

# **Efficient Leak Resistant Modular Exponentiation in RNS**

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# Efficient Leak Resistant Modular Exponentiation in RNS

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# **Outline**

#### 1 Cryptography

- RSA cryptosystem
- Power analysis
- Montgomery multiplication in RNS

#### 2 Randomized modular exponentiation in RNS

- Randomized Montgomery multiplication
- Proposed approach
- **•** Level of randomization



# **Outline**

#### 1 Cryptography

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- **C** Level of randomization

RSA encryption (Rivest, Shamir and Adleman)

Bob chooses p and q two large prime numbers and computes  $N = pq$ . He generates E and D two integers such that  $ED = 1$  (mod  $(p - 1)(q - 1)$ ).

- $\bullet$  Public Key: N, D.
- $\bullet$  Private Key: E, p, q.
- Alice encrypts a message *m* by:  $c = m^D$  mod *N*.
- Bob decrypts *c* by doing:  $c^E = m^{ED}$  mod  $N = m$ .

# An algorithm for modular exponentiation : Right-to-left Square-and-multiply

Require: A modulus N, an integer  $X \in [0, N]$  and an exponent  $E = (e_{\ell-1}, \ldots, e_0)_2$ **Ensure:**  $R = X^E$  (mod N) 1:  $R \leftarrow 1$ 2:  $Z \leftarrow X$ 3: for i from 0 to  $\ell - 1$ do 4: if  $e_i = 1$  then 5:  $R \leftarrow R \times Z \pmod{N}$  $6:$  end if 7:  $Z \leftarrow Z^2 \pmod{N}$ 8: end for 9: return R

$$
X^E=X^{\sum\limits_{i=0}^{\ell-1}e_i2^i}
$$

$$
X^{\mathsf{E}} = X^{e_{\ell-1} 2^{\ell-1}}{\small{\times}}\cdots{\small{\times}} X^{e_1 2^1}{\small{\times}} X^{e_0 2^0}
$$







Square-and-multiply
$R \leftarrow 1$
$Z \leftarrow X$
for $i = 0$ to $\ell - 1$ do
if $e_i = 1$ then
$R \leftarrow R \cdot Z \mod N$
endif
$Z \leftarrow Z^2 \mod N$
endfor
return( $R$ )

↑

Square-and-multiply-always  $R_0 \leftarrow 1$  $R_1 \leftarrow 1$  $\overline{Z} \leftarrow X$ for  $i = 0$  to  $\ell - 1$  do if  $e_i = 0$  then  $R_0 \leftarrow R_0 \cdot Z \mod N$ else  $R_1 \leftarrow R_1 \cdot Z \mod N$ endif endfor  $Z \leftarrow Z^2 \mod N$ return $(R_1)$ ↓ ↓  $\Omega$ 

Montgomery-ladder  $R \leftarrow 1$  $R' \leftarrow X$ for  $i = \ell$  to 1 do if  $k_i = 1$  then  $R \leftarrow R \cdot R' \mod N$  $R' \leftarrow R'^2 \mod N$ else  $R' \leftarrow R \cdot R' \mod N$  $R \leftarrow R^2$ endif endfor return $(R)$ 



 $6 / 19$ 

# Differential power analysis

$$
m = \frac{1}{2} \int_{\frac{1}{2} \text{A}} \int_{\frac{1}{2} \text{A}}
$$

#### Differential power analysis My Mandal Mandal Mandal m loop 1 loop 2 loop 3 loop 4 loop 5  $e_1 = 1$   $e_2 = 0$   $e_3 = 1$   $e_4 = 0$   $e_5 = ??$  $0 \times 5$  $r_1$  $r<sub>2</sub>$ r3 r4  $\overline{1}$ r 1 5

Differential power analysis  
\n
$$
m \frac{1}{n} \frac
$$

trace 1-MMANMANMANMANMANMANMANMANMANMANMAN trace 2-MMMMMMMMMMMMMMMMMMMMMMMMMMMMMMM trace 3 . . .

