needs more than one file: the DEM and the image of texture being the essential. To coalesce this disparate data to a single JPEG2000\(^7\)http://www.remotesensing.org/geotiff/spec/contents.html.
file, while taking into account the requirements of synchronization and scalability, we propose a data hiding-based method. An overview of the method is given in Section III-A. Section III-B presents the transformation of the DEM and the texture. The embedding is explained in Section III-C while the decoding and 3-D visualization are elaborated in Section III-D.

A. Overview

In this work the thrust is on the performance of the proposed method by the inclusion/exclusion of high frequency subbands in the DWT resolution hierarchy rather than modifying the data by quantization or tier-1 coding. That is why the JPEG2000 encoder has been set at the lossless mode and the wavelet transform is integer-to-integer. As already stated, the scalability prospects offered by JPEG2000 in the form of multiresolution is to our advantage, especially in the client/server environment. In a nutshell, our method is the LSB-based embedding of lossless wavelet transform DEM into wavelet transformed luminance (Y) plane of texture extracted from a reversible JPEG2000 coding pipeline after the DWT step. Because of the small embedding factor needed for our application, we have chosen to embed the data only in the Y component in order to have a fast extraction and to preserve a better bitrate. The marked Y plane of texture is then reinserted to the JPEG2000 coding pipeline. Two factors have been taken into account in the course of embedding. First, the level of transform in both the cases, i.e., DEM and texture, is the same. Second, there is a synchronization in embedding: low subband DEM coefficients are to be embedded into those of low subband of texture while higher ones in the higher. The method is blind since there is no need of original texture image at the decoding side. The final image format is thus JPEG2000 compliant implying that there is no need of additional technology for the proposed method. A generalized scheme of the method is given in Fig. 4.

B. Transformation to Get the Cover and the Message

The two files of DEM and texture are the inputs whereby the former would process into the message and the latter would give the cover in the data embedding step. The DEM consists of 16 bit coefficients that represent the elevations in the form of altitudes. Each of these coefficients corresponds to a particular square block of pixels in the texture. Texture is already a color image in some standard format with RGB components. From the size of the DEM we can calculate the ratio between a DEM coefficient and its associated block of texture. Lossless DWT is applied, in isolation, to the DEM at a particular level, say L that corresponds to \( R = L + 1 \) resolutions. The resultant coefficients constitute the bits of our message \( M \) in the traditional sense of data hiding. In fact, to represent the DEM in the spatial domain, only 14 bits per coefficient are necessary (altitude between \(-8192 \text{ m} \) and \(+8191 \text{ m}\)), but after the DWT 16 bits are necessary to represent each coefficient. Simultaneously, the RGB space texture image is introduced to a standard JPEG2000 encoder. The encoder, after necessary preprocessing, passes it from RGB space to the luminance-chrominance (YCrCb) space. In the next step, i.e., DWT step, the three YCrCb components are reversibly transformed at level \( L \). As can be seen in Fig. 4, the encoding path is diverted, after the DWT step, as far as the luminance (Y) image is concerned. The transformed Y component is our cover \( C \). Note that whether it is the transformation of the DEM or it is the JPEG2000 encoder for texture, the implementation of DWT is based on the lifting method [18] that employs the JPEG2000 supported reversible Daubechies (5/3) filter [3].

C. Embedding of the Data

This section explains the embedding of the message \( M \) into the cover \( C \) to get the marked cover \( C' \). It has been ensured that both \( M \) and \( C \) are at the same level of transformation and embedding is according to the synchronization of subbands as illustrated in Fig. 4. One important point to mention is that in this work neither any copyright problem is solved nor is there any threat to the security of message. What we want is to carry out embedding without significant loss in the visual quality of the 3-D rendering. At the same time, the hiding capacity is also important since day by day the resolution quality is improving at the expense of data size. Hence, of the traditional requirements of data hiding, we are more particular about perceptual transparency and payload which implies that robustness and tamper resistance are secondary in importance.

