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Jesus Guerrero, Jorge Torres, Vincent Creuze, Ahmed Chemori, Eduardo Campos Mercado. Saturation based nonlinear PID control for underwater vehicles: Design, stability analysis and experiments. *Mechatronics*, 2019, 61, pp.96-105. 10.1016/j.mechatronics.2019.06.006 . lirmm-02163345

**HAL Id: lirmm-02163345**

**<https://hal-lirmm.ccsd.cnrs.fr/lirmm-02163345v1>**

Submitted on 24 Jun 2019

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# Saturation Based Nonlinear PID control for Underwater Vehicles: Design, Stability Analysis and Experiments

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## Abstract

During sea missions, underwater vehicles are **often** exposed to changes in the parameters of **their control** systems and subject to external disturbances due to the **influences of** ocean currents. These issues make the design of a robust controller quite **a** challenging task. This paper focuses on the design of a nonlinear PID controller, based on a set of saturation functions for trajectory tracking on an underwater vehicle. The main feature of the proposed control law is that it preserves the advantages of robust control and remains easy to **fine-tune** in real applications. Using **the** Lyapunov concept, we prove the asymptotic stability of the closed-loop tracking system. The effectiveness and robustness of **our** proposed controller for trajectory tracking in depth and yaw dynamics is demonstrated through real-time experiments.

*Keywords:* Underwater vehicle, non-linear PID control, trajectory tracking, real-time experiments.

*2010 MSC:* 00-01, 99-00

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## 1. Introduction

There are two main classes of Unmanned Underwater Vehicles (UUVs): Remotely Operated Vehicles (ROVs), and Autonomous Underwater Vehicles

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<sup>☆</sup>Fully documented templates

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(AUVs). Both require advanced controllers, as their dynamics are highly non  
5 linear and they have to deal with unpredictable external disturbances, such as  
the ones generated by ocean currents or by the tether [1]. In the case of AUVs,  
all of the degrees of freedom (DoF) are controlled, while in the case of ROVs a  
part of the DoF are piloted by a human (shared control). Both classes require  
controllers and this paper will refer to Underwater Vehicles in general.

10 Proportional-Derivative (PD) and Proportional Integral Derivative (PID)  
controllers are the most commonly used techniques to control the position and  
orientation of commercial underwater vehicles, this is due to their design sim-  
plicity and their good performance, especially when some system parameters  
are unknown [2, 3, 4]. However, it is well-known that when the plant's dynam-  
15 ics is highly nonlinear, time-varying, or with significant time delays the PID  
controls performance is often degraded. The impact of these drawbacks can be  
reduced by using adaptive, saturated or nonlinear PD/PID strategies. Inspired  
by this problem, several advanced PD/PID control schemes for underwater vehi-  
cles have been proposed in previous literature and some of them are summarized  
20 below.

It is acknowledged that the PID control tuning process to obtain the best  
controller behavior can be time-consuming. Consequently, intelligent tuning and  
self-adjusting control parameter methodologies have been developed in recent  
years. In [5], a genetic algorithm was used to tune the gains of a fractional  
25 order PID for setpoint regulation in depth and steering subsystems of an AUV.  
Following the same lines, a PID control was tuned using the Particle Swarm  
Optimization (PSO) method for setpoint regulation and trajectory tracking in  
diving and steering subsystems [6]. A Fuzzy Logic Controller (FLC) was used  
with the PID algorithm to tune its gains adaptively. For example, in [7], a  
30 decoupled Adaptive Fuzzy PID Controller (AFPIDC) for trajectory tracking in  
heading and depth of an AUV was proposed. In this work, the adaption law  
is composed of two elements, the initial constant control gains, given by the  
designer, and the time-varying incremental gains which depend on the tracking  
error and its ratio. The incremental gain is adjusted by fuzzy rules derived from

35 the expert's knowledge. Based on simulation results, the performance of the AFPIDC is superior to nominal PID design during tracking trajectory tests. Similar methodologies, using **fuzzy logic** to improve the PID controller for path following or to demonstrate its robustness with respect to external disturbances can be found in [8, 9]. Finally, inverse optimal PID control applied to a self-  
40 tuning controller for an AUV, modeled as a nonlinear autoregressive moving average model with exogenous inputs was proposed in [10].

