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Considering Floating Contact and Un-Modeled Effects for Multi-Contact Motion Generation

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Abstract—In this paper, we plan robotic multi-contact non-gaited motion by solving an overall optimization problem. Our algorithm takes as input the contact stances, the model of the robot and its environment, and generates the joints trajectories that achieve multi-contact motion under explicit constraints such as joint position, velocity and torque limits, equilibrium and eventually other task objectives. We improve our previous work in order to consider floating contacts for which some components of the contact position and/or orientation are not specified. We also discuss how, in practice, we bridge theoretical computations based on a rigid model of the robot to actual experiments by considering additional constraints during the optimization process.

Index Terms—Humanoid robots, multi-contact, floating contact, flexibilities

I. INTRODUCTION

Recently, there has been an increasing interest in planning non-gaited motion where a humanoid robot is allowed to contact the environment with any possible part of its body to support motions in bulky and uneven spaces. For example, [1], [2] developed a contact-before-motion planning algorithm that generates a sequence of contacts for such problems. Complex examples have already been successfully experimented on a real HRP-2 robot [3]. However, in these experiments, the motion between two successive contacts, namely the transitions, was not fully dynamic. For some classes of motions, such as walking, we can use a model reduction to compute trajectories. In [4]–[6], the entire robot is assumed as an inverted pendulum having a mass or the so called cart table model. Model reduction under additional constraints allows fast motion planning from which whole body motion is generated in a latter stage. Since the generated trajectories are computed based on and for such simplified models, there is no guarantee that its expansion to whole body motion is always possible.

Multi-contact non-gaited motion uses non-stereotypical key postures. Subsequently, model reduction is not beneficial because the COMs height does not hold within a small interval range, the number of the supporting contacts varies, it is often not possible to predict non-collisions or auto-collisions, or assume that torque and joint limits will not be reached. For all these reasons, planning safe non-gaited general multi-contact motion based on models reductions is extremely difficult.

Computing dynamic motions for complex robotic systems including multiple contacts is still an open issue. Motion planning based on probabilistic methods proved to be very efficient in practice. Yet, there are tasks that require the robot to exploit dynamical effects, or reach its limits in terms of capabilities and performances. Example of such tasks are kicking motions [7], [8], fast motion with collision avoidance [9] or lifting heavy objects [10]), etc. Due to their complexity, these extreme tasks are impossible to achieve by state-of-the art planning or local control method [4], [11], [12]. Generating off-line explicit and cost optimal trajectories using full-body model is most often the only and the safest option.

Nowadays, several methods emerge to generate full body single-contact motions [8], [13]. But multi-contact motion has always been considered as separate piecewise motions between fixed contacts that are connected afterwards.

Fig. 1. The robot has to put the ball in the box behind the desk. The motion and the contact position of the left are optimized.

In our recent work [14], we proposed a method to generate full dynamic multi-contact motions between sequences of contacts, including dynamic transitions. In this paper, we propose variants to our algorithms in order to include floating contacts, where some components of the contact position and/or orientation are not specified as presented in Figure 1. We also discuss more thoroughly the difficulty to bridge the optimization computations based on a perfect model simulation to the actual implementation and experimentation on the humanoid robot HRP-2 [15]. Despite a successfull simulations, some obtained motions were not successfully replayed in actual experiments. However, with ad-hoc tuning and addition constraints these failures could finally be recomputed and replayed successfully.
II. PROBLEM STATEMENT

Here, we introduce the basics in terms of terminology, notations, and the general formulation of the optimization problem.

A. The motion planning problem

The motion planning problem is to find the best joint trajectories \( q(t) \) that minimize a cost function an ensure sets of continuous inequality constraints \( g \), continuous equality constraints \( h \) and discrete inequality constraints \( z \). In order to make the problem computationally solvable, most of the methods reduce such complexity by defining a parameters set \( P \in \mathbb{R}^N \) that give at least a parametric shape for the functions \( q(t) \) to be found. Based on prior work in robotic, e.g. [13], we made the choice to shape the joint trajectories with clamped uniform cubic B-Splines curves. Subsequently, we have a finite set of B-splines’ control points that constitute the set of optimization parameters. For the choice we made, we have \( q_i(t) = \sum_{j=1}^m b_j(t) \times P_{i,j} \).

