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Methodology for Power Mode Selection in FD-SOI circuits with DVFS and Dynamic Body Biasing

Y. Akgul¹, D. Puschini¹, S. Lesecq¹, E. Beigne¹, P. Benoit², L. Torres²

Abstract—Embedded systems need ever increasing computational performances. Since they have limited energy resources, power consumption has to be minimized. Dynamic Voltage and Frequency Scaling (DVFS) techniques combined with Body Biasing techniques decrease the power consumption of a chip by providing just enough computational performance to the chip so as to finish the task at its deadline. A Power Mode (PM) is defined with the clock frequency F applied to the chip and the power P consumed by the chip. Executing tasks with the 2 neighbor frequencies of the target frequency should minimize the power consumption. Unfortunately, this choice is not always optimal since the set of available PMs may not fulfil the convexity property anymore when 3 actuators are considered. Here, a method is proposed to tackle this issue. PMs are selected to form a discretely convex subset. Results for a ring oscillator in FD-SOI exemplify that the proposed approach can save power consumption.

I. INTRODUCTION

The ever increasing requirements in computational performance for embedded systems have lead to an increase in the clock frequency applied to the circuit. Meanwhile, the computational performance requirements and power efficiency have become highly critical for mobile platforms powered by batteries. As a consequence, the designer has to implement methodologies to meet the computational performance requirements while minimizing the power consumption P . Note that this latter actually depends on the supply voltage V_{dd} applied to the circuit, the clock frequency F , the threshold voltage V_T , the operating temperature T° , the circuit activity A , etc. The circuit activity A corresponds to the average number of cells which switch during a clock cycle. Moreover, P is usually split in “leakage” and “dynamic” parts.

Several solutions can be implemented to reduce the power consumption. First, large chips can be split in several Frequency Islands, leading to the well known Globally-Asynchronous-Locally-Synchronous (GALS) architectures [1]. Furthermore, the voltage of each island can be modified. So, each island can be switched on/off depending on the amount of tasks it has to run. This solution when applied at fine-grain is admitted saving power consumption. Moreover, when associated with Dynamic Voltage and Frequency Scaling (DVFS), the gain can be tremendous. In this situation, V_{dd} and F applied to each island should ideally be adapted to provide enough computational performance to execute the task running

on the Processing Element (PE) burried in the island, but no more.

Dynamic V_T Scaling (DVTS) techniques can also decrease the power consumption by adjusting the threshold voltage V_T to balance the leakage power and minimize the overall power consumption. The threshold voltage V_T is modified thanks to the body bias voltage V_{bb} either to reduce the power consumption while maintaining/increasing computational performance, or to increase the computational performance for the same power budget/a lower one.

Power Management has become even more difficult for advanced technologies that operate with V_{dd} close to V_T , leading to “Near-Threshold Circuits” (NTCs) [2]. Actually, decreasing V_{dd} is still considered the most efficient way to reduce dynamic power consumption. However, running at V_{dd} very close to V_T induces new side effects, e.g. the leakage power has a great influence on the overall power budget. At the same time, the clock frequency F applied to the PE must be carefully chosen to avoid timing faults. Thus, the triplet (V_{dd}, F, V_{bb}) cannot be independently chosen to ensure a functional operating point that satisfies the computational performance constraints. Moreover, even if one triplet makes the chip functional, it might not be the most power efficient operating point [3]. As a consequence, choosing of an operating point is an intricate problem, even worse when 3 “actuators” (i.e. supply voltage, clock frequency and body bias voltage) are considered.

In the present work, the performance constraint which is considered is the speed as the task T running on the PE has to meet its deadline d . A methodology for selecting the operating points to be applied to the PE for task T is proposed. Task T has to meet its deadline d while minimizing the power consumption. The notion of “operating point” is preferred to the classical (V_{dd}, F) or (V_{dd}, F, V_{bb}) set of actuator values. Indeed, it is more general and it does not care about a particular implementation. The power consumption depends on the operating point values, leading to the so-called “Power Modes” (PMs) [4]. As the speed (related to the clock frequency F) cannot be chosen independently from V_{dd} and/or V_{bb} , the plane (F, P) is considered here. Note that $P(F)$ can be a continuous function, a piecewise continuous function, or even P can take its values in a finite set of values. Therefore, this choice encompasses a wide variety of situations a designer might encounter regarding the implementation of the actuators that feed the PE (e.g. hopping technique [5] [6], DC-DC converter for V_{dd} [7], Frequency Locked-Loop or frequency division [8], etc.).

The present paper extends previous results [3] in the context

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of a finite set S of PMs obtained by 3 actuators. First, a discretely convex subset \mathbb{S} of PMs is extracted from the initial set S . This step does not require to distinguish leakage and dynamic power; it is solely based on total power consumption figures which can be estimated at design time or measured on the chip. Then, an optimal selection of PMs applied to the PE for a given task to meet its deadline while minimizing the power consumption is proposed. This step is close to part of the results proposed in [3].