. . . . . . . . .

trace L-MMMMMMMMMMMMMMMMMMMMMMMMMMMMM

Differential power analysis loop 1 e<sup>1</sup> = 1 r1 loop 2 e<sup>2</sup> = 0 r2 loop 3 e<sup>3</sup> = 1 r3 loop 4 e<sup>4</sup> = 0 r4 loop 5 e<sup>5</sup> =?? m <sup>0</sup> r<sup>5</sup> r 0 5 1 trace 1 trace 2 trace 3 . . . . . . . . . . . . trace L correct guess wrong guess Differentials:



Counter-measure: Randomization of the exponent and data.

Basic modular multiplication. For  $X, Y \in [0, N]$ 

**O** Product.  $Z \leftarrow X \times Y$ 

2 Reduction.  $Q \leftarrow |Z/N|$  and  $R \leftarrow Z - Q \times N$ 

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Montgomery representation.

$$
\bullet \quad \widetilde{X} = XA \mod N \text{ provides}
$$

2  $\mathcal{M}$ ont $\mathcal{M}$ ul $(X, \hat{Y}) = (X\mathcal{A}) \times (\mathcal{Y}\mathcal{A}) \times \mathcal{A}^{-1}$  mod  $\mathcal{N} = XY\mathcal{A}$  mod  $\mathcal{N}$ 

• Let  $A = \{a_1, \ldots, a_t\}$  be a set t co-prime integers.

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- An integer  $X$  such that  $0 \leq X < A = \prod_{i=1}^t a_i$  is represented by

$$
[X]_{\mathcal{A}} = (x_1 = X \mod a_1, \ldots, x_t = X \mod a_t).
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$$

• The Chinese remainder theorem tell us that for op  $\in \{+, \times\}$  $[X]_{\mathcal{A}}$  op  $[Y]_{\mathcal{A}} = ([x_1 \text{ op } y_1]_{a_1}, \ldots, [x_t \text{ op } y_t]_{a_t}) \Leftrightarrow X$  op Y mod A

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#### Montgomery Multiplication in RNS

Require:  $X, Y$  in  $A \cup B$ Ensure:  $XYA^{-1}$  mod N in  $A \cup B$ 1:  $[Q]_{\mathcal{A}} \leftarrow [XYN^{-1}]_{\mathcal{A}}$ 

$$
3: [Z]_{\mathcal{B}} \leftarrow [(XY - QN)A^{-1}]_{\mathcal{B}}
$$

5: return  $(Z_{\mathcal{A}\cup\mathcal{B}})$ 

- Let  $A = \{a_1, \ldots, a_t\}$  be a set t co-prime integers.
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#### Montgomery Multiplication in RNS

```
Require: X, Y in A \cup BEnsure: XYA^{-1} mod N in A \cup B1: [Q]_{\mathcal{A}} \leftarrow [XYN^{-1}]_{\mathcal{A}}2: [Q]_B \leftarrow BE_{A\rightarrow B}([Q]_A)3: [Z]_\mathcal{B} \leftarrow [(XY - QN)A^{-1}]_\mathcal{B}4: [Z]_{\mathcal{A}} \leftarrow BE_{\mathcal{B} \rightarrow \mathcal{A}}([Z]_{\mathcal{B}})5: return (Z_{A\cup B})
```
# **Outline**

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#### Randomization in RNS (LRA CHES 2004) We have

$$
\widetilde{X}_{old} = [XA_{old}]_{A_{old} \cup B_{old}}
$$

we permute the basis elements  $A_{old} \cup B_{old} \rightarrow A_{new} \cup B_{new}$ 



this leads to a new representation of  $X$ 

$$
\widetilde{X}_{new} = [X A_{new}]_{A_{new} \cup B_{new}}
$$

#### Cost

Two Montgomery multiplications :

 $XA_{old}$  mod  $N \rightarrow XA_{old}A_{new}$  mod  $N \rightarrow XA_{new}$  mod N.  $11 / 1$ 