From a \( N \times N \) pixel texture image and the corresponding map of \( m \times m \) altitudes, we deduce the embedding factor \( E = m^2/N^2 \) altitude coefficients per pixel. To ensure a spatial coherence between the altitudes and the texture, the cover \( C \) is

![Fig. 4. Description of the method: embedding transformed DEM coefficients into the transformed coefficients of each Y texture subband.](image-url)
partitioned into square blocks of \(1/E\) coefficients for data embedding and every such block would hide one transformed altitude coefficient of the message \(M\). We thus achieve a synchronization in the embedding as far as the incremental levels of the wavelets are concerned, i.e., low resolution coefficients of the altitude map are embedded in the low resolution subbands of texture whereas high resolution coefficients of the altitude map are embedded in the high resolution subbands. In this way the transmission of the part concerned with the low resolution of the texture map enables us to directly access the corresponding low resolution part of the altitude map.

For perceptual transparency, an embedding strategy based on least significant bit (LSB) substitution is proposed. The data embedding is carried out by modifying the LSBs of a certain number of coefficients of the luminance plane of the texture. An allocation policy is needed to determine which coefficients are to carry the message. These coefficients are chosen by using a PRNG with a seed, \(K\), as a seed. The use of a secret key allows us to restrict access to DEM data. Since the chosen JPEG2000 coding is reversible the hidden message can be extracted losslessly. A high level description of the embedding strategy is outlined in Algorithm 1.

**Algorithm 1** The embedding strategy

1: **begin**
2: **read** \(C\) which is level-\(L\) transformed Y texture from the JPEG2000 coding pipeline
3: **read** the corresponding DEM file as an image
4: **apply** lossless DWT to DEM at level \(L\) to get \(M\)
5: **for** each subband of \(C\) and its counterpart in \(M\) **do**
6: **partition** the \(C\) subband into square blocks in relation to the \(M\) subband
7: **initialize** a PRNG with a seed \(K\)
8: **for** each correspondence of \(C\) subband block \(B_{uv}\) and its \(M\) subband coefficient \(d_{uv}\) **do**
9: **for** \(k = 0\) to 15 **do**
10: generate the index which is the next pseudo-random number to get \(i, j\)
11: get the \(C\) subband coefficient \(t_{ij}\)
12: substitute the LSB of \(t_{ij}\) with the \(k^{th}\) bit of \(d_{uv}\)
13: **end for**
14: **end for**
15: **end for**
16: **label** the block-wise marked \(C\) as \(C'\)
17: **end**

In Fig. 5, we illustrate the low level detail of the embedding procedure. Let the \(m \times m\) transformed DEM coefficients are represented by \(d_{uv}\), where \(u, v \in \{0, \ldots, m - 1\}\). The \(N \times N\) transformed Y plane of texture is consequently partitioned into \(m^2\) blocks \(B_{uv}\), with \(u, v \in \{0, \ldots, m - 1\}\). Each of \(B_{uv}\) is composed of \(r^2 = N^2/m^2\) coefficients \(t_{i, j}\) with \(i, j \in \{0, \ldots, r - 1\}\). Let \(b_0, b_1, b_2, \ldots, b_{16}\) and \(\beta_1, \beta_2, \beta_3, \ldots, \beta_4\) be the bitwise representations of 16 bits \(d_{uv}\) and the 8 bit \(t_{ij}\), respectively. Embedding involves the hiding of each of the 16 \(b_{k}\) bits in as many different coefficients \(t_{ij}\) of the given \(B_{uv}\) block. These coefficients are selected by running a PRNG using the key \(K\) for one time initialization.

The PRNG that will generate 16 numbers per \(B_{uv}\) which correspond to the allocated \(t_{ij}\) coefficients. Care must be taken to avoid collisions so that the same subscript is not generated twice. One of the \(b_{k}\) bits would substitute the LSB of the allocated \(t_{ij}\) coefficient \(\beta_1/\beta_2/\beta_3/\beta_4\) that would yield \(t_{ij} = t_{ij} + \beta_1/\beta_2/\beta_3/\beta_4\) after embedding. Hence 16 of the \(r^2\) coefficients of each of the embedded block would be changed from \(t_{ij}\) to \(t_{ij}'\). The procedure mentioned in the previous lines is followed for each block of the transformed Y texture and for each subband of \(C\), as described in Algorithm 1.