The paper is organized as follows. Section II provides an overview of previous works dedicated to the choice of operating points so that task T meets its deadline d while minimizing the PE power consumption. Section III summarizes the results proposed in [4]. They show how and where an intermediate PM could be added when 2 PMs are already available on the PE (low power and high performance modes). The intermediate PM can be fixed in order to minimize the power consumption for a given range of workload. Then section IV is dedicated to the choice of PMs applied to the PE when a finite set is available. Results show that not all PMs are optimal. The method is exemplified in section V. Power figures have been obtained with the simulation of a ring oscillator in STMicroelectronics 28nm FD-SOI technology and it can be extended to a more complex circuit. Furthermore, the concept has been evaluated in a FD-SOI context and it can be reused for other CMOS technologies. Finally, section VI sums up the main contributions and provides future work directions.

II. RELATED WORKS

Several power management techniques can be found in the literature. They can broadly be classified in two main families, namely, the “static” techniques that are applied at the circuit design phase or test phase, and the “dynamic” ones that adapt at run-time the operating point in order to decrease the power consumption. In this latter family, the operating point is modified by acting on up to 3 actuators (V_{dd} , F , V_{bb}). A subset of these works is now shortly discussed.

The power consumption of a PE for a given computational performance can be optimized during the test phase by an appropriate setting of V_{bb} and V_{dd} [9]. However, the optimization is done once and it cannot take into account dynamic variations. When Dynamic Frequency Scaling (DFS) is associated, the power consumption can be decreased but it is well known that DFS cannot reach the minimum power consumption when tasks with different computational performance demands are executed on the PE.

Another way to reduce the power consumption is to use Dynamic Voltage and Frequency Scaling (DVFS) techniques. The main idea is to adapt at run-time V_{dd} and F to reduce the power consumption while maintaining the computational performance (e.g. meet the time constraint for the task processed on the PE). This situation obviously requires information about the task (amount of work) to choose the accurate clock frequency. Several implementation variants of this technique exist, depending on the choice of the V_{dd} and F actuators, leading to discrete sets or continuous intervals of values that

can be applied to the PE. [10] determines the “optimal” (V_{dd} , F) couple applied to a PE to execute a task when a Dynamic Voltage Scaling (DVS) technique (with a continuum of values in a given interval) is used in conjunction with a finite set of frequencies. A ratio energy/deadline is taken into account to determine if the operating point is efficient or not. The frequency profile (i.e. the number of frequencies applied and their individual time duration) depends on the deadline of the task.

Other works consider that a finite set S of operating points (V_{dd} , F) is available. For instance, a V_{dd} -hopping [5] is implemented for the V_{dd} actuator, leading to few (usually 2 or 3) available supply voltages, while a finite set of frequencies can be applied with a Dynamic Frequency Locked-Loop [8]. In these situations, the computational performance demand is satisfied thanks to the application of several PMs, each PM being defined by a couple (V_{dd} , F). Note that a unique operating point is applied if the frequency fulfilling the constraint (hereafter called target frequency F_{target}) exists in the frequency set. When F_{target} is not in the frequency set, the computational performance is usually met by the application of 2 PMs in “hopping” execution. Such an execution consists in processing part of the task T with frequency $F_2 \geq F_{target}$ during the time period $\alpha \cdot d$ and the remaining part of T is processed with frequency $F_1 < F_{target}$ until the deadline is met such that:

$$F_{target} = \alpha \cdot F_2 + (1 - \alpha) \cdot F_1$$

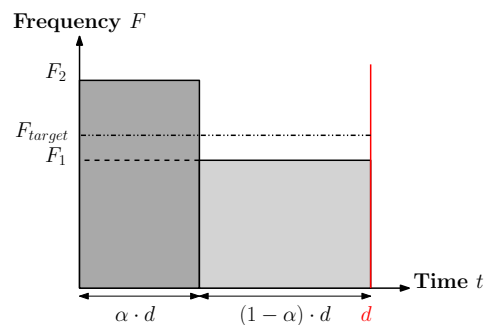


Fig. 1: Execution of task T with deadline d in “hopping” execution.

Figure 1 illustrates this “hopping” execution. [11] applies this concept with ($V_{dd,1}$, F_1) and ($V_{dd,2}$, F_2) such that $F_1 \leq F_{target} \leq F_2$, $F_1 = \max\{F_i, F_i \leq F_{target}\}$, $F_2 = \min\{F_i, F_i \geq F_{target}\}$. However, this choice is not always optimal, depending on some $P(F)$ properties. Actually, it can be proved [3] that the optimal power consumption is reached when the neighbors F_1 and F_2 are used if the points of $P(F)$ form a discretely convex set as defined in [12]. This property is not always fulfilled when DVFS techniques are combined with the body bias voltage actuator. Actually, with new technologies such as FD-SOI, the body bias voltage V_{bb} actuator has a greater influence because the modification range of V_{bb} is very wide.