- Input:  $N, X \in [0, N], E = (e_{\ell-1}, \ldots, e_0)_2$  and  $\mathcal{M} = \{m_1, \ldots, m_{2t}\}.$
- Output:  $X^E$  mod  $N$

```
Square-and-mult-always
    \mathcal{A}, \mathcal{B} \leftarrow random split \mathcal{M}\widetilde{Z} \leftarrow [\widetilde{X}]_{A\cup B},R_0 \leftarrow [\tilde{1}]_{A\cup\mathcal{B}}, R_1 \leftarrow [\tilde{1}]_{A\cup\mathcal{B}}for i from 0 to \ell - 1 do
            R_{e_i} \leftarrow MM\_RNS(R_{e_i}, Z, A, B)<br>
\approx \approx \approx \approx \approx \approx \approx \approx\widetilde{Z} \leftarrow \text{MM\_RNS}(\widetilde{Z}, \widetilde{Z}, A, B)end for
     return R_1
```
• Input:  $N, X \in [0, N], E = (e_{\ell-1}, \ldots, e_0)_2$  and  $\mathcal{M} = \{m_1, \ldots, m_{2t}\}.$ Output:  $X^E$  mod  $N$ 

```
Randomized
Square-and-mult-always
     \mathcal{A}, \mathcal{B} \leftarrow random split \mathcal{M}Z \leftarrow [X]_{A\cup B},
     \widetilde{R}_0 \leftarrow [\widetilde{1}]_{A\cup\mathcal{B}}, \widetilde{R}_1 \leftarrow [\widetilde{1}]_{A\cup\mathcal{B}}for i from 0 to \ell - 1 do
            R_{e_i} \leftarrow MM\_RNS(R_{e_i}, Z, A, B)<br>
\approx \approx \approx \approx \approx \approx \approx \approxZ \leftarrow MM_RNS(Z, \bar{Z}, A, B)Randomise(A_{old}, B_{old}, A, B)
           \widetilde{Z} \leftarrow \mathsf{Update}(Z, \mathcal{A}_{old}, \mathcal{B}_{old}, \mathcal{A}, \mathcal{B})\widetilde{R}_0 \leftarrow \mathsf{Update}(\widetilde{R}_0, \mathcal{A}_{old}, \mathcal{B}_{old}, \mathcal{A}, \mathcal{B})R_1 \leftarrow Update(R_1, \mathcal{A}_{old}, \mathcal{B}_{old}, \mathcal{A}, \mathcal{B})end for
     return R_1
```
• Input:  $N, X \in [0, N], E = (e_{\ell-1}, \ldots, e_0)_2$  and  $\mathcal{M} = \{m_1, \ldots, m_{2t}\}.$ Output:  $X^E$  mod  $N$ 