The resultant embedded image, \(C'\), i.e., marked Y plane of the texture in the wavelet domain, is then reinserted into the JPEG2000 pipeline at the same point from where it was extracted. The final encoded image thus carries the DEM coefficients hidden in some DWT coefficients.

**D. Extraction and Scalable 3-D Reconstruction and Visualization**

The above coded image can be utilized like any other JPEG2000 image and sent across any communication channel. The decoding is the reverse of the above process. Since the method is blind, only the secret key \(K\) is needed, along with the size of the original DEM, to recover the hidden DEM coefficients at the receiving end. Just before the inverse DWT stage of the JPEG2000 decoder, the DEM can be extracted using the above mentioned partitioning scheme and PRNG with \(K\) as the seed. All the DEM bits are LSBs of the coefficients, indexed by the PRNG sequence, in the luminance plane of the carrier texture.

One advantage of the method is in the fact that the DEM and texture can be reconstructed at the original size, even if we have only a small subset of the coefficients of the cover. The resolution scalability of wavelets and the synchronized character of our method enable a 3-D visualization even with a number of layers smaller than the number of original resolution layers as a result of partial or delayed data transfer. The method thus enables to effect a visualization from a fraction of data in the form of the lowest subband, of a particular resolution level. The idea is to have a 3-D visualization utilizing lower frequency \(3L' + 1\) subbands out of the initial \(3L + 1\) subbands \((L' \leq L)\), by padding a 0 for each of the coefficient of the rest of the high frequency \(L - L'\) parts. Indeed, it is always possible to stuff 0’s for the higher bands. Hence a reconstruction with level \(L'\) lowest frequency subband is effected with just \((1/L')\times100\%\) of the count of the original coefficients: the result would be what is called level \(L\) approximation image. With this padding approach, irrespective of the number of subbands used for the reconstruction, the reconstructed DEM and texture have the same spatial sizes as the original ones. The reconstruction procedure
from a JPEG2000 codestream of the marked texture is depicted in Fig. 6.

It is important to note that level \( L \) wavelet decomposition corresponds to \( R = L + 1 \) resolution levels in the range \( L \) to 0 in ascending order of quality as well as quantity of data. This implies \( R \) different visualizations of which the first one requires only the lowest \( LL_{R-1} \) subband. The second visualization would require four subbands which include the previous one, \( LL_{R-1} \), and three others namely \( LH_{R-1}, HL_{R-1}, \) and \( HH_{R-1} \). Seven subbands, \( LL_{R-1} \), \( \bigcup_{i=1}^{2} LH_{R-i} \), \( \bigcup_{i=1}^{2} HL_{R-i} \), and \( \bigcup_{i=1}^{2} HH_{R-i} \) constitute the data for third visualization. In general \( R^{th} \) visualization is based on \( 3(l - 1) + 1 \) lowest subbands \( LL_{R-1}, \bigcup_{i=1}^{2} LH_{R-i}, \bigcup_{i=1}^{2} HL_{R-i}, \) and \( \bigcup_{i=1}^{2} HH_{R-i} \). All the \( 3(R - 1) + 1 \) subbands are necessary for the highest quality \( R^{th} \) visualization.

In a loose sense, any given resolution is a superset of all the preceding ones. The scalability has its origin in the fact that one can have \( R \) different images of approximation. Choice can be dynamically made among these \( R \) different options depending on the client’s resources, constraints and requirements as well as network and distance considerations. A client with a powerful platform and high available bandwidth may be able to download all the data timely and decode the level 0 JPEG2000 image to get the highest quality visualization. On the other hand a client on a smart-phone and weak communication signal may have to be content with a small subset of subbands (Fig. 6) which it will stuff with 0’s for higher frequency bands during the decoding process to get the approximation rather than the original image with the improvement of signal he may have the luxury to go for higher quality. All this becomes more critical
in the real-time case since now the frame rate, for example, can become more important than the quality and one can compromise over latter to certain extent. In essence, even for a very small fraction of the number of initial coefficients, of the texture and its DEM, one can have a 3-D visualization that is considerably cost effective.