[13] proposes to use a body bias voltage V_{bb} actuator to reduce the leakage power consumption while [14] [15] show that the use of the V_{bb} actuator in conjunction with a DVFS technique is more efficient to reduce the power consumption while maintaining or increasing the computational performance. Other works propose to reduce the device power consumption by reaching a constant ratio of the leakage power consumption to the dynamic power consumption [16] or a constant ratio of the switching current I_{sw} to the leakage current I_{leak} [14]. However, the power consumption is not necessarily minimized by keeping I_{sw}/I_{leak} constant [9].

Dynamic Voltage and Frequency Scaling (DVFS) together with Body Biasing techniques are combined in order to reach a trade-off between reliability, computational performance and power consumption [17]. This latter work considers that V_{dd} and V_{bb} are continuous on known intervals. The optimization problem is expressed as a Geometric Program one [18].

[3] proves that an optimal speed profile is reached when certain conditions are fulfilled. To obtain this result, the Q-function is introduced which corresponds to the ratio of power to speed. The optimal speed profile is attained when the relation Q-function/speed is convex. Furthermore, the authors state that devices by default satisfy this convexity property. This assertion is correct if the PE is managed by 2 actuators (e.g. V_{dd} and F or V_{bb} and F or V_{dd} and V_{bb}). Nevertheless, for advanced technologies, when 3 actuators are combined, this statement depends on the range of each actuator. Therefore, a selection of PMs has to be implemented. In the present work, 3 actuators are supposed to feed the PE so that a finite discrete set S of PMs can be applied. Moreover, no discrete convexity conditions as defined in [12] are assumed for S because the subset is unlikely to fulfil this condition.

III. INFLUENCE OF THE DISTRIBUTION OF POWER MODES ON POWER CONSUMPTION

The main objective of the paper is to provide a methodology to optimally select from a PM set the PMs to be applied to an island. However, the power reduction greatly depends on the PM distribution. A method to optimally fix a 3rd PM between 2 PMs for a given range of workload is now summarized.

Each island can be composed of a PE, cache or scratchpad memory. It is supposed to possess its own frequency and/or supply voltage actuators. Figure 2 depicts a simplified overview of an island. A task T to be run requires N_c clock cycles for completion, taking into account memory and peripheral accesses. T runs on the PE and must meet its deadline d . To fulfil these requirements, the PE should theoretically run at $F_{target} \geq \frac{N_c}{d}$. Since a discrete frequency actuator is taken into consideration, if F_{target} is not available, higher and lower frequencies are applied successively to reach the required computational performance on average, with “hopping” execution [5].

A Power Mode (PM) is defined as a pair (F, P) , where F is the clock frequency, and P the power consumed. P depends on F and on a set of parameters (activity A , supply voltage V_{dd} , body bias voltage V_{bb} , temperature T° , etc.) [4]. A given

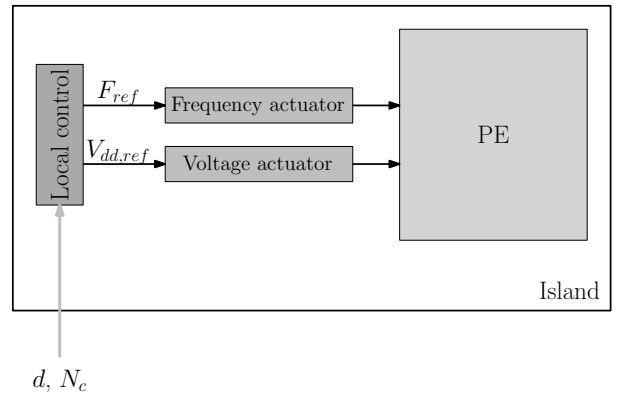


Fig. 2: Schematic of an island with 2 actuators. d is the deadline and N_c is the number of clock cycles.

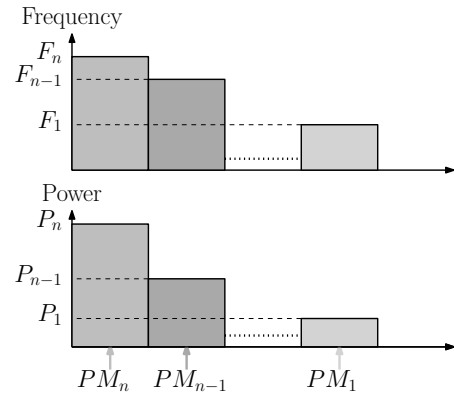


Fig. 3: n PMs $(F_i; P_i)$, $i = 1 : n$.