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           Z \leftarrow Update(Z, \mathcal{A}_{old}, \mathcal{B}_{old}, \mathcal{A}, \mathcal{B})\widetilde{R}_0 \leftarrow Update(\widetilde{R}_0, \mathcal{A}_{old}, \mathcal{B}_{old}, \mathcal{A}, \mathcal{B})
           \widetilde{R}_1 \leftarrow Update(\widetilde{R}_1, \mathcal{A}_{old}, \mathcal{B}_{old}, \mathcal{A}, \mathcal{B})
     end for
     return R_1
```
• Input:  $N, X \in [0, N], E = (e_{\ell-1}, \ldots, e_0)_2$  and  $\mathcal{M} = \{m_1, \ldots, m_{2t}\}.$ Output:  $X^E$  mod  $N$ 



For  $E = 7 = (111)_2$  and  $\mathcal{M} = \{m_1, m_2, m_3, m_4\}$ 

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 $\bullet$  Initialization:  $\mathcal{A} = \{m_1, m_2\}, \mathcal{B} = \{m_3, m_4\}$  leads to

$$
R_1 = m_1 m_2 \mod N
$$
  

$$
Z = Xm_1 m_2 \mod N
$$

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$$
  

$$
Z = Xm_1 m_2 \mod N
$$

• Loop 1:  $A_1 = \{m_2, m_4\}, B_1 = \{m_1, m_3\}$  we get  $R_1 = (m_1 m_2) \times (X m_1 m_2)$  $\frac{1}{z}$ Z  $\times (m_2^{-1}m_4^{-1}) = Xm_1^2m_2m_4^{-1}$ Mont. factor

For  $E = 7 = (111)_2$  and  $\mathcal{M} = \{m_1, m_2, m_3, m_4\}$ 

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$$
R_1 = m_1 m_2 \mod N
$$
  

$$
Z = X m_1 m_2 \mod N
$$

• Loop 1: 
$$
A_1 = \{m_2, m_4\}, B_1 = \{m_1, m_3\}
$$
 we get  
\n
$$
R_1 = (m_1 m_2) \times \underbrace{(X m_1 m_2)}_{Z} \times \underbrace{(m_2^{-1} m_4^{-1})}_{\text{Mont. factor}} = X m_1^2 m_2 m_4^{-1}
$$
\n
$$
A = \{m_1, m_3\}, B = \{m_2, m_4\} \text{ leads to}
$$
\n
$$
Z = X^2 m_1 m_3
$$

For  $E = 7 = (111)$ <sub>2</sub> and  $\mathcal{M} = \{m_1, m_2, m_3, m_4\}$ • Initialization:  $A = \{m_1, m_2\}, B = \{m_3, m_4\}$  leads to  $R_1 = m_1 m_2 \mod N$  $Z = Xm_1m_2 \mod N$ • Loop 1:  $A_1 = \{m_2, m_4\}, B_1 = \{m_1, m_3\}$  we get  $R_1 = (m_1 m_2) \times (X m_1 m_2)$  ${\gamma}$  $\times (m_2^{-1}m_4^{-1})$ Mont. factor  $= X m_1^2 m_2 m_4^{-1}$  $\mathcal{A} = \{m_1, m_3\}, \mathcal{B} = \{m_2, m_4\}$  leads to  $Z = X^2 m_1 m_3$ 

• Loop 2: 
$$
A_1 = \{m_1, m_4\}, B_1 = \{m_2, m_3\}
$$
 we get  

$$
R_1 = Xm_1^2 m_2 m_4^{-1} \times (X^2 m_1 m_3) \times (m_1^{-1} m_4^{-1}) = X^3 m_1^2 m_2 m_3 m_4^{-2}
$$

For  $E = 7 = (111)$ <sub>2</sub> and  $\mathcal{M} = \{m_1, m_2, m_3, m_4\}$ • Initialization:  $A = \{m_1, m_2\}, B = \{m_3, m_4\}$  leads to  $R_1 = m_1 m_2 \mod N$  $Z = Xm_1m_2 \mod N$ • Loop 1:  $A_1 = \{m_2, m_4\}, B_1 = \{m_1, m_3\}$  we get  $R_1 = (m_1 m_2) \times (X m_1 m_2)$  ${\gamma}$  $\times (m_2^{-1}m_4^{-1})$ Mont. factor  $= X m_1^2 m_2 m_4^{-1}$  $\mathcal{A} = \{m_1, m_3\}, \mathcal{B} = \{m_2, m_4\}$  leads to  $Z = X^2 m_1 m_3$ 

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$$
A_1 = \{m_1, m_4\}, B_1 = \{m_2, m_3\}
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R_1 = Xm_1^2 m_2 m_4^{-1} \times (X^2 m_1 m_3) \times (m_1^{-1} m_4^{-1}) = X^3 m_1^2 m_2 m_3 m_4^{-2}
$$

Etc.

### Random evolution of the mask

After i loop iterations we have

$$
\widetilde{R}_1^{(i)} = X^{\sum_{j=0}^{i-1} e_j 2^j} \times \prod_{j=0}^{2t} m_j^{\gamma_j^{(i)}} \mod N
$$