The motion planning problem reduces into finding the best parameter set \( P \in \mathbb{R}^N \) such that:

\[
\begin{align*}
\arg\min_{P} & \quad C(P) \\
\forall i, \forall t \in [\Delta_j] & \quad g_i(P, t) \leq 0 \\
\forall j, \forall t \in [\Delta_j] & \quad h_j(P, t) = 0 \\
\forall t_k \in \{t_1, t_2, ..., t_n\} & \quad z_k(P, t_k) \leq 0
\end{align*}
\] (1)

The problem 1 is called a Semi Infinite Programming (SIP) problem since it deals with a finite set of variables and a set of continuous constraint equivalent to infinite sets of constraints [16]–[18].

B. Solving SIP

In most cases, SIP is solved using a time-grid discretization of the constraints, e.g. [16]–[18]. As discussed in [7], [19], it is not easy to set a priori a time-grid discretization which guarantees that the constraints hold in-between a pair of sample time-point. Even if in practice, this could be checked a posteriori, we present another interface that accounts for continuous constraints evaluation in a guaranteed way, as presented hereafter.

We believe\(^1\) that it is better to use a solver from on-the-shelf available ones since the theory is not enough to provide the necessary tuning and implementation tricks that tackle efficiently numerical problem. We also take this policy by using the IPOPT solver [20]. IPOPT is free; it handles large non-linear optimization problems; it has a C++ interface, and was used in [7], [8].

C. Dealing with Continuous Constraints

To solve the problem (1) without using a time-grid discretization, in [14], we ensured the joint position and velocity limits through constraints on the control points and propose a time-interval discretization within which we approximate the constraints and the cost function using Taylor polynomials. Thus, all the state variables of the robots are approximate over a time-interval by:

\[
\forall t \in [\Delta t] \quad f(t) \approx \sum_{i=0}^n a_i(P) \times t^i
\] (2)

The continuous equality constraints, used to ensure constant position of the bodies during multi-contact motions, is taken into account by considering the following constraints:

\[
\forall i \in \{0, \ldots, N_c\} \quad a_i(P) = 0
\] (3)

the continuous equality constraint being of order \( N_c \) Eq. (3), \( N_c \leq n \) is the order that we set for the solver to avoid an over-constrained formulation (here \( N_c = 2 \)). Note that it is also possible to consider constant value without specifying the value, as used in Section V to defined floating contacts:

\[
\forall i \in \{1, \ldots, N_c\} \quad a_i(P) = 0
\] (4)

Where the first coefficient of the polynomial is not constrained.

III. MULTI-CONTACT MOTION CONSTRAINTS

In multi-contact motion, we have to pay to attention to the geometrical constraints (to ensure the constant position of the contact bodies) and to the reaction forces (to prevent from excessive interval forces and ensure balance).

A. Geometrical constraints

To define the position of a contact body, we set two Cartesian frames; one on the contact body \( X_c \) and one on the environment at the desired position of the contact \( X_c^e \). Considering \( N_c \) contacts, we must ensure \( N_c \) sets of frame equality constraint as follows:

\[
\forall t \in [\Delta t], \forall i \in \{1, \ldots, N_c\} \quad X_c(t) = X_c^e
\] (5)

As we want to use floating contacts, some component of Equation (5) refers to continuous equality constraint (Eq.(3)) and the other refers to the continuous constant constraint (Eq.(4)).

B. Inverse Dynamic Model

For each contacting link we define a set of \( C_i \) forces,and introduce the inverse dynamic model:

\[
\begin{bmatrix}
\Gamma \\
0
\end{bmatrix} = 
\begin{bmatrix}
M_1(q) \\
M_2(q)
\end{bmatrix} \ddot{q} + 
\begin{bmatrix}
H_1(q, \dot{q}) \\
H_2(q, \dot{q})
\end{bmatrix} + 
\begin{bmatrix}
J_1^T(q) \\
J_2^T(q)
\end{bmatrix} F_c
\] (6)

where \( q \) is a vector containing the \( n \) joint position \((q_i)\) and the position and orientation of a reference frame, \( \Gamma \) is the vector of size \( n \) of the torques, \( M \) the inertial matrix, \( H \) the vector due to the gravity, centrifugal and Coriolis effects, \( J \) is the Jacobian matrix and \( F_c \) is the vector of the active contact forces. In the following we note the dynamic efforts due to the dynamic of the motion: \( D_2 = M_2(q) \ddot{q} + H_2(q, \dot{q}) \).