IV. RESULTS

This section has two parts. In Section IV-A we analyze the application of our method when applied to an example altitude map of 64 x 64 coefficients [Fig. 7(a)] associated with a 3200 x 3200 pixel texture [Fig. 7(b)]. For the purpose of comparison a 128 x 128 pixel detail of the above mentioned image of texture is presented in Fig. 7(c). Section IV-B is concerned with the 3-D visualization simulation with respect to another example that is to be demonstrated at high and low bitrates.

A. Analysis of the Method as Applied to a Real World Example

For the example illustrated in Fig. 7, each coefficient of the altitude is coded with 2 bytes implying the embedding factor of 1 coefficient per 50 x 50 pixels of texture. The application of a level 1 lossless wavelet transformation to the DEM results in Fig. 8(a). The corresponding transformed Y-plane of the texture [Fig. 8(b)] is extracted in situ from the JPEG2000 encoding process of the texture image. The same set of images for level 3 are illustrated in Fig. 8(c) and (d).

To analyze the quality of the embedded texture image, with respect to the original, the measure of PSNR (peak signal to noise ratio) has been employed:

\[
PSNR = 10 \log_{10} \frac{255^2}{MSE},
\]

where mean square error (MSE) is a measure used to quantify the difference between the initial image \( I \) and the distorted image \( I' \). If the image has a size of \( M \times N \) then

\[
MSE = \frac{1}{MN} \sum_{i=0}^{M-1} \sum_{j=0}^{N-1} (I(i,j) - I'(i,j))^2.
\]

In order to judge compression performance, a measure called bitrate, which is the amount of necessary bits per pixel (bpp), is utilized:

\[
Bitrate = \frac{\text{Compressed Image Size in bits}}{\text{Original Image Size in pixels}} \text{ in bpp}.
\]

Strictly speaking, DEM is a set of altitude coefficients rather than pixels which requires some modifications in the definition of the above measures. Hence, instead of bitrate, a measure we call bits per coefficient (i.e., amount of information per altitude coefficient) has been used. Since altitudes are expressed in meters, it would be better to use MSE in square meter unit for error measurement. For a more comprehensive explanation one can rely on the one dimensional version of root mean

Fig. 6. Decoding, data extraction and scalable 3-D reconstruction and visualization.
square error (RMSE) which is the positive square root of MSE: \( RMSE = \sqrt{MSE} \). Embedding of the transformed DEM in the transformed texture takes place according to the policy explained in Section III. It is worthwhile to note that, in general, the data embedding at level \( L \) decomposition takes place in \( 3L + 1 \) partitions. Hence for the DWT at level 1 [Fig. 8(a)] the embedding has been done in four partitions (\( LL_1, LH_1, HL_1 \) and \( HH_1 \)) whereas for level 3 wavelet decomposition, the embedding of data has been realized in ten partitions. The marked luminance plane of texture is reintroduced to the JPEG2000 coding pipeline at the point where it was extracted and thus the output is JPEG2000 compliant. No matter what is the level of decomposition \( L \), degradation in the texture image, due to data embedding, amounts to a mean square error (MSE) of 0.01 corresponding to a PSNR of 68.5 dB. This is attributed to the meager embedding factor of \( 6.4 \times 10^{-3} \) altitude coefficients per pixel since only one 16 bit DEM coefficient is embedded per 50 x 50 block of coefficients of the Y component of texture.