The Active Disturbance Rejection Controller (ADRC) can estimate the influence of the external disturbances such as ocean currents or wave effects over an AUV. On **the** one hand, in paper [1], an adaptive DOB control (ADOB)  
45 for set point regulation and trajectory tracking **problems** on the 6 degrees of freedom of ODIN AUV was proposed. In this work, the proposed controller was designed for a known nominal model, where the external disturbances and modeling errors were estimated through the DOB method. Then, a regressor-free adaptive control law was adopted to provide robustness to the DOB control  
50 towards uncertainties in the system model. The effectiveness of the proposed methodology was shown through real-time experiments on the x-y-z dynamics, while the AUV's orientation was kept stable (i.e.,  $\phi = \theta = \psi = 0$ ). From these results, **we can observe** that the ADOB algorithm improves the performance of the PID controller considerably under constant external disturbances and parameter uncertainties. On the other hand, in [11], the DOB method was applied  
55 to the PID control of an AUV based on the frequency analysis approach. In [12], a diving ADRC has been proposed to deal with the high nonlinearity, strong coupling and time-varying features in the AUV system.

It is worth **noting** that, during sea missions, an AUV can be disturbed by  
60 ocean currents or subject to unknown objects **sticking** to the submarine body **which** suddenly **changes** its physical parameters. To overcome this problem, adaptive controllers **can be used** as a suitable solution to control AUVs. The main feature of an adaptive controller lies in its ability to update the control gains based on the changes in vehicle dynamics and external disturbances. As  
65 an example of this methodology, an adaptive PD controller for setpoint regula-

tion was proposed in [13]. The designed controller needed only the knowledge of the vector of gravitational and buoyancy forces. The control law consists of a PD plus buoyancy compensation (PD+) with an adaptive term that estimates and compensates parameter uncertainties and external disturbances.

70 The behavior of the adaptive controller was validated through simulations and real-time experiments for setpoint regulation in  $(x, y, z, \psi)$  dynamics. Based on the obtained experimental results, it can be observed that the adaptive control has a better performance in depth dynamics than the PD, but the behavior of both methodologies is almost the same for  $(x, y, \psi)$  dynamics. Also, following

75 the same methodology, an adaptive PD controller for a region reaching controller was proposed in [14]. We can compare this to [13], which is based on a saturated PD control instead of a linear PD law. Although the effectiveness of the proposed controller was only shown in simulations.

In practical applications, it can be observed that a standard PID control design can be improved by bounding its signal [15]. Consequently, several nonlinear bounded PID controllers have been proposed. For instance, in [16], a model reference adaptive (MRAC) PID control structure with an anti-windup (AW) compensator for pitch trajectory tracking of the REMUS AUV was proposed. It was demonstrated that adding the AW compensator improves the nominal

80 adaptive control. The AW term is obtained by solving a linear Riccati equation. Simulation results show the improvements of the proposed controller over the nominal MRAC in terms of external disturbances rejection and saturation of the AUV's actuators. Another version taking into account the saturation of the AUV's actuators, resulting in a  $\mu$  modified adaptive controller was proposed in

90 [17]. Also, a dual-loop variable-structure PID (VSPID) controller with AW term for controlling the surge and sway dynamics of an AUV is proposed in [18]. Experimental results show that the VSPID with AW reduces the overshoot as well as the settling time compared to the nominal VSPID. Finally, inspired by the works of [19] and [20], a nonlinear PD and PD+ controllers for trajectory tracking

95 on depth and yaw dynamics of an AUV has been proposed in [15]. In this work, the authors introduced a whole set of nonlinear functions to improve the

PD controller. Real-time experiments on the L2ROV vehicle demonstrate the effectiveness and robustness of the proposed control law. Indeed, **an improved** performance of the proposed controller for trajectory tracking in yaw dynamics **is** demonstrated. However, the performance of the controller for depth trajectory tracking is **reduced** when the system's parameters are subject to uncertainties.

