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Real-Time Experimental Comparison of Two Depth Control Schemes for Underwater Vehicles

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Abstract
This paper deals with an experimental comparison between the proportional integral derivative (PID) control law and the adaptive nonlinear state feedback control, both applied on the AC-ROV underwater vehicle. The experimental results evaluate the closed-loop behaviour of the system under each controller in various operating conditions in order to compare how robust they are towards parameters’ change and how they can reject external disturbances. It was concluded that the adaptive controller ensures a faster convergence and can adapt to a change of parameters as well as compensate for external disturbances. The PID needs to be retuned for every parameter change and is more sensitive to external disturbances.

Keywords Underwater robotics, Depth regulation, PID controller, Adaptive Controller

1. Introduction
Underwater vehicles have gained an increased interest in the last decades given the multiple operations they can perform in various fields. The recent development of such robots enlarged the range of tasks in environments considered as hazardous or dangerous. Lots of advantages in terms of operational cost and safety were brought with the usage of such vehicles in underwater inspection, as in various other tasks involving manipulation, assembly or repair of offshore structures \cite{1, 2}. We are particularly interested in the category of tethered vehicles also called remotely operated vehicles (ROV). The teleoperation of these vehicles is difficult since the execution of the above mentioned tasks require the simultaneous monitoring of various parameters and degrees of freedom. Automated depth control facilitates the missions involving systematic longitudinal scanning, such as the inspection of dams or ship hulls. Different challenges in controlling such systems arise from the inherent high nonlinearities and the time varying behaviour of the vehicle’s dynamics subjected to hydrodynamic effects and disturbances. In fact, the model parameters are likely to change with the environment and the mission. For example, when the robot is required to manipulate objects or carry payloads, or when it is equipped with additional sensors, its weight, inertia, and drag change. Moreover, the buoyancy varies with the salinity of...
the water and the damping increases if some algae get a
grip on the vehicle. Trajectory tracking involves also
accounting for some expected or unexpected external
disturbances such as waves that are common in shallow
waters, or random obstacles that the vehicle might fail to
avoid. It is therefore highly desirable to design and develop
a controller able to deal with the inherent complex dynam‐
ics of the system while being able to properly compensate
parameters changes and reject disturbances. Various
approaches to solve this control problem can be found in
the literature. Most of them aim at being robust and
adaptive. In [3, 4] and [5], a robust $H_{\infty}$ control approach
was proposed and tested on AsterX AUV (autonomous
underwater vehicle) in simulations. The authors have
tested this control scheme in situations where variations
were brought to the mass of the robot and to the sampling
time control interval. Other successful simulation results
have been reported with the adaptive controller on the
Phantom ROV [6] with 4 degrees of freedom in the aim of
compensating persistent hydrodynamic terms in different
frames of reference. The same approach was used in [7]
where a more explicit description of the varying param‐
ers and their plots was presented. Experimental results
of this controller can be found in [8] where the AUV
ODIN was tested in a pool with a constant current disturbance.
Various chattering free sliding mode schemes have been
applied on such systems to cope with heavy uncertainties
and were experimentally validated in [9] where a fuzzy
sliding mode controller was applied on the AUV-HMI and
in [10] where a higher order sliding mode was tested on an
underwater vehicle prototype designed at the Cagliari
University. Combining various techniques has also been
studied with the usage of adaptive fuzzy sliding mode
controllers for trajectory tracking and depth control as
presented with numerical results in [11] and [12]. Intelli‐
gent control methods applying reinforcement learning or
artificial intelligence can be found in [13, 14, 15] and [16]
where simulation results are provided. An experimental
study was reported in [17] where the robot ICTINEU AUV
was subjected to reinforcement learning for a cable tracking
application. Comparisons among various controllers can be found in the
literature through simulations. In [18] and [19] a comparison among adaptive controllers is reported. The
former study shows robustness of each control law against
measurements noises and parameters uncertainties while
the latter one describes the ability of each adaptive control‐
er to compensate for the currents and restoring forces. The
sliding mode controller was compared in simulations to the
Mu synthesis in [20] and to the robust adaptive fuzzy
sliding mode controller in [11], in terms of trajectory
following and measurement noise. In [21], four various
model based controllers (adaptive and nonadaptive exact
linearizing controllers, adaptive and nonadaptive nonlinear
controllers) were experimentally compared to the PD
controller in the case of a good and bad initial parameter
estimation and in the case of thruster saturation. Trajectory
following plots were shown only for the nonlinear control‐
er. The study was based on the tracking error among the
various controllers that shows a bad performance of
nonadaptive controllers in presence of wrong model values
and a degraded performance for all controllers in presence
of a thruster saturation. This study lacks robustness tests to
disturbances and parameter changes as well as illustrative
plots. To the best of our knowledge, no detailed compara‐
tive experimental study between two controllers with
various robustness tests has been performed. We propose
in this paper to study the closed-loop system behaviour
under a Proportional Integral Derivative (PID) controller
and an adaptive nonlinear state feedback one. Our contri‐ution lies in reporting an experimental evaluation of the
effects of parameters changes and external disturbances on
the closed-loop response of the system for the tethered
underwater vehicle AC-ROV. For this purpose, the buoy‐
ancy and the damping parameters will be modified and
external disturbances including a mechanical shock and
waves, will be applied on the system. These scenarios will
be conducted on each controller and results ranging from
system response to control input, and changes in model
parameters will be presented. This paper is organised as
follows: in the second section we present the dynamic
modelling of the system, the third section shows the
theoretical aspects of both controllers to be compared, the
fourth section presents the prototype and the experimental
setup and in the fifth section the obtained experimental
results and their analysis.