Fig. 9(a) shows an altitude map reconstructed from the coefficients extracted from a level 1 image of approximation (\( LL_1 \)) of the embedded texture image. The reconstruction has been done by stuffing 0’s in place of the three higher subbands and subsequently applying inverse DWT. Thus only 25% of the count of the initial coefficients have been used for reconstruction. The difference of this image with the original altitude is illustrated in Fig. 9(b). When the above process of reconstruction is applied to the level 1 lowest subband of the embedded texture image Fig. 9(c) is obtained. For comparison with the original example, the 128 x 128 pixel magnified part is shown in Fig. 9(d). The same sequence of four figures, i.e., a to d, is maintained in each of the Fig. 10–12 which corresponds to the reconstruction from levels 2 to 5 lowest subbands, respectively. For subjective analysis, one can visually compare the part c of Fig. 7, with the same of each of Fig. 9–12. There is certainly degradation in the visual quality but it is far more less in the face of the quantity of data utilized for reconstruction, e.g. level 3 reconstruction has been carried out with only 1.56% of the total coefficients. The degradations in the quality of texture are presented in Fig. 13 in the form of difference images in terms of the magnified part corresponding to Fig. 7(c).

Objectivity demands a quantitative comparison which we have done in terms of the images of difference by observing the measures, like MSE or PSNR, as a function of bitrate. The results are summarized in Table I for the DEM and Table II for the texture. The effectiveness of our method is revealed by the fact that even for a bitrate as low as 0.26 bpp (corresponds to level 3 approximation image of texture, Table II) one observes a PSNR of 25.47 dB corresponding to a RMSE for DEM of 22.02 meters (Table I). Given the fact that being computed from a small fraction of initial data, this error is tolerable if the observation is made from a high altitude. To elaborate further, MSE has been plotted as a function of bitrate for the texture.
Fig. 9. Reconstruction of the images from the approximation image at Level 1: (a) extracted altitude, (b) difference image between the original altitude and the extracted one, (c) texture, and (d) magnified part of texture corresponding to Fig. 7(c).

Fig. 10. Reconstruction of the images from the approximation image at Level 2: (a) extracted altitude, (b) difference image between the original altitude and the extracted one, (c) texture, and (d) magnified part of texture corresponding to Fig. 7(c).

Fig. 11. Reconstruction of the images from the approximation image at Level 4: (a) extracted altitude, (b) difference image between the original altitude and the extracted one, (c) texture, and (d) magnified part of texture corresponding to Fig. 7(c).

Fig. 12. Reconstruction of the images from the approximation image at Level 5: (a) extracted altitude, (b) difference image between the original altitude and the extracted one, (c) texture, and (d) magnified part of texture corresponding to Fig. 7(c).
Fig. 13. Difference between the original luminance and reconstructed texture [for the magnified part of texture corresponding to Fig. 7(c)] of (a) Level 1, (b) Level 3, and (c) Level 5.

### Table I

**Results Obtained for DEM After the Extraction and Reconstruction as a Function of the Used Data (for level 0, all of the transmitted data is used for reconstruction)**

<table>
<thead>
<tr>
<th>Approximation image</th>
<th>l5</th>
<th>l4</th>
<th>l3</th>
<th>l2</th>
<th>l1</th>
<th>l0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bits per coefficient</td>
<td>0.016</td>
<td>0.062</td>
<td>0.25</td>
<td>1.00</td>
<td>4.00</td>
<td>16.00</td>
</tr>
<tr>
<td>RMSE (dB)</td>
<td>72.92</td>
<td>49.33</td>
<td>22.62</td>
<td>8.90</td>
<td>3.60</td>
<td>0.00</td>
</tr>
<tr>
<td>PSNR (dB)</td>
<td>10.87</td>
<td>14.27</td>
<td>21.27</td>
<td>29.14</td>
<td>37.00</td>
<td>∞</td>
</tr>
</tbody>
</table>

### Table II

**Results Obtained After the Extraction and Reconstruction of the Texture as a Function of the Used Data in the Form of Embedded Texture**