In summary, on **the** one hand, **fuzzy** approaches [7] and intelligent algorithms such as PSO and AG (see [5],[6]), which are used to tune the PID control, can be useful to obtain good performance **from** the controller. On the other hand, the disturbance estimation made by ADRC can provide robustness to the PID, as seen in the experiments shown in references [1], [11], [12]. However, based on the experimental results of these works, the robustness improvement of this methodology towards parameter uncertainties or external disturbances is not clear. Furthermore, the main ADRC drawback is the tedious task of tuning numerous parameters. Concerning the adaptive controllers [13],[14], **their** main advantages are the self-adjustment of gains and the fact that only partial information about the vehicle's mathematical model is **required**. However, the low rate of gains adjustment and the overestimation of feedback gains **remains a drawback to** this method. Continuing, the MRAC with the AW term can improve PID performance, as shown in the simulation results of study [16]. Nevertheless, the proposed methodology requires **computing** the Ricatti equation **online**, which could be difficult. Finally, the introduction of saturation functions in the gains of the PD controller improves its performance, as one can see in the experimental results of work [15]. However, this methodology is not robust enough **to encompass** large and persistent parameter uncertainties. Taking into account this drawback, in this paper, a nonlinear PID controller is proposed to overcome the shortcoming of the previous algorithm introduced in [15]. The main contributions of the actual work are summarized as follows:

- (i) A whole **range** of nonlinear functions to improve the PID controller **are** proposed.
- (ii) The stability analysis of the proposed controller is formalized based on

Lyapunov design.

- (iii) External disturbance rejection and robustness towards parameter uncertainties are demonstrated through real-time experiments.
- 130 (iv) Compared to previous work [15], the speed in the time-varying yaw trajectory is increased twice during experiments.

This paper is organized as follows: a description of the dynamic model of the underwater vehicle is given in Section 2. The proposed control technique is described in Section 3. **Real-time** experimental results for trajectory tracking  
 135 of two DoF of the submarine are presented and, discussed in Section 4. Finally, some concluding remarks, and future work on the proposed controller are **presented** in Section 5.

## 2. Dynamic Model

The dynamic model of underwater vehicles **has** been described in several  
 140 references (see [3, 21, 22] **for examples**).

The dynamics of an underwater vehicle involves two frames of reference: the body-fixed frame and the earth-fixed frame (as illustrated in Figure 1). Considering the generalized inertial forces, hydrodynamic effects, gravity and buoyancy contributions as well as the forces of actuators (i.e., thrusters), the  
 145 dynamic model of an underwater vehicle in matrix form, using the SNAME (Society of Naval Architects and Marine Engineers) notation [23] and the representation introduced by [3], can be written as follows:

$$\begin{aligned}
 M\dot{\nu} + C(\nu)\nu + D(\nu)\nu + g(\eta) &= \tau + w_e(t) \\
 \dot{\eta} &= J(\eta)\nu
 \end{aligned}
 \tag{1}$$

where  $\nu = [u, v, w, p, q, r]^T$  is the vector of velocity in the body-fixed frame and  $\eta = [x, y, z, \phi, \theta, \psi]^T$  represents the vector of position and orientation in the  
 150 earth-fixed frame.  $J(\eta) \in \mathbb{R}^{6 \times 6}$  is the transformation matrix between the inertial frame and the body-fixed frame.  $M \in \mathbb{R}^{6 \times 6}$  is the inertia matrix where the

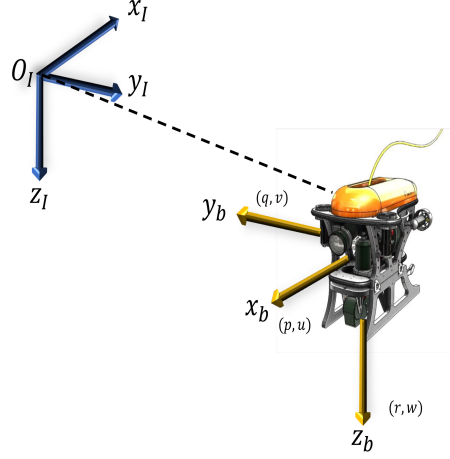


Figure 1: The **underwater** vehicle with the inertial-fixed frame  $(O_I, x_I, y_I, z_I)$  and the body-fixed frame  $(O_b, x_b, y_b, z_b)$ .