\(^1\)It is also very strongly suggested in all the optimization textbooks!
C. Balance

In non-coplanar multi-contact motion, restrictive balance criteria such as the Zero Moment Point [21] do not apply. Recent work [22]–[24] propose alternative balance criteria that can deal with general non-coplanar multi-contact postures more efficiently.

For multi-contact motions, we characterize the balance by searching the contact forces that must be feasible; namely those that are necessary to hold a desired contact state, e.g. prohibiting from possible detachment or sliding of the link on the surface if not needed:

\[ \forall t \in [\Delta t], \forall i \in \{1, \ldots, N_f\} \left\{ \begin{array}{l} F_i^n(t) > 0 \\
||F_i(t)||^2 \leq \mu_i^2 F_i^n(t)^2 \end{array} \right. \] (7)

where \( N_f \) is the number of contacts, \( F_i^n \) the normal component of the contact force, \( F_i \) the 2D vector component of the tangent force, \( \mu_i \) is the friction coefficient of contact \( i \).

D. Computation of contact forces

We compute the contact forces from the joint trajectories and a set of parameters, as shown in [14]:

\[ F_i = -W_i^{-1} \left[ \begin{array}{c} \dot{P}i \times A_i \\
A_i \end{array} \right] \Omega^{-1} (M2\ddot{q} + H2) \] (8)

with \( W_i = \text{diag} (\beta_i, \alpha_i, \beta_i, \beta_i) \), \( \dot{P}_i \), the screw operator of the contact position, \( A_i \) the orientation of the contact framework and:

\[ \Omega = \sum_i \left( \begin{array}{c} \dot{P}i \times A_i \\
A_i \end{array} \right) W_i^{-1} \left[ \begin{array}{c} \dot{P}i \times A_i \\
A_i \end{array} \right] \] (9)

The coefficient \( \beta_i \) and \( \alpha_i \) are used to modify the internal forces and can be set constant or part of the optimization variables.

In this paper, we define the coefficient \( \alpha_i \) for all the contact forces of the same body \( j \) such that:

\[ \forall i \alpha_i = \frac{1000}{\mu_i \times N_i} \] (10)

With \( N_i \) the number of linear contact forces acting on one body.

IV. OPTIMIZATION PROCESS

A. Decomposition of the multi-contact motion

We decompose a multi-contact motion into a set of \( N_p \) phases corresponding to the number of changes of the contact configuration, namely: breaking contact, adding contact, transition between two successive contact configurations. The duration of each phase \( T_i \) can be optimized or fixed. Moreover, each phase corresponds a set of B-Spline basis function and each B-Spline is decomposed into several time-intervals in which the same basis function remains non null, as shown in the Fig. 2. Since we use cubic B-Splines, only four control points (that are part of the optimization parameters) influence the joint trajectory in each interval. That is, all along each time-interval any joint trajectory is under control of four control points among the total number.

Fig. 2. Decomposition of the motion into phases and intervals. Between two phases we can break, add or maintain a contact.

The motion is defined by the optimization vector \( P \)

\[ P = [P_{1,1}, P_{1,2}, \ldots, P_{N_mp}, \beta_{1,1}, \ldots, \beta_{N_mp}, T_1, \ldots, T_{N_p}] \] (11)

where \( P_{i,j} \) is the control point \( i \) of phase \( j \), \( \beta_{i,j} \) is the force coefficient of the contact \( i \) of phase \( j \), and \( T_i \) is the time duration of phase \( i \).

We enforce the joint position, velocity and acceleration continuity by computing the three first control points of phase \( j \in [2, \ldots, N_p] \) from the three last control points of the previous phase \( j-1 \). Then, we compute the constraints on each interval to feed the optimization solver, at each step. Since we use the inverse dynamic model, the computation for one interval is fully independent from the other ones. Subsequently, we use multi-threading to reduce the computation time.