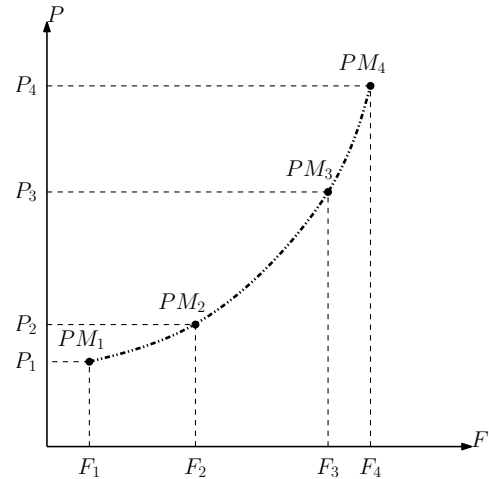
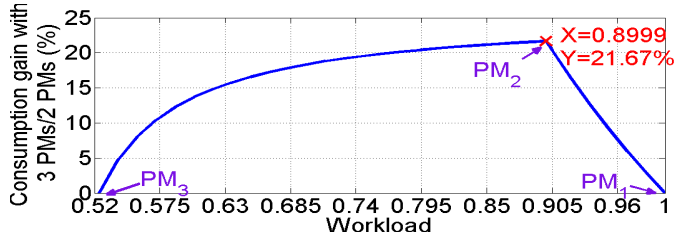


Fig. 4: P as a function of F with n PMs $(F_i; P_i)$, $i = 1 : n$, $n = 4$.

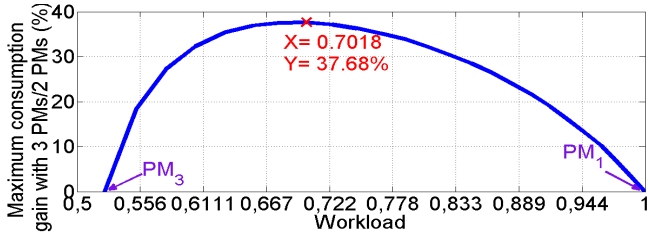
PE is assumed to operate in n PMs, depicted in Figure 3 and in Figure 4, depending on different combinations of internal with external parameters. Recall that the concept of PM has been introduced because it is independent of the particular implementation of the actuators (e.g. V_{dd} -hopping [5], V_{bb} -

hopping [6], DC-DC converter [7]).

An analytical study is presented in [4] when 3 PMs are available on the PE. In this latter paper, it has been proved that for a given distribution of the PMs, a maximum gain in power consumption can be attained for a specific workload WL range, when the 3^{rd} PM (PM_2) is properly fixed between PM_1 and PM_3 see Figure 5. The workload is defined as the load of the processor. It corresponds to a ratio of target frequency F_{target} to the maximal frequency F_{max} available on the PE, $WL = \frac{F_{target}}{F_{max}}$.



(a) Consumption improvement when a 3^{rd} PM is added [4].



(b) Maximum consumption improvement when a 3^{rd} PM is added [4].

Fig. 5: Improvement of the power consumption when a 3^{rd} PM is added vs. normalized workload [4].

Note that the results in [4] might be used in the current work in order to optimally fix the set of PMs for a given range of activity.

IV. POWER MODE SELECTION IN A DISCRETELY NON-CONVEX SET

In the present work, the operating points are obtained thanks to 3 actuators to adjust the supply voltage V_{dd} , the body bias voltage V_{bb} and the clock frequency F of an island (see Figure 6). In Multiprocessor System-on-Chips, sensors and actuators are distributed in each island. In order to reduce their Silicon overhead, discrete mechanisms are preferred to continuous ones. Here, V_{dd} is considered as a finite set of values, supplied for example by a hopping mechanism. The clock frequency F is discrete with a few achievable values. For instance, it could be provided by a Digital Frequency Locked-Loop [8]. The body bias voltage V_{bb} actuator takes its values in a small finite discrete set. It could be furnished through a V_{bb} -hopping technique [6]. Therefore, there is a finite set of PMs $S = \{(P_i, F_i), i = 1 : n\}$, where $F_i \leq F_{i+1}$ for all $i = 1 : n - 1$. This set is not necessarily discretely convex as defined in [12]. In this section, a methodology to select the PMs distribution will be presented. This methodology extends

the results of [3] while the method proposed in [4] can be applied to choose the distribution of PMs in S .

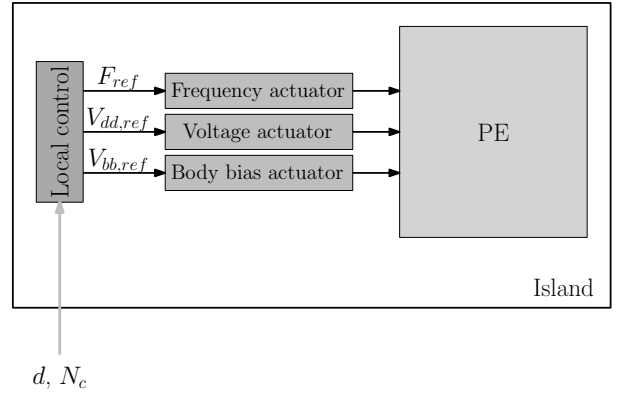


Fig. 6: Schematic of an island with 3 actuators. d is the deadline and N_c is the number of clock cycles.