effects of added mass are considered,  $C(\nu) \in \mathbb{R}^{6 \times 6}$  is the Coriolis-centripetal matrix,  $D(\nu) \in \mathbb{R}^{6 \times 6}$  **representing** the hydrodynamic damping matrix also including the effects of added-mass,  $g(\eta) \in \mathbb{R}^6$  is the vector of gravitational/buoyancy forces and moments. Finally,  $\tau \in \mathbb{R}^6$  is the control input vector acting on the   
 155 underwater vehicle and  $w_e(t) \in \mathbb{R}^6$  represents the vector of external disturbances.

The above formulation **for** underwater vehicle dynamics is expressed in the body-fixed frame and can be transformed to the earth-fixed frame based on the kinematic transformations of the state variables and the model parameters as   
 160 follows:

$$\begin{aligned}
 M_\eta(\eta) &= J^{-T}(\eta) M J^{-1}(\eta) \\
 C_\eta(\nu, \eta) &= J^{-T}(\eta) \left[ C(\nu) - M J^{-1}(\eta) \dot{J}(\eta) \right] J^{-1}(\eta) \\
 D_\eta(\nu, \eta) &= J^{-T}(\eta) D(\nu) J^{-1}(\eta) \\
 g_\eta(\eta) &= J^{-T}(\eta) g(\eta) \\
 \tau_\eta(\eta) &= J^{-T}(\eta) \tau
 \end{aligned}$$

Based on these **equations**, the dynamics (1) can therefore be rewritten in the



earth-fixed frame as:

$$M_\eta(\eta)\ddot{\eta} + C_\eta(\nu, \eta)\dot{\eta} + D_\eta(\nu, \eta)\dot{\eta} + g_\eta(\eta) = \tau_\eta(\eta) + w_\eta(t) \quad (2)$$

For a deeper description of the model, the reader **may** refer to [3, 24].

### 3. Proposed Nonlinear PID Controller

In this section, a nonlinear PID controller based on saturation functions with variable parameters is introduced. The design of the controller is focused on both setpoint regulation, as well as trajectory tracking. The stability analysis of the resulting closed-loop system for both cases is **explained in detail**. Let us consider the underwater vehicle mathematical model (2), and the following control law

$$\tau = J^T \left[ M_\eta(\eta)\ddot{\eta}_d + C_\eta(\nu, \eta)\dot{\eta}_d + D_\eta(\nu, \eta)\dot{\eta}_d + g(\eta) - \tau_{PID} \right] \quad (3)$$

where the PID controller is defined as follows:

$$\tau_{PID} = K_p e(t) + K_i \int_0^t e(s) ds + K_d \frac{de(t)}{dt} \quad (4)$$

165 The feedback gains are defined as  $K_p = \text{diag}(k_{p1}, k_{p2}, \dots, k_{p6}) > 0$ ,  $K_i = \text{diag}(k_{i1}, k_{i2}, \dots, k_{i6}) > 0$ , and  $K_d = \text{diag}(k_{d1}, k_{d2}, \dots, k_{d6}) > 0$ , where  $k_{pj}$ ,  $k_{ij}$  and  $k_{dj}$  are positive constants for all  $j = 1, \dots, 6$ . The error is expressed as  $e(t) = [e_1(t), e_2(t), \dots, e_6(t)]^T = \eta(t) - \eta_d(t)$ , with  $\eta_d(t)$  the desired trajectory vector.