2. Dynamic modelling of the system

Throughout this paper, the variables in bold represent
matrices and the ones in normal font represent scalars. By
considering the inertial generalised forces, the hydrody‐
amic effects, the gravity, and buoyancy contributions as
well as the effects of the actuators (thrusters), the dynamic
model of an underwater vehicle in matrix form, using the
SNAME notation and the representation proposed by
Fossen in [22], is written as:

$$\begin{align*}
\dot{\eta} &= J(\eta)\nu \\
M\ddot{\nu} + C(\nu)\dot{\nu} + D(\nu)\nu + g(\eta) = \tau + \omega_d
\end{align*}$$

(1)

where $\nu = [u, v, w, p, q, r]^T$, $\eta = [x, y, z, \phi, \theta, \psi]^T$ are vectors of
velocities (in the body-fixed frame) and position/Euler
angles (in the earth-fixed frame) respectively. $J(\eta) \in \mathbb{R}^{6\times6}$ is the
transformation matrix mapping from the body-fixed
frame to the earth-fixed one. The model matrices $M$, $C$, and
$D$ denote the inertia (including added mass), Coriolis-
centripetal (including added mass), and damping respec‐
tively, while $g$ is a vector of gravitational/buoyancy forces
and moments. $\tau$ is the vector of control inputs and $\omega_d$ the
vector of external disturbances. In the case of our study, the vehicle will be moving at low velocities which makes the Coriolis terms negligible. Therefore, the dynamics (1) can be rewritten as:

\[ M \ddot{v} + n(v, \eta) = \tau + w_d \]  

(2)

with \( n(v, \eta) = D(v) v + g(\eta) \)

Equation (2) describes the system in 6 degrees of freedom taking into account the 3 translations and the 3 orientations. The input vector \( \tau \in \mathbb{R}^6 \) considers 6 actions on the system to fully control it. In this paper, given the available sensors and instrumentation, we only study the dynamics of the vehicle in its translational motion along the \( z \) axis. Although the results concern only one DOF, this allows us to highlight each method’s advantages and drawbacks throughout the experimental results. We can easily extract from equation (2) our studied dynamics as:

\[ M_z \ddot{w} + D_z w - \cos(\phi) \cos(\theta)(W - B) = \tau_z + w_d \]  

(3)

The effects of gravitational and buoyancy forces are now brought to a single term which is a nonlinear combination between the weight \( W \) and the buoyancy \( B \). \( \tau_z \) is therefore the one dimension control input expressed in Newton and controlling the depth. It is given by:

\[ \tau_z = TKu \]  

(4)

where \( u \in \mathbb{R}^2 \) is the vector of control inputs in volts (we have two thrusters acting on the degree of freedom of interest), \( K \) is the force coefficient in Newton per Volts and it has been previously identified through experiments. \( T \in \mathbb{R}^{1 \times 2} \) is the actuators configuration matrix taking into account the position and orientation of the motors, thus allowing to determine the associated forces in the body-fixed frame.

3. Proposed control schemes

Our control objective is to achieve a depth regulation with a satisfactory closed-loop system response in spite of various external disturbances or parameters changes. For this purpose, we propose two different controllers: the Proportional Integral Derivative and an adaptive nonlinear state feedback. The former controller has been tuned using a method that minimises the ISTSE (Integral of Squared Time Multiplied by Squared Error) [23] while the latter one was tuned empirically so as to minimise the same criterion. For this purpose, the gains of this latter controller have been initially set to the same values than the optimised ones of the PID controller. Then, once the adaptation has been included, these gains have been finely adjusted to minimise the ISTSE criterion. Since each proposed scheme is expected to exhibit its best performance, the main characteristics and differences between these two controllers will be revealed throughout the proposed experimental scenarios even if a more thorough or slightly different tuning could be possible. In this study the single control input intended for the dynamics described in (3) will be computed. The indices (1) and (2) will be used for the gains of the PID and the adaptive controller respectively. General \( K_p, K_i, K_d \) will be used only to explain the mathematical description of each law.