In this paper, we get rid of the impact model and the switching among model (which otherwise turn to be a hybrid system) by considering perfectly inelastic contact. This is plausible as long as the multi-contact motion is made with contact breaking and creation at zero to low speeds (which is the case of our motions).

B. Set of Constraints

We consider humanoid robots as rigid bodies, with \( N_{dof} \) degrees of freedom (dof). To produce safe motions, we check for the joint position, velocity and torque limit all along the motion duration \( \forall t \in [0, T] \):

\[ \forall k \in \{1, \ldots, N_{dof}\} \left\{ \begin{array}{l} q_k \leq q_k(t) \leq \bar{q}_k \\
\ddot{q}_k \leq \dot{q}_k(t) \leq \ddot{q}_k \\
\Gamma_k \leq \Gamma_k(t) \leq \bar{\Gamma}_k \end{array} \right. \] (12)

The balance is ensured by considering no-sliding constraints (cf. Eq. (7)), which are gathered into a unique constraint for each contact forces \( F_i \):

\[ F_{i,x}(t)^2 + F_{i,y}(t)^2 - \text{sign}(F_{i,z}) \times \mu_i^2 F_{i,z}(t)^2 \leq 0 \] (13)

The Equation (13) cannot be satisfied if \( F_{i,z} < 0 \) or if the force is not within the friction cone. Unfortunately, the function
We heuristically found a left hand contact forces. This emphasize the effects of the applied on the left hand. Nevertheless, the sum of the two robot does not have force sensor to measure the contact forces during the real experiments. Unfortunately, the world frame located between the foot.

The Figure 4 shows the contact force measured by the force sensors during the motion presented in Figure 3 with the left hand located at the left hand in order to put an object in a trash located behind a motion where the robot has to lean on a table with its on static postures, they can lead to unfeasible motion and the motion generation. Since the contact stance are given based on joint position or limits on contact forces.

We note \( N_g \) the total number of constraints, which includes the continuous inequality \( g(P) \), the equality \( h(P) \) and the discrete inequality \( z(P, t_k) \) used by the optimization solver.

**C. Cost function**

For humanoid robots, one can find a lot of different cost functions, depending on the robot performances and desired task. Nevertheless, it is not easy to guess the cost function that human beings minimize during their motions. In order to get human-like motion, we tried several cost functions: minimum jerk for smooth motion, minimum time for fast motion, minimum energy consumption. Eventually, in this paper, we consider a combination of these three criteria:

\[
C = \sum_{i=1}^{N_{p}} a T_{i} + \sum_{i=1}^{N_{dof}} \int_{0}^{T} \left( b \dot{q}_{i}^{2} + c \ddot{q}_{i}^{2} \right) dt
\]  

We heuristically found \( a = 5, b = 10^{-2}, c = 10^{-6} \).

**V. FREE CONTACT POSITION**

In order to assess the validity of our approach, we already designed experiments on a real humanoid platform: the HRP-2 robot [15]. In [14], we produced kicking motions with and without hand contact and a sitting motion, where the robot perform several contact on the table in order to sit on the chair. In [25], we reproduced walking motion emulating leg injuries and diseases by adding some constraints on the knee joint position or limits on contact forces.

In this paper, we extend our work by taking into account floating contacts, where some components of the contact position and/or orientation are not fixed and optimized during the motion generation. Since the contact stance are given based on static postures [2], they can lead to unfeasible motion and their position may need to be different, thus to be optimized.

To emphasize the effectiveness of our method, we generate a motion where the robot has to lean on a table with its left hand in order to put an object in a trash located behind the table. The x and y-position and z-orientation of the left hand is not given and are optimized. Eventually, we get the motion presented in Figure 3 with the left hand located at \( x = 50cm, y = 0.19cm \) and \( \theta_z = -0.5rad \) regarding to the world frame located between the foot.

The Figure 4 shows the contact force measured by the force sensors during the real experiments. Unfortunately, the robot does not have force sensor to measure the contact forces applied on the left hand. Nevertheless, the sum of the two contact forces of the foot (blue line on Figure 4) gives us some indications about it, since it does not compensate the total weight of the robot. This emphasize the effects of the left hand contact forces.