<table>
<thead>
<tr>
<th>Approximation image</th>
<th>l5</th>
<th>l4</th>
<th>l3</th>
<th>l2</th>
<th>l1</th>
<th>l0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Compression ratio</td>
<td>1509</td>
<td>377</td>
<td>92</td>
<td>23</td>
<td>5.8</td>
<td>1.95</td>
</tr>
<tr>
<td>Bitrate (bpp)</td>
<td>0.016</td>
<td>0.064</td>
<td>0.26</td>
<td>1.06</td>
<td>4.14</td>
<td>12.31</td>
</tr>
<tr>
<td>MSE</td>
<td>297</td>
<td>246</td>
<td>185</td>
<td>108</td>
<td>42</td>
<td>0.01</td>
</tr>
<tr>
<td>PSNR (dB)</td>
<td>23.40</td>
<td>24.22</td>
<td>25.47</td>
<td>27.80</td>
<td>31.9</td>
<td>68.53</td>
</tr>
</tbody>
</table>

B. Simulation Example

To present an application of our method it would be worthwhile to run a practical visualization simulation. The inputs used in the simulation example are given in Fig. 17. The DEM (64 × 64) from Fig. 17(a) and its corresponding 3200 × 3200 aerial image [Fig. 17(b)] are subjected to our method. Two series of simulations were effected with one based on full resolution, i.e., level 0 approximation images, and the other on level four images of approximation. Some snapshots of the simulations, at regular intervals, from a transmitted image sequence of more than 300 images are presented.

Five different snapshots from the 3-D visualization of our example are illustrated Fig. 18 for level 0 (corresponding to a bitrate of 240 Mbps) and Fig. 19 for level 4 (corresponding to a bitrate of 640 kbps). The snapshots are at regular intervals when the distant observer is coming closer and closer to the terrain and such they are taken as a function of the decreasing aerial distance of the viewer from his point of focus. The viewer’s aerial position is the same for the two bitrates (240 Mbps in Fig. 18 and 640 kbps in Fig. 19) at a given interval. The difference is obvious but not glaring given the fact that the data of Fig. 19 corresponds to only 0.39% of the number of coefficients of the data of Fig. 18. This lower than expected degradation in quality motivate us to have an effective scalable visualization. For example a 3200 × 3200 aerial image requires 30 MB of storage employing a 240 Mbps bandwidth requirement if only one image is to be transferred per second. In other words a 100 Mbps connection would require 2.4 seconds for a single image to transfer and the same for wireless networks is around 1200, 625, 133 and 48 seconds for EDGE (200 Kbps), 3G (384 Kbps), HSDPA (1.8 Mbps), and WIFI (5 Mbps), respectively. A level 4 approximation of the same embedded image in JPEG2000 format would have a size in the order of 80 KB implying the requirement of 640 kbps for transferring one image per second. With EDGE one can transfer one such image in about 3 s and WIFI can transmit eight such images/s. Level 5 approximation may further reduce the payload and now one can transfer one image per second over EDGE and 32 images over WIFI making the latter suitable for video based streaming.

For the level 4 approximation, a closer examination of Fig. 19 reveals that of the DEM/texture pair it is the DEM which is affected the most in terms of quality. This means that the DEM is...
Fig. 14. Graphical display of variation in quality as a function of bitrate: (a) texture and (b) DEM.

Fig. 15. The 3-D surface representation using the extracted DEMs and obtaining their approximations at various levels. (a) Level 0 (all the data), (b) Level 1, (c) Level 3, and (d) Level 4.
more sensitive than the texture to a partial reconstruction. This sensitivity of DEM necessitates the fact that the level of wavelet decomposition could be lower for DEM than texture before embedding. Since the size of DEM file is much smaller than that of the texture, the lowest frequency subband at some level can be used for embedding. But this would undermine the perceptual transparency since the embedding density of the energy-richer part would be increased. Moreover, the synchronization management between DEM and texture would be more difficult and this could be costlier in terms of time.