3.1 Proportional Derivative Integral (PID) controller

3.1.1 Control law formulation

A classical PID controller has been used to achieve the desired depth regulation. The control input is given by:

\[ \tau_z = -K_h (z - z_{des}) - K_i \int_{0}^{t} (z - z_{des}) dt - K_d (\dot{z} - \dot{z}_{des}) \]  

(5)

where \( \tau_z \) is the input in Newton to be applied along the \( z \) axis, \( K_p, K_i \), and \( K_d \) are positive constants gains representing respectively the proportional, the integral and the derivative gains. \( z \) is the measured depth, \( z_{des} \) the desired one and \( \dot{z} \) and \( \dot{z}_{des} \) are their respective time derivatives.

3.1.2 PID Controller Design

The control input in equation (5) is based on the well known mathematical description of the PID controller given by:

\[ u(t) = K_p \left[ e(t) + \frac{1}{T_i} \int_{0}^{t} e(t) dt + T_d \frac{de(t)}{dt} \right] \]  

(6)

with \( e(t) \) being the error signal, \( K_p \) the proportional gain, \( T_i \) the integral time and \( T_d \) the derivative time.

To tune the parameters of a PID controller, several methods exist in the literature such as Ziegler-Nichols, Cohen-Coon and Chien-Hrones-Reswick tuning methods. The depth behavior of an underwater vehicle can be approximated by an integral process with dead time. Many tuning rules for such systems can be found in [24] and [25]. Our system can therefore be approximated according to the following Integrator Plus Dead Time (IPDT) model:

\[ G(s) = \frac{a}{sL} e^{-sl} \]  

(7)

where the parameters \( L \) and \( a \) are the intersections of the tangent to the system step response with the \( x \) and \( y \) axes respectively (as illustrated in the Figure 1), and \( s \) is the Laplace variable.
In order to identify the parameters a and L of our vehicle’s model, we have experimentally applied a thrust step along the z axis and we have observed the output behaviour. The experimental data normalized to a step input of 1 N are displayed in Figure 2. By comparing the experimental step input response with Figure 1, we have found: L = 2.6570 seconds and a = 2.3 meters.

Once these two parameters have been found, according to [23], the gains of the PID controller can be computed from Table 1. This table holds all the coefficients for the design of either a PD or a PID according to different criteria (Integral of Squared Error (ISE), Integral of Time Squared Error (ITSE) and Integral of Squared Time multiplied by Squared Error (ISTSE)). The parameters $a_1$ and $a_2$ are used for the design of a PD whereas $a_3$, $a_4$ and $a_5$ are used for a PID. In this paper, we focus on inspection applications. We have chosen to optimise both speed and accuracy, and thus have decided to minimise the ISTSE criterion which is well suited for this purpose. Of course, this choice has to be made according to the targeted application and in other situations the optimisation of another criterion could be preferred.

Using table 1, the computation of the gains of the PID controller becomes straightforward. With $a_3 = 1.34$, $a_4 = 1.83$, and $a_5 = 0.49$, and by letting $K = \frac{a}{L}$, the gains are found to be:

$$K_i = \frac{a_3}{KL} = 0.58, \quad K_d = \frac{K_{pi}}{T_i} = 0.12, \quad K_{i1} = K_{pi} T_d = 0.76$$

with $T_i = a_6 L$ and $T_d = a_7 L$.

<table>
<thead>
<tr>
<th>Criterion</th>
<th>$a_1$</th>
<th>$a_2$</th>
<th>$a_3$</th>
<th>$a_4$</th>
<th>$a_5$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ISE</td>
<td>1.03</td>
<td>0.49</td>
<td>1.37</td>
<td>1.49</td>
<td>0.59</td>
</tr>
<tr>
<td>ITSE</td>
<td>0.96</td>
<td>0.45</td>
<td>1.36</td>
<td>1.66</td>
<td>0.53</td>
</tr>
<tr>
<td>ISTSE</td>
<td>0.9</td>
<td>0.45</td>
<td>1.34</td>
<td>1.83</td>
<td>0.49</td>
</tr>
</tbody>
</table>

Table 1. Coefficients of the PID controller for the integral plus dead time plants

3.2 Adaptive nonlinear state feedback controller

3.2.1 Background

The adaptive state feedback controller is a state feedback controller with an adaptation part. It provides an online estimation of the unknown model parameters in order to ensure to the system a good trajectory following [22]. The control law is extracted from the dynamics of the robot presented in equation (2) and rewritten as:

$$\tau = M a^b + \hat{n}(v, \eta)$$

where the hat symbol denotes the parameter estimates, $a^b$ the body frame commanded acceleration, and $\hat{n}(v, \eta)$ the estimate of $n(v, \eta)$ in (2). Given that the dynamic model is linear in its parameters, the adaptive control law (8) can then be rewritten as:

$$\tau = \Phi(a^b, v, \eta) \hat{\theta}$$

where $\Phi$ is the regressor matrix and $\hat{\theta}$ is the vector of the estimated parameters. The computed input is calculated in the body frame but the trajectory following is performed in the earth frame and therefore $a^b$ is calculated from a simple transformation between the body and the earth frame given by:

$$a^b = J^{-1}(a^e - J v)$$

where $a^e$ is the commanded acceleration in the earth frame and $J$ the transformation matrix. To guarantee that the error converges to zero, $a^e$ is chosen as the following Proportional Integral Derivative (PID) control:

$$a^e = \tilde{\eta}_{des} - K_p \tilde{\eta} - K_i \int_0^{\tilde{\eta}} dt - K_d \dot{\tilde{\eta}}$$
with \( \hat{\eta} = \eta - \eta_{\text{des}} \) and \( \hat{\eta} \) is its first derivative, \( \eta_{\text{des}} \) is the desired trajectory and \( \eta_{\text{des}}^{\ddagger} \) is its corresponding acceleration.

The vector of the estimated parameters is updated according to the following update law:

\[
\dot{\hat{\theta}} = -\Gamma \Phi^T (a_b, v, \eta) J^{-1} y
\]

where \( \Gamma \) is a diagonal positive definite matrix representing the adaptation gain, \( J \) the transformation matrix, and \( y \) the combined error defined as:

\[
y = c_0 \hat{\eta} + c_1 \hat{\eta}^\prime
\]

\( c_0 \) and \( c_1 \) are constant positive gains chosen according to the algorithm presented in [22] which states that the error on the trajectory, represented by \( y \), is guaranteed to converge to zero by applying Barbalat’s lemma. It has to be mentioned that the convergence of \( y \) is only possible when the parameters also converge. Moreover, if the parameters are not adequately initialised (for instance if their initial values are too far from the true values), they might never converge, thus leading to instability of the plant. It is also important to note that a good parameter convergence is more guaranteed to occur when the followed trajectory is rich enough to excite the parameters under study [26]. However, parameters will converge to a set of values that allow trajectory following. Moreover, under the assumption of a good initialisation, the parameter vector is seen to be convergent according to Barbalat’s lemma as shown in the proof of stability found in [22].

### 3.2.2 Case of the depth control

Given the available sensors and actuators with which our underwater vehicle is equipped, we have chosen to study a trajectory varying along the heave direction. The vector of parameters to be estimated includes \( M_z \) which is the third diagonal element in the inertia matrix, \( D_z \) the third diagonal element in the damping matrix, and \( (W-B) \) the parameter representing the difference between the weight and the buoyancy. Even if the addressed problem concerns depth control, it is worth to note that this study can be easily generalised to more degrees of freedom. From equations (8) to (13), we extract the explicit formulation of our controller as:

\[
\tau_z = \Phi \hat{\theta}
\]

with the vector of the estimated parameters being:

\[
\hat{\theta} = \begin{bmatrix} \hat{M}_z \\ \hat{D}_z \\ \begin{bmatrix} 0 & \cdots & 0 \\ -1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ -1 & \cdots & 0 \end{bmatrix} \end{bmatrix}
\]

the regressor matrix:

\[
\Phi = \begin{bmatrix} \Phi_m & \Phi_d \\ \Phi_y \end{bmatrix} = \begin{bmatrix} d_z^b & w - \cos(\theta) \cos(\varphi) \end{bmatrix}
\]

the commanded acceleration in the earth frame:

\[
a_z^e = -K_{d_1} (z - z_{\text{desired}}) - K_{d_2} \int (z - z_{\text{desired}}) dt - K_{D_2} \dot{z}
\]

the commanded acceleration in the body frame:

\[
a_z^b = \cos(\varphi) \cos(\varphi) \left( a_z - \left( -q \sin(\theta) - p \cos(\theta) \sin(\varphi) \right) w \right)
\]

the parameter adaptation law:

\[
\dot{\theta} = -\Gamma \Phi^T \cos(\varphi) \cos(\varphi) y_z
\]

and finally the combined error:

\[
y_z = c_0 (z - z_{\text{desired}}) + c_1 (\dot{z})
\]

Since we are performing a regulation around a desired depth, \( \dot{z}_{\text{desired}} \) and \( z_{\text{desired}} \) are equal to 0.