Definition. A set is defined to be convex on an interval I if and only if (see Figure 7) $\forall F_1, F_2 \in I, \forall \beta \in [0, 1]$,

$$P(\beta \cdot F_1 + (1 - \beta) \cdot F_2) \leq \beta \cdot P(F_1) + (1 - \beta) \cdot P(F_2) \quad (1)$$

with $P(F)$ the power consumption related to F .

In other words, a set is defined as convex if every point of the curve $P(F)$ between two points is situated below the segment of line connecting these points.

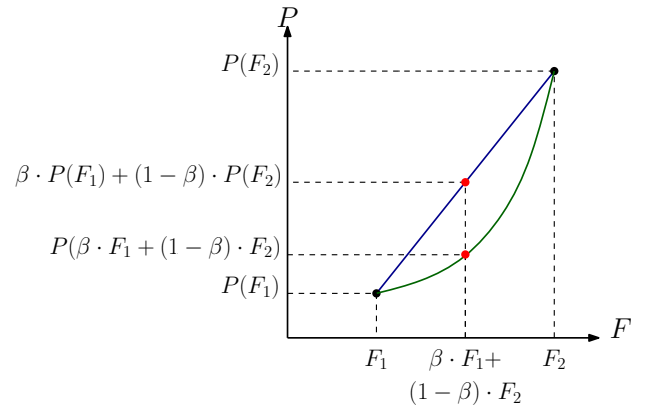


Fig. 7: Example of an increasing convex set $P(F)$.

In section A of the Appendix, it is proved that the use of (F_1, F_2) in “hopping” execution with F_2 just above the target frequency F_{target} and $F_1 < F_{target}$, minimizes the power consumption when S is discretely convex. Moreover, section B of the Appendix shows that the use of (F_1, F_2) in “hopping” execution with $F_1 \in S$ just below F_{target} and $F_2 > F_{target}$, minimizes the power consumption when S is discretely convex. Finally, in section C of the Appendix, deduced from section A and section B of the Appendix, it is shown that the use of the 2 neighbor frequencies of F_{target} will minimize the power consumption in “hopping” execution when the set of points is discretely convex. Note that this result

is similar to the one in [3] where the authors prove that the optimum speed is reached for an execution of the task with a combination of the two neighbor frequencies which belong to the convex set of the Q-function in function of the speed. Here, the proof is conducted directly on P , not on the Q-function. Thus, to ensure an optimal “hopping” execution, a discretely convex subset of PMs \mathbb{S} must be extracted from S .

Therefore, the proposed method is composed of two parts. The first one consists in finding the discretely convex subset \mathbb{S} of S since new technologies do not necessarily lead to a convex set S . The second part of the methodology consists in executing tasks with the two frequencies surrounding F_{target} in \mathbb{S} [3]. The main objective is to apply the target frequency. However this frequency can be reached only by applying a PM or a combination of PMs. The aim of the proposed method is to reduce the total power consumption whatever the ratio of the leakage power consumption to the dynamic power consumption.

To summarize, since the set S is not always convex as supposed in [3], a subset of PMs has to be defined in order to fulfil the discrete convexity hypothesis. Then the “hopping” execution approach can be applied. Note that the present work directly deals with power consumption figures, without any power consumption equation.

V. APPLICATION IN THE CONTEXT OF FD-SOI TECHNOLOGY

In section IV, it has been proposed to select the PMs that belong to the discretely convex subset \mathbb{S} of S , and to process tasks only with the points belonging to \mathbb{S} . This proposition enables to save more power when compared to an execution of the tasks without an initial selection of the PMs. After the selection phase the PMs in the discretely convex subset \mathbb{S} are used. In fact, the main purpose of this proposition is to minimize the power consumption while satisfying the time constraint. However, to apply the proposed methodology, the PMs have to be characterized, i.e. the power consumption has to be quantified. For instance, the power consumption can be determined thanks to voltage and temperature sensors [19] combined with activity sensors [20] or with current sensors [21] or obtained by simulation.

The testbench is a ring oscillator in STMicroelectronics 28nm FD-SOI technology. In this example, 2 levels of body bias V_{bb} and 3 levels of supply voltage V_{dd} are available on the PE. Note that in [22], the number of supply voltages available is 3 and there is more than a dozen levels for the body bias voltage. The voltage values are: $V_{dd,1} = 0.6$ Volt (V), $V_{dd,2} = 0.8$ V, $V_{dd,3} = 1.0$ V, $V_{bb_L} = 0$ V (unboosted level) and $V_{bb_H} = 1.2$ V (boosted level). A ring oscillator has been simulated. Its oscillating frequency depends on the supply voltage and the body bias voltage. It has also a constant activity, here equal to 100%.

Figure 8 represents the frequency F in function of V_{dd} with V_{bb_L} the unboosted level and V_{bb_H} the boosted one. Nevertheless, the representation in the (F, P) plane in Figure 9 is preferred to properly select the PMs that are in the discretely

TABLE I: Values for each PM of the supply voltage V_{dd} , the body bias voltage V_{bb} , the normalized frequency F , the normalized power consumption P .