**VI. FROM PERFECT MODEL TO ACTUAL EXPERIMENTS**

In this section, we experiment a walking motion overcrossing a fifteen-centimeter platform. During the first experiment of the walking motion on the fifteen-centimeter platform, after passing over the platform, the landing foot induces an impact such that it generated an entire (small) hop of the robot as shown in Figure 5; although this was not observed in simulation.

Indeed this motion emphasize the difficulties to bridge off-line model-based motion planning computations to actual robotic experiments. Unfortunately, during real experiments. We formulate the multi-contact motion generation as an optimization problem. The cost function and the constraints are explicitly or implicitly written based on a perfect model of the robot. We considered the HRP-2 as a poly-articulated system made of rigid links and perfect links, that is, no uncertainties and no flexibility. However, the robot is equipped with a shock absorbing mechanism, placed at the ankle, and which is by design flexible in order to limit the effects of impact forces due contacts of the leg with the ground during walking or running.

Unfortunately, this system is equivalent to a non-controllable joint that influences the attitude behavior of the robot, especially during contact creation and release. To deal with this problem, it is possible to use a stabilizer such as the one proposed in [26], [27], i.e., a control loop that compensate for these flexibilities and even light external perturbations.
Nevertheless, the stabilizer as it is conceived now on the HRP-2 cannot deal with some motions such as those shown on Figure 5.

![Figure 6](image_url)

Figure 6 shows the time history of the vertical component $F_z$ of the free dynamic force $D_2$ that must be counterpart by the contact forces. We see that there is a large variation of this force during the platform passing over. We assume that this force (more than 125% of the force in static posture) introduces an energy that is stored as a deformation potential of the flexible shock absorbing mechanism. When this force is suddenly reduced at landing time, the stored energy is released which produces a hop. To avoid this phenomena, we added a constraint on the normal component $F_z$ of $D_2$ during the optimization process:

$$\forall t \in [\Delta t] \quad 560 \leq F_z(t) \leq 580$$  \hspace{1cm} (16)$$

Eventually, we successfully perform the experiment as shown in Figure 7.

In summary, by ad-hoc restraining the free dynamic effects we can generate a walking motion that can be performed during real experiments without any hop due to ankle flexibilities. Even if the stabilizer is very effective for walking motions, it is based on a set of assumptions that is very limitative and cannot fit with all the motions the robot can actually perform.

VII. DISCUSSION

In this paper, we propose a method to generate multi-contact motions in full-body dynamics. We assessed its effectiveness by demonstrating some challenging experiments using the HRP-2 humanoid robot. The one presented here constitute a sample of all the motions we computed under other conditions or cost functions. Moreover, these experiments proved to be repeatable at will. The videos of all the experiments we performed are available on the website [28].

Some of the motions we computed produce collision between the robot and the environment or often self-collision. In the presented motion, we had added artificial constraints to avoid this phenomena. As an urgent work, we need to integrate collision avoidance constraints, which require a thorough investigation because the problem is far from being simple. Actually we are already working on a solution to evaluate the distance function on the entire time interval and extend the safe advanced techniques proposed in the computer graphics community [29]. This method works by assuming a constant velocity between two time samples, we are working on getting ride of this and we are confident to reach a satisfactory solution. However, we realized that the metrics, which is used to evaluate the distance function, might be not well posed from the mathematical basis viewpoint. Another problem is that such constraints will certainly increase the non-convexity of the problem that need to be considered.

VIII. CONCLUSION

In this paper, we present a method to generate multi-contact dynamical and non-gaited motions. First, the motion planning is formulated as an optimization problem with a set of continuous constraints that describes the motion, the limitations of the robot and a cost function. We handle those continuous constraints using a polynomial approximation and ensure their validity all along the motion. We proposed some improvement in order to consider floating contact for which some components of the contact position and/or orientation are not specified and discussed how, in practice, we bridge theoretical computations based on a rigid model of the robot
to actual experiments by considering additional constraints during the optimization process.

To assess our method, we compute several dynamical motions to highlight the effectiveness and the robustness of our method. We developed a method to produce generic motions that cannot be generated by state-of-the-art methods using only contact between the foot and the ground. We will also work on adding sliding contacts in order to generate some tasks motions such as cleaning a table or a board and considering free floating motion such as running or jumping.

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