In order to improve the performance of the closed-loop system, we propose **introducing** a saturation function  $\sigma_{\bar{b}}(h)$  defined **as**:

$$\sigma_{\bar{b}}(h) = \begin{cases} \bar{b} & \text{if } h > \bar{b} \\ h & \text{if } |h| \leq \bar{b} \\ -\bar{b} & \text{if } h < -\bar{b} \end{cases} \quad (5)$$

where  $\bar{b}$  is a positive constant, and  $h$  represents a linear function. In this paper, the terms to which this saturation will be applied are the tracking error, its

integral, and its time derivative. Then, if we consider this saturation with the previous control law, we obtain the following nonlinear PID (NLPID) controller:

$$\tau_{NLPID} = \sigma_{\bar{b}_p} \left[ K_p e(t) \right] + \sigma_{\bar{b}_i} \left[ K_i \int_0^t e(s) ds \right] + \sigma_{\bar{b}_d} \left[ K_d \frac{de(t)}{dt} \right] \quad (6)$$

where

$$\sigma_{\bar{b}_p} [K_p e(t)] = \begin{bmatrix} u_{p1} & 0 & \cdots & 0 \\ 0 & u_{p2} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & u_{p6} \end{bmatrix} \quad (7)$$

$$\sigma_{\bar{b}_i} \left[ K_i \int_0^t e(s) ds \right] = \begin{bmatrix} u_{i1} & 0 & \cdots & 0 \\ 0 & u_{i2} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & u_{i6} \end{bmatrix} \quad (8)$$

$$\sigma_{\bar{b}_d} \left[ K_d \frac{de(t)}{dt} \right] = \begin{bmatrix} u_{d1} & 0 & \cdots & 0 \\ 0 & u_{d2} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & u_{d6} \end{bmatrix} \quad (9)$$

170 with  $u_{p_j} = \sigma_{\bar{b}_{p_j}} [k_{p_j} e_j(t)]$ ,  $u_{i_j} = \sigma_{\bar{b}_{i_j}} [k_{i_j} \int_0^t e_j(s) ds]$ , and  $u_{d_j} = \sigma_{\bar{b}_{d_j}} [k_{d_j} \frac{de_j(t)}{dt}]$  for all  $j = 1, \dots, 6$ .

Without loss of generality, let us now consider the scalar case:

$$\tau_{NLPID1} = \sigma_{\bar{b}_{p1}} [k_{p1} e_1(t)] + \sigma_{\bar{b}_{i1}} \left[ k_{i1} \int_0^t e_1(s) ds \right] + \sigma_{\bar{b}_{d1}} \left[ k_{d1} \frac{de_1(t)}{dt} \right] \quad (10)$$

The above equation can be rewritten in a compact form as follows:

$$\tau_{NLPID1} = \sum_{n=1}^3 u_n \quad (11)$$

where  $u_n = \sigma_{\bar{b}_n} (k_n h_n)$  represents the saturation function, with  $\bar{b}_1 = \bar{b}_{p1}$ ,  $\bar{b}_2 = \bar{b}_{i1}$ ,  $\bar{b}_3 = \bar{b}_{d1}$ , and the controller feedback gains  $k_1 = k_{p1}$ ,  $k_2 = k_{i1}$ ,  $k_3 = k_{d1}$ . The error term, its integral and its time derivative are represented by  $h_1, h_2$ ,

and  $h_3$ , respectively. Then, from equation (5),  $u_n$  can be rewritten as:

$$u_n = \begin{cases} \bar{b}_n & \text{if } k_n h_n > \bar{b}_n \\ k_n h_n & \text{if } |k_n h_n| \leq \bar{b}_n \\ -\bar{b}_n & \text{if } k_n < -\bar{b}_n \end{cases} \quad (12)$$

In the above equation, we can **observe** that the linear function  $k_n h_n$  is saturated by  $|h_n| = \bar{b}_n/k_n$ . Let us define  $d_n$  as:

$$d_n = \bar{b}_n/k_n \quad (13)$$

Then, (12) can be rewritten as follows:

$$u_n = \begin{cases} \text{sgn}(h_n)\bar{b}_n & \text{if } |h_n| > d_n \\ \bar{b}_n \bar{d}_n^{-1} h_n & \text{if } |h_n| \leq d_n \end{cases} \quad (14)$$

where tuning parameters of the controller are  $b_n$  and  $d_n$ , for  $n = 1, 2, 3$ . Moreover, considering that:

$$\text{sgn}(h_n)\bar{b}_n = h_n \text{sgn}(h_n)\bar{b}_n \bar{h}_n^{-1} \quad (15)