PM	V_{dd} (V)	V_{bb} (V)	F (normalized)	P (normalized)
PM_1	0.6	0	0.2308	0.0484
PM_2	0.6	1.2	0.3846	0.1612
PM_3	0.8	0	0.5385	0.1852
PM_4	0.8	1.2	0.6923	0.4397
PM_5	1.0	0	0.8462	0.4651
PM_6	1.0	1.2	1.0000	1.0000

convex set. Figure 9 shows the curve of power consumption P in function of the available frequencies F for the 3 supply voltage V_{dd} ($V_{dd,1}$, $V_{dd,2}$, $V_{dd,3}$) and 2 values of the body bias voltage V_{bb} (V_{bb_L} , V_{bb_H}). The normalized PMs values are given in Table I (see Figure 8 as well). As can be seen in Figure 9, the set of points S does not form a globally discrete convex set. Thus a subset of points in S are selected to form a discretely convex subset \mathbb{S} . This PM subset will be used so as to minimize the power consumption.

The PMs selected from ones in Table I are depicted in red on Figure 9 (PM_1 , PM_3 , PM_5 , PM_6). These PMs belong to the discretely convex subset \mathbb{S} of S . Therefore, they allow to minimize the power consumption. Hence, in order to perform a task while satisfying its power and time constraints, only the points in the discretely convex subset \mathbb{S} (PMs in red in Figure 9) will be applied to the circuit possibly in “hopping” execution way. Figure 10 shows the operating points after the PMs selection step has been performed.

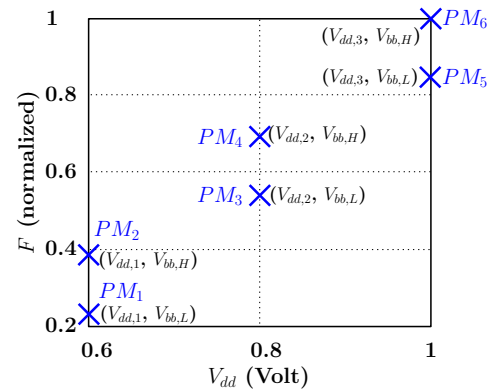


Fig. 8: Set of available frequencies F in function of the supply voltage V_{dd} : $F(V_{dd})$.

Different situations may appear when executing a task:

- If the target frequency F_{target} is available on the PE and if the PM corresponding to F_{target} belongs to the discretely convex subset \mathbb{S} , the PM is applied directly in order to execute the task;
- If the target frequency F_{target} is available on the PE and if the PM corresponding to F_{target} does not belong to the discretely convex subset \mathbb{S} , the 2 PMs in the discretely convex subset \mathbb{S} surrounding F_{target} are applied in order

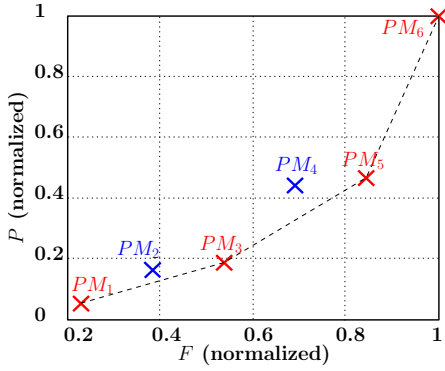


Fig. 9: Set of PMs in the (F, P) plane. Red crosses correspond to PMs in the discretely convex subset.

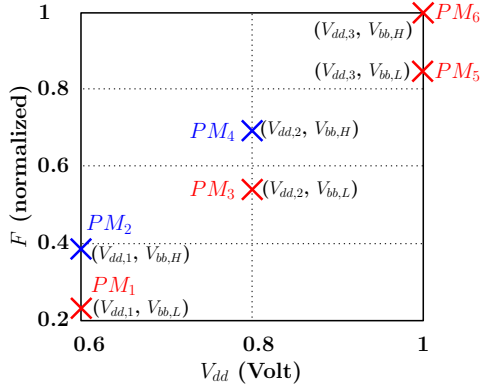


Fig. 10: Set of PMs in the (V_{dd}, F) plane. Red crosses correspond to PMs in the discretely convex subset.

to execute the task;

- If the target frequency F_{target} is not available on the PE, the 2 PMs that surround F_{target} and which are in the discretely convex subset \mathbb{S} are applied.

Now, the power consumed by executing a task with a target frequency F_{target} which is available on the PE but corresponding to a PM that does not belong to the discretely convex set is compared to the power consumed when executing the task with 2 PMs in the discretely convex set so as to attain F_{target} on average. For instance, consider the target frequency F_{target} associated to PM_4 . Executing the task with PM_3 and PM_5 (see Table II) provides to gain 26.04% in the power consumption. Now, if the target frequency F_{target} corresponds to PM_2 , the task will be processed with PM_1 and PM_3 (see Table III). In this case, the gain in power consumption amounts to 27.55%. Note that the gain in power consumption is not absolute: the 2 examples given here only the capability of the methodology proposed. A similar study might be done with different activities. Indeed, the total power consumption depends on the average activity. However, the PMs position has to be reevaluated. Then the selection of PMs has to be re-executed as it has been shown in [4] that the gain in power consumption depends on the PMs distribution.