Finally, given the configuration matrix \( T \) and the force coefficient \( K \) explained in equation (4), the control input can be expressed as:

\[
u = \frac{T^{-1} \tau_z}{K}
\]

### 3.3 State variables measurement and estimation

From our dynamical model (3), it appears that the used state variables are \( w, z, \) and \( \dot{z}; z \) is obtained from the depth sensor, whose data will also serve for the estimation of \( \dot{z} \). For that, the proposed solution is based on an Alpha-Beta observer [27] described hereafter. From the estimation of \( \dot{z}, \) \( w \) will be found using the transformation between the earth frame and the robot frame. The Alpha-Beta observer is a simple observer formulated for state estimation in a closely related fashion to the well known Kalman Filter. Its main advantage is its independence from the system model which makes it easily implementable. The aim is to estimate the two internal states of a system where one state is the derivative of the second (case of many robotic systems). We consider the two states as being a position and a velocity, and then we use a two-step-algorithm: the first step is the estimation of the states using basic dynamics and the second step is the update of this estimate using the error computed from the position measurements and two
constants $a$ and $\beta$ tuned empirically. The estimation step is formulated by the following:

\[
\begin{align*}
\hat{x}_k &= \hat{x}_{k-1} + \Delta T. \\
\hat{v}_k &= \hat{v}_{k-1}
\end{align*}
\] (22)

where $k$ is the iteration, $\Delta T$ the sampling time, and $\hat{x}_k$ and $\hat{v}_k$ the two estimated states at instant $k$.

The update step is written as:

\[
\begin{align*}
\hat{x}_k &= \hat{x}_{k_{\text{max}}} - \hat{x}_k \\
\hat{v}_k &= \hat{v}_{k_{\text{max}}} + \alpha \hat{r}_k \\
\hat{v}_k &= \hat{v}_{k_{\text{max}}} + \left(\beta / \Delta T\right)\hat{r}_k
\end{align*}
\] (23)

where $\hat{r}_k$ is the residual error, $x_{k_{\text{max}}}$ is the measured position and $\alpha$ and $\beta$ are two constants between 0 and 1. In our case the position is the depth $z$ updated with the pressure sensor and the estimated velocity is $\dot{z}$.

4. Real-time experimental setup

4.1 Modified AC-ROV experimental platform

The AC-ROV (cf. Figure 3-(a)) is an underactuated underwater vehicle, whose propulsion system consists of six thrusters (DC motors + propellers) controlling five degrees of freedom. These actuators allow controlling the vehicle’s orientation in pitch and yaw as well as all translational motions along the three axes ($x$, $y$ and $z$). The yaw control is provided thanks to the differential speed control of the thrusters 1, 2, 3, and 4 (cf. Figure 3-(a)). These four thrusters also control the translation along $x$ and $y$ axes. Pitch control is obtained using thrusters 5 and 6, whereas the roll is left uncontrolled. However, the roll dynamics remains stable due to the positive damping parameter $D_{\text{roll}}$ and because the centre of gravity is situated below the centre of buoyancy. The translational motion along the $z$ axis is regulated by decreasing or increasing the combined speed of thrusters 5 and 6. The axes of the vehicle are shown in Figure 3-(b). For measurement purposes, our prototype is equipped with various sensors. A 6 DOF (Degrees of Freedom) MEMS based IMU (Inertial Measurement Unit) is fixed inside the body of the AC-ROV in order to be able to measure roll, pitch, and yaw. A pressure sensor allows depth measurement. To pre-process and transmit the sensors’ data to the PC, a microcontroller board is used (cf. Figure 4). Once the control law has been computed by the control PC, the values of the control inputs are transmitted to the power stage through a dedicated microcontroller board. Then, the PWM modulated signals are sent to the actuators of the AC-ROV through the tether. The control software has been developed using C++ language under Windows Operating System. Figure 4 shows a schematic view summarising the various components of the vehicle’s hardware and their interactions.

\[\text{Figure 3. Description of the Prototype, a: AC-ROV underwater vehicle and orientations of the forces produced by the 6 thrusters, b: AC-ROV Reference Frames (X,Y,Z: earth fixed frame, X_b,Y_b,Z_b: body fixed frame)}\]

4.2 Conditions of the experiments

The experiments have been performed in a $4m^3$ water tank. The tether has been sufficiently unrolled in order to avoid additional drag to the dynamics of the vehicle. The feedback gains computed for each of the control laws and used in nominal conditions, have been kept unchanged during all the experiments despite some eventual changes in the physical system (AC-ROV) or its environment in order to evaluate the robustness of each controller. The noisy data of the depth measured by the pressure sensor are filtered using a second order Butterworth filter. The information
concerning the velocity in the z direction is estimated by an Alpha-Beta observer with \( a = 0.15 \) and \( \beta = 0.045 \), as described in section 3. Figure 5 displays the experimental test-bed.