and each  $\gamma_i^{(i)}$  $j^{\left( \prime \right) }$  evolves randomly as

$$
\gamma_j^{(i+1)} = \gamma_j^{(i)} + \delta_j^{(i)}
$$
 with  $\delta_j^{(i)} \in \{-1, 0, 1\}$  and 
$$
\begin{cases} \mathbb{P}(\delta_j^{(i)} = 1) = 1/8, \\ \mathbb{P}(\delta_j^{(i)} = -1) = 1/8, \\ \mathbb{P}(\delta_j^{(i)} = 0) = 3/4. \end{cases}
$$



### Removing the final mask

Problem: at the end we have to remove the final mask  $\prod_{j=1}^{2t} m_j^{\gamma^{(\ell)}}$  from

$$
\widetilde{X}=X^E\cdot\prod_{j=1}^{2t}m_j^{\gamma_j^{(\ell)}}\mod N.
$$

Strategy: we force  $\gamma_i^{(\ell)}$  $j^{(\ell)}$  to be equal 0 as follows

- During the first half of the iterations each  $\gamma_i^{(i)}$  $j^{\left(\prime\right)}$  evolves freely.
- During the second half we constrain each  $|\gamma_i^{(i)}\rangle$  $\binom{y}{j}$  to decrease toward 0.



#### Level of randomization

• The probabilities of the mask exponents satisfy

$$
\mathbb{P}(\gamma_j^{(i)} = d) = \sum_{k=d}^{d+\lfloor (i-d)/2 \rfloor} {i \choose k} {i-d \choose k-d} \left(\frac{1}{8}\right)^{2k-d} \left(\frac{3}{4}\right)^{i-2k+d}
$$
  

$$
\mathbb{P}(\Gamma^{(i)} = \Gamma) \leq \prod_{j=1}^t \mathbb{P}(\gamma_j^{(i)} = \gamma_j) \leq \prod_{j=1}^t \mathbb{P}(\gamma_j^{(i)} = 0)
$$

## Level of randomization

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$$
  

$$
\mathbb{P}(\Gamma^{(i)} = \Gamma) \leq \prod_{j=1}^t \mathbb{P}(\gamma_j^{(i)} = \gamma_j) \leq \prod_{j=1}^t \mathbb{P}(\gamma_j^{(i)} = 0)
$$

• Comparison: for a 2048-bit RSA modulus and  $t = 32$ :

- $\triangleright$  CHES 04:
	- $\star$  Montgomery-ladder,
	- $\star$  4MM\_RNS per randomization,
	- $\star$  all masks are controled.
- ▶ Proposed:
	- $\star$  right-left square-and-multiply-always,
	- $\star$  2MM\_RNS per randomization
	- $\star$  the masks for  $R_0$  and  $R_1$  are not controled.



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#### **Conclusion**

# Conclusion

#### Secure embedded implementation of RSA:

- Randomized modular exponentiation
- But leak resistant arithmetic (CHES 04) is costly: 4 MM RNS per randomization

# Conclusion

#### Secure embedded implementation of RSA:

- Randomized modular exponentiation
- But leak resistant arithmetic (CHES 04) is costly: 4 MM\_RNS per randomization

We proposed:

- To apply LRA to right-to-left exponentiation.
- Avoid some correction of Montgomery Factor.
- This decreases the computational cost: 2 MM RNS per randomization.
- Increases the level of randomization after a small number of loop.

# Conclusion

#### Secure embedded implementation of RSA:

- Randomized modular exponentiation
- But leak resistant arithmetic (CHES 04) is costly: 4 MM\_RNS per randomization

We proposed:

- To apply LRA to right-to-left exponentiation.
- Avoid some correction of Montgomery Factor.
- This decreases the computational cost: 2 MM RNS per randomization.
- Increases the level of randomization after a small number of loop.

Perspectives:

- A better estimation of the level of randomization.
- Is it a good counter-measure against horizontal power analysis ?

# Thank you for your attention!