To summarize, the selection of PMs is a necessary phase

TABLE II: PMs selected to execute the task with F_{target} corresponding to PM_4 .

PM	PM_1	PM_2	PM_3	PM_4	PM_5	PM_6
Execution			X		X	

TABLE III: PMs selected to execute the task with F_{target} corresponding to PM_2 .

PM	PM_1	PM_2	PM_3	PM_4	PM_5	PM_6
Execution	X		X			

since it ensures a gain in power consumption if the set S is not globally discretely convex. However, the gain in consumption depends on the workload and on the PMs distribution [4].

VI. CONCLUSION AND FUTURE WORKS

In this paper, the power management problem for a PE when n PMs are available is studied. Most of the works in the literature execute a given task with the 2 neighbor frequencies of F_{target} . However, this choice is not always optimal from a power consumption point of view because the set of available PMs is not ensured to fulfil the convexity property anymore. Actually, to be energy efficient the task has to be performed with PMs belonging to a convex set. The method proposed here overtakes this problem by selecting the PMs that form a discretely convex subset. Furthermore, the proof is given in Appendix. This methodology is exemplified in the case of a discrete set of PMs available on the PE, considering 3 actuators. The proposition takes into account the behavior induced by new technologies as tuning parameters have effects on the convexity of the power/speed curve (e.g. V_{bb}). Numerical results are given to illustrate the proposed power management methodology. They are obtained from the simulation of a ring oscillator in STMicroelectronics 28nm FD-SOI technology. These results attest that executing tasks with PMs in the discretely convex subset permits to save up to 27.55% of power consumption.

In future works, the presented method will take into account the switching power consumption overhead. Actually, the switching power consumption could reduce the gain obtained by applying the methodology.

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APPENDIX

Proof

\mathbb{F} is the set of frequency $F_n \in \mathbb{R}$ applicable to the circuit and \mathbb{P} is the set of power $P_n \in \mathbb{R}$ such that $P : F_n \rightarrow P_n, \forall n \in \mathbb{N}^*$. $P(F)$ is supposed to be an increasing set. Let $F_{n-1}, F_n, F_{n+1} \in \mathbb{F}$, such that $F_{n-1} < F_n < F_{n+1}$. As

\mathbb{P} is increasing on \mathbb{F} , $P_{n-1} \leq P_n \leq P_{n+1}$. The notation $P_n^{(i,j)}$ (see Figures 11 and 12) is used to the value of the power corresponding to the frequency F_n located on the line's segment which connects P_i and P_j with $i < j$, $\forall i, j \in \mathbb{N}^*$. The notation a_i^j (see Figures 11 and 12) corresponds to the slope of the segment of line which connects P_i and P_j .

Let's take an example to understand, the value of the power corresponding to the frequency F_4 located on the segment of line which links P_3 and P_6 will be noted $P_4^{(3,6)}$. The value corresponding to slope of the line's segment connecting P_3 and P_6 is noted a_3^6 .

A. Frequency above F_{target}

Let $F_{target} \notin \mathbb{F}$ the frequency to reach thanks to the "hopping" technique with $F_{n-1} < F_{target} < F_n$ such in the Figure 11. The aim is to prove that an operating in "hopping" execution between F_{n-1} and F_n will not consume more than an operating in "hopping" execution between F_{n-1} and F_{n+k} , $\forall k \in \mathbb{N}^*$, i.e. the goal is to demonstrate that:

$$P_{target}^{(n-1,n)} \leq P_{target}^{(n-1,n+k)}$$

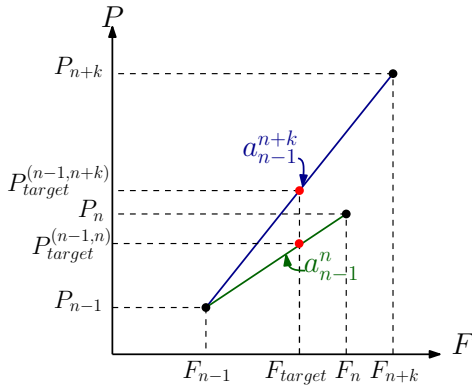


Fig. 11: Example of 3 possible frequencies in the plane (F, P) .