![Figure 4. Schematic View of the Hardware Architecture of AC-ROV Prototype](image)

Our parameter vector has been initialised with our rough initial knowledge of the system. The gains used in the experiment are shown in the table below.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( K_{c1} )</td>
<td>0.5</td>
<td>( c_1 )</td>
<td>0.15</td>
</tr>
<tr>
<td>( K_{c2} )</td>
<td>0.45</td>
<td>( M_{\text{initial}} )</td>
<td>3 kg</td>
</tr>
<tr>
<td>( K_{D1} )</td>
<td>0.1</td>
<td>( D_{\text{initial}} )</td>
<td>14 N.s/m</td>
</tr>
<tr>
<td>( \Xi )</td>
<td>1.5</td>
<td>( (W-\beta)_{\text{initial}} )</td>
<td>1 N</td>
</tr>
<tr>
<td>( \epsilon_{\text{opt}} )</td>
<td>0.15</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 2. Parameters values of adaptive controller used in the experiments

5. Experimental results

In this section the obtained experimental results will be presented and discussed. The controllers detailed in section 3 have been used to control the underwater vehicle described in section 4. We will start by explaining the different scenarios performed to test the two proposed controllers and then we will analyse the obtained results presented through Figures 7 to 17. The vehicle is regulated to reach a depth of 0.35 m when starting from a static surface position. On the depth response figures, the light grey lines represent the noisy measurements of the sensor, the thick black lines the filtered data and the dashed ones the desired regulated depth position. The evolution of the control inputs, generated by the actuators 5 and 6 controlling the movements along the z axis are also plotted for each scenario. Finally, Figure 17 shows the evolution of the parameter \( (W-\beta) \).

5.1 Proposed experimental scenarios

Three experimental scenarios were performed, namely:

i. **Scenario 1**: Control in Nominal Conditions:

The objective of this scenario is to control the depth of the AC-ROV without any external disturbance. The gains for each controller have been tuned to accommodate this case and were kept unchanged for the rest of the experiments.

ii. **Scenario 2**: Robustness towards External Disturbances

The following external disturbances are considered:

a. **Punctual External Disturbance**: With the launching of the test, waves were generated manually by periodically disturbing the environment of the pool which created waves of approximately 15 cm amplitude. The two proposed controllers will be tested and compared in this situation where the controlled system is subject to this punctual external disturbance and deduce which one could be more suitable for applications performed in shallow waters, where waves are likely to be present.

iii. **Scenario 3**: Robustness towards Modelling Uncertainties

In this scenario two uncertainties on two parameters will be considered, namely:

a. **Change in Buoyancy**:

The physical system has been changed by the addition of a rectangular piece of polyester as shown in Figure 6-(b) introducing a change of buoyancy of approximately +0.32 N and bringing a variation of 32% to the parameter \( (W-\beta) \). The aim of this modification is to impede the motion of the system downwards due to its new tendency to float. The objective of this scenario is to see whether the proposed controllers are sufficiently robust to compensate this uncertainty and keep the performance of the controlled closed-loop system.
b. Change in Damping:
As before, the physical system has also been changed by the addition of a floating rectangular ruler on the top of the vehicle as shown in Figure 6-(c) to increase the damping. As before, we would like to study the effects of this change on the response of the system and evaluate the performance of the proposed two controllers.


Figure 6. View of the AC-ROV in different configurations: a: Nominal conditions, b: Buoyancy change, c: Damping change

5.2 Control in nominal conditions
Figure 7 displays the evolution of the controlled vehicle’s position for each of the proposed controllers. The PID controller in Figure 7-(a) needs around 80 seconds to reach steady state with an overshoot of 57%. Note that the delay of 40 seconds, noticed in Figure 7-(a), is caused by the time needed for the integral part to compensate the floatability of the robot \((W - B) = -1\) N. The adaptive controller reveals to be much faster and converges to the desired depth in 20 seconds with an overshoot of 28%. The settling time of this controller also coincides with the time needed for the parameter \((W - B)\) to converge to its steady state value (cf. Figure 17-(a)). The evolution of this parameter is depicted in Figure 17-(a) and reaches a steady state value of \(-0.97\) N.

The other two parameters did not evolve noticeably and hence were not represented. The reason of this latter observation lies behind the idea of enough parameter excitation that needs to be present in order to induce changes. The suggested trajectory excites mainly the parameter \((W - B)\) which has a big effect on the dynamics of the vehicle. The initial parameter of \(M_z\) was carefully initialised since it was only required to weigh the robot. Indeed, the added elements shown in Figures 6-(b) and 6-(c) to increase the buoyancy and the damping respectively have a negligible weight. As for the parameter \(D_{s2}\) its rough initial estimate was enough since the vehicle moves at low velocities. As explained in section 3, assuming that the parameters are adequately initialised, they will converge. Once they have converged for the first time, it is convenient
to record the values of this “nominal” set of parameters and to initialise them with these values for the next experiments. If we had not initialise them to these values, this would have simply induce a delay (convergence time of the parameters) but the comparison with the PID would not have been fair. The convergence of parameters that have been initialised with erroneous values will be illustrated by the results of scenario 3.

The maximal admissible force that can be generated by the motors is \( F = 2 \) N and we can notice from the curves of Figure 8 that this limit has not been exceeded and that the control force oscillates around a steady state value of 0.5 N for both controllers. We notice though that the control input exhibits larger oscillations (noise) in the case of the adaptive control. This point is important as it not only increases the power consumption (this is however not critical for tethered vehicles like ROV), but it also increases the thrusters’ fatigue. This noise in the control inputs is mainly due to the noisy depth measurement (even when filtered) and to the derivative term of the controller. The possible solutions of this problem are indicated in the conclusion of the paper.