V. CONCLUSION

In this paper we presented a new method for a scalable 3-D terrain visualization through reversible JPEG2000-based blind data hiding. This paper is focused on the topic of data synchronization and scalability. The results reveal that the proposed method offers at least three advantages. First is the synchronized integration of disparate 3-D data into one whole by the application of data hiding. The second advantage is the scalability in 3-D visualization through the utilization of JPEG2000 supported DWT. Last, but not the least, is the integrability of the method with the JPEG2000 encoders to result in a monolithic standalone JPEG2000 format file that eliminates the need to develop any additional technology or data format, thus implying portability and conformance which is asked by our industrial constraints. In addition the approach is cost effective in terms of memory and bandwidths. The results shown in the case of our examples are witness to this fact since even with a tiny number of coefficients a comparatively better 3-D visualization was effected. The resolution scalability of wavelets enables this 3-D visualization to improve incrementally with the reception of higher frequencies/subbands. Besides, this property is helpful in real-time environment when quicker transfer of data is required. The results of 3-D visualization simulation give a useful insight.
to the effectiveness of our method in various network conditions.

In the continuation of this work it would be worthwhile to
develop a method based on lossy wavelets to further decrease
bitrate. This option will however eliminate, to a considerable
extent, the possibility of very high quality visualization since
the lossy case is not fully reversible. A situation may thus arise
that losing details of texture becomes less important than that
of DEM. Using a desynchronized algorithm would be a good
way and should be taken into consideration in the near future.
The LSB-based embedding strategy adopted in this work has
to be reconsidered for the lossy case and it will be important to
explore some other embedding strategies, like the spread spectrum
embedding [2], in order to keep DEM quality high for the recon-
struction. As far as triangulation is concerned, there is also every
likelihood of using a non-uniform grid on various levels of de-
tails, thus allowing a considerable reduction in the number of tri-
angles necessary for a good representation of the terrain. In this
paper links between tiles are not managed but our future focus
is likely to be on the strategies to generate a soft transition be-
tween several tiles without cracks. In future, the streaming man-
agement between the server and its clients is also being mulled.

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Fig. 18. Snapshots of the 3-D visualization simulation based on level 0 (for 240 Mbps) images of approximation extracted and reconstructed from the DEM embedded texture.

Fig. 19. Snapshots of the 3-D visualization simulation based on level 4 (for 640 kbps) images of approximation extracted and reconstructed from the DEM embedded texture.


Khizar Hayat was born on June 3, 1971 in Turlandi, Swabi, Pakistan. He received the M.Sc. (chemistry) degree from the University of Peshawar, Pakistan, in 1993. Since 1995, he is working as a Lecturer in Higher Education Department, NWFP, Pakistan. During this period, he was awarded a scholarship in 2001 by the Government of Pakistan and received the M.S. degree in computer science from Muhammad Ali Jinnah University, Karachi, Pakistan, in 2004. He also received the “Master 2 by Research (M2R)” degree in computer science from the University of Montpellier II (UM2) France. He is currently pursuing the Ph.D. degree at LIRMM (UM2) under the supervision of Dr. William Puech (LIRMM) and Dr. Gilles Gesquière (LSIS - University of Aix-Marseille) with a scholarship from The Higher Education Commission of Pakistan. His topic of research is scalable online visualization through dissimulated integration of 3-D terrain data. His areas of interest are image processing and data hiding.

William Puech was born in December 1967 in France. He received the diploma of Electrical Engineering from the University of Montpellier, France, in 1991 and the Ph.D. degree in signal-Image-speech from the Polytechnic National Institute of Grenoble, France, in 1997.

He started his research activities in image processing and computer vision. He served as a Visiting Research Associate to the University of Thessaloniki, Greece. From 1997 to 2000, he had been an Assistant Professor in the University of Toulon, France, with research interests including methods of active contours applied to medical images sequences. Since 2000, he is Associate Professor at the University of Montpellier, France. He works now in the LIRMM Laboratory (Laboratory of Computer Science, Robotic and Microelectronics of Montpellier). His current interests are in the areas of protection of visual data (image, video and 3-D object) for safe transfer by combining watermarking, data hiding, compression and cryptography. He has applications on medical images, cultural heritage, and video surveillance. He is the head of the ICAR team (image and interaction).

Gilles Gesquière received the Ph.D. in computer science from the University of Burgundy, France, in 2000.

He is currently an Assistant Professor at the LSIS Laboratory, Aix-Marseille University, France. His research interests include geometric modeling, 3-D visualization and deformation. He is currently working on projects focused on 3-D geographical information systems.