The value corresponding to F_{target} on the segment which connects P_{n-1} and P_{n+k} is calculated:

$$P_{target}^{(n-1,n+k)} = a_{n-1}^{n+k} \cdot (F_{target} - F_{n-1}) + P_{n-1} \quad (\text{A.2})$$

The value corresponding to F_{target} on the segment which connects P_{n-1} and P_n is calculated:

$$P_{target}^{(n-1,n)} = a_{n-1}^n \cdot (F_{target} - F_{n-1}) + P_{n-1} \quad (\text{A.3})$$

By subtracting (A.2) and (A.3) member-wise, the equation below is found:

$$P_{target}^{(n-1,n+k)} - P_{target}^{(n-1,n)} = (a_{n-1}^{n+k} - a_{n-1}^n) \cdot (F_{target} - F_{n-1}) \quad (\text{A.4})$$

By assumption:

$$\begin{aligned} F_{n-1} &< F_{target} < F_n \\ \Rightarrow F_{target} - F_{n-1} &> 0 \end{aligned}$$

By assumption, \mathbb{P} is a rising discretely convex set on \mathbb{F} so by definition:

$$\begin{aligned} a_{n-1}^n &\leq a_{n-1}^{n+k} \\ \Leftrightarrow a_{n-1}^{n+k} - a_{n-1}^n &\geq 0 \end{aligned}$$

Consequently, it can be deduced that:

$$\begin{aligned} P_{target}^{(n-1,n+k)} - P_{target}^{(n-1,n)} &\geq 0 \\ \Leftrightarrow P_{target}^{(n-1,n+k)} &\geq P_{target}^{(n-1,n)} \end{aligned}$$

It has been proved that the use of a frequency just above F_{target} will minimize the power consumption of the task executed in "hopping" execution if the set of power corresponding to frequencies which are able to be applied is discretely convex and increases in the plane (F, P) .

B. Frequency below F_{target}

Let $F_{target} \notin \mathbb{F}$ the frequency to reach by means of "hopping" technique with $F_n < F_{target} < F_{n+1}$ such in the Figure 12. The aim is to prove that an operating in "hopping" execution between F_n and F_{n+1} will not consume more than an operating in "hopping" execution between F_{n-k} and F_{n+1} , $1 \leq k < n$, $\forall k \in \mathbb{N}^*$, i.e. the purpose is to demonstrate that:

$$P_{target}^{(n-k,n+1)} \geq P_{target}^{(n,n+1)}$$

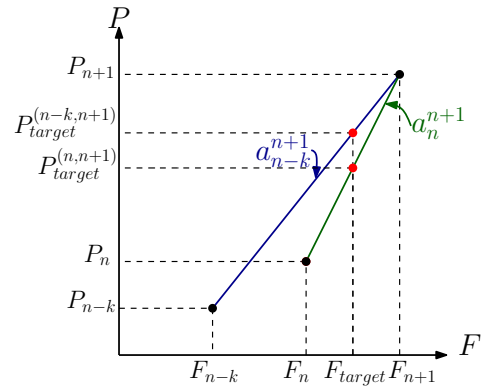


Fig. 12: Example of 3 possible frequencies in the plane (F, P) .

The value corresponding to F_{target} on the segment which connects P_{n-k} and P_{n+1} is calculated:

$$P_{target}^{(n-k,n+1)} = a_{n-k}^{n+1} \cdot (F_{target} - F_{n+1}) + P_{n+1} \quad (\text{A.5})$$

The value corresponding to F_{target} on the segment which connects P_n and P_{n+1} is calculated:

$$P_{target}^{(n,n+1)} = a_n^{n+1} \cdot (F_{target} - F_{n+1}) + P_{n+1} \quad (\text{A.6})$$

By subtracting (A.5) and (A.6) member-wise, the equation below is found:

$$P_{target}^{(n-k,n+1)} - P_{target}^{(n,n+1)} = (a_{n-k}^{n+1} - a_n^{n+1}) \cdot (F_{target} - F_{n+1}) \quad (\text{A.7})$$

By assumption:

$$\begin{aligned} F_n &< F_{target} < F_{n+1} \\ \Leftrightarrow F_{target} - F_{n+1} &< 0 \end{aligned}$$

By assumption, \mathbb{P} is a rising discretely convex set on \mathbb{F} so by definition:

$$\begin{aligned} a_{n-k}^{n+1} &\leq a_n^{n+1} \\ \Leftrightarrow a_{n-k}^{n+1} - a_n^{n+1} &\leq 0 \end{aligned}$$

Consequently, it can be deduced that:

$$\begin{aligned} P_{target}^{(n-k,n+1)} - P_{target}^{(n,n+1)} &\geq 0 \\ \Leftrightarrow P_{target}^{(n-k,n+1)} &\geq P_{target}^{(n,n+1)} \end{aligned}$$

It has been proved that the use of a frequency just below F_{target} will minimize the power consumption of the task executed in “hopping” execution if the set of power corresponding to frequencies which are able to be applied is discretely convex and increases in the plane (F, P) .

C. Frequencies framing F_{target}

Hence, from A and B, the use of the frequencies just below and just above to F_{target} in “hopping” execution will minimize the power consumption if the set of frequencies available forms a discretely convex and increasing set in the plane (F, P) . Note that this proposition is extended to a set of discretely convex points in the plane (F, P) .

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