![Figure 7](image.png)

**Figure 7.** Depth Response in Nominal Regime

![Figure 8](image.png)

**Figure 8.** Control Input in Nominal Regime

### 5.3 Robustness to external disturbances

#### 5.3.1 Punctual external disturbance

As specified earlier, series of mechanical impacts have been applied on the vehicle after it has reached steady state (cf. Figure 9). For the PID controller, the mean recovery time was of 30 seconds against 25 seconds for the adaptive controller. The system responses of both controllers are similar even though we can notice larger oscillations around the regulated depth with the PID after the recovery from the disturbance was achieved. The control inputs shown in Figure 10 reveal an important overshoot with the adaptive controller, while the PID witnesses a decrease in its commanded input in absolute value. The former controller had a sudden change in its parameters leading to an overshoot of 1.5 N in its control input, while the latter was compensating for the induced error by sending a lower order to the thrusters. In this case, the PID controller seems to behave better in terms of energy consumption.
5.3.2 Persistent external disturbance (Waves)

The obtained results of this scenario are depicted in Figures 15 and 16. Figure 15 shows the system response of the robot in presence of disturbing waves. Varying oscillations around the regulated depth are observed with both controllers. However, those of the PID controller are more significant with an average of 20 cm amplitude. It is worth to notice that the adaptive controller exhibits smaller oscillations with 10 cm of average amplitude which means that it was able to partially attenuate the effect of the waves in order to remain around the value of the desired depth. The oscillations observed in Figure 15-(a) are reflected in Figure 16-(a) where the control input is observed to be oscillating without converging to a steady state value. In Figure 16-(b), less severe oscillations can be observed on the control signals generated by the adaptive controller.

5.4 Robustness to modelling uncertainties

5.4.1 Change in buoyancy

The additional buoyancy incorporated in the system disturbs in a persistent way the motion of the vehicle that would tend to float more. The PID controller in this case responded with a delay of 35 seconds and an overshoot of 128%; furthermore oscillations of approximately 10 cm can clearly be observed around the desired depth (cf. Figure 11-(a)). Its control input seems to be similar to the nominal case except that it stabilises to a steady state value in a steeper manner with some small oscillations. We notice in this scenario a new delay in Figure 11-(b) when applying the adaptive controller. The delay is of 8 seconds and the settling time is of 40 seconds compared to 20 seconds in nominal conditions. This can be explained with the necessary time to adapt the parameter to the change and converge to its new steady state value of −1.18 N which also took 40 seconds to be reached (cf. Figure 17-(b)). The added buoyancy is found to be 0.21 N (−0.97−(−1.18)=0.21 N) when comparing the steady state values of the parameter (W−B) in Figures 17-(a) and 17-(b). This value of 0.21 N is close to the real one (0.32 N) by 65%. It is worth to note that adaptive controllers do not necessarily ensure the convergence of the updated parameters to their desired values [26] in order to obtain the convergence of the system to its desired position. The control law detailed in section 3.2 ensures the boundedness of the parameters but not necessarily their convergence to the real values. Concerning the control inputs generated by this controller, and depicted in Figure 12-(b), we can observe that the robot’s actuators are exerting more effort and they oscillate around a mean value of 0.65 N. These oscillations are seen to be larger than with the PID case. This profile reveals the
additional difficulty experienced by the motors in order to immerse the vehicle.

5.4.2 Change in damping

Similarly to the previous scenario, a change in the physical system was considered. It was integrated to damp the dive of the vehicle as illustrated in Figure 6-(c). The PID controller in Figure 13-(a) starts reacting at around 40 seconds and displays an overshoot of 171% but reaches steady state after 80 seconds. The required control input generated by this controller (cf. Figure 14-(a)) has a maximal value of 0.9 N and converges to a steady state value of 0.55 N after a small oscillation matched with the oscillation observed in the response of the system. The adaptive controller stabilizes the system with a settling time of 20 seconds and a small overshoot of 28% like the nominal case but the oscillations around the desired depth are more important. The response could have been improved with a better excitation of the parameter $D_z$.
Figure 14. Control Input in Presence of a Damping Change

Figure 15. Depth Response in Presence of Waves

Figure 16. Control Input in Presence of Waves

Figure 17. Evolution of the Parameter (W-B)
5.5 Summary of comparison between the proposed controllers

Table 3 below summarises the comparisons performed above between the two proposed controllers for different scenarios. Some relevant criteria have been chosen to perform this comparison which has been done in a qualitative and quantitative way depending on the criterion. It can be easily seen that the adaptive controller drives the system to steady state faster than the PID controller. Indeed, its closed-loop response has a settling time of approximately three times smaller than the case of the PID controller. This difference can be explained (as mentioned before) by the fact that the PID controller needs some time for its integral action to counterbalance the effect of the floatability. The adaptive controller needs a certain time to converge its parameters to their steady state values. However, this time depends on the adaptation gain and can therefore be shortened by increasing this design parameter. However, it is known that the adaptive control is not robust when the adaptation gain is set to be high and that justifies the reasonable choice of $\Gamma = 1.5$ (see Table 2). The settling time of the closed-loop system controlled by the PID is around 60 seconds in the nominal case, however it increases to 80 seconds when considering the uncertainty on damping. In the case of the adaptive controller, the settling time is around 20 seconds but it doubles when an uncertainty on buoyancy is considered. Indeed, this unexpected uncertainty will lengthen the necessary time for the parameters to converge to their steady state values. Therefore the control input will be changed accordingly which affects the settling time of the closed-loop system. The PID controller always exhibits large overshoots when any kind of change is introduced to the system, while the adaptive controller stays around the performance of its nominal conditions thanks to the adaptation of its parameters. Regarding the precision of the output response, it is worth to note that the depth sensor used has an uncertainty of 5 cm and that’s why the steady state oscillations were meant to be quantitatively indicated. The adaptive controller requires more energy than the PID controller and this can be shown from the more relevant force generated by the thrusters. This behaviour can be explained by the fact that the adaptive controller remains faster and more robust to all kind of disturbances. Even though both controllers could not compensate completely the persistent disturbance (waves), the adaptive controller was able to better compensate for it with less significant oscillations.

<table>
<thead>
<tr>
<th>Nominal Conditions</th>
<th>PID Controller</th>
<th>Adaptive Controller</th>
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<tbody>
<tr>
<td>Settling Time</td>
<td>60 s</td>
<td>20 s</td>
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<tr>
<td>Maximum Overshoot</td>
<td>57%</td>
<td>28%</td>
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<tr>
<td>Residual oscillations</td>
<td>5 cm</td>
<td>2.5 cm</td>
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<tr>
<td>Control Input</td>
<td>Oscillations of 0.1 N</td>
<td>Oscillations of 0.5 N</td>
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<td>ISTSE</td>
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<tr>
<th>Punctual Disturbance</th>
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<tr>
<td>Recovery Time</td>
<td>30 s</td>
<td>25 s</td>
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<tr>
<td>Maximum Overshoot</td>
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<tr>
<td>Residual oscillations</td>
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<tr>
<td>Control Input</td>
<td>Smooth motor response</td>
<td>Overshoot of 1.5 N</td>
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<th>Persistent Disturbance: Waves</th>
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<tr>
<td>Maximum Overshoot</td>
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<td>37%</td>
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<tr>
<td>Residual oscillations</td>
<td>20 cm average</td>
<td>5 cm</td>
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<tr>
<td>Control Input</td>
<td>Oscillations of 0.2 N</td>
<td>Oscillations of 0.2 N</td>
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<td>0.1572 s^2.m^2</td>
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<tbody>
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<td>40 s</td>
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<td>Maximum Overshoot</td>
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<td>28%</td>
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<tr>
<td>Residual oscillations</td>
<td>10 cm</td>
<td>2.5 cm</td>
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<tr>
<td>Control Input</td>
<td>Overshoot of 0.95 N</td>
<td>1 N oscillations and later 0.5 N</td>
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<tr>
<td>ISTSE</td>
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<td>Maximum Overshoot</td>
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<td>28%</td>
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<td>Residual oscillations</td>
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<td>10 cm</td>
</tr>
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<td>Control Input</td>
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<td>Oscillations of 1 N</td>
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<tr>
<td>ISTSE</td>
<td>0.2236 s^2.m^2</td>
<td>0.0283 s^2.m^2</td>
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</table>

Table 3. Controllers Performance Comparison
6. Conclusion

This paper deals with the problem of depth control of an underwater vehicle. The proposed solution lies in an experimental comparison study between a PID controller and a nonlinear adaptive one, both applied on the modified AC-ROV underwater vehicle. These two controllers have been tested in various conditions such as nominal case as well as different situations to highlight robustness towards external disturbances and uncertainties. To the best knowledge of the authors, such an experimental study comparing the performance of two proposed controllers was not conducted before. It gives a good insight on the robot’s behaviour in real environments when carrying out different tasks. The adaptive controller was observed to converge faster than the PID controller and compensate better for external disturbances and parameters changes. Furthermore, less overshoots and oscillations were observed on the output response with the adaptive controller. The only drawback of the latter is the oscillations observed on the control input. This is due to its need to react fast and ensure the convergence of the parameters. Our future work includes the design and implementation of a nonlinear multivariable L1 adaptive controller, for depth and pitch control of the same underwater vehicle.

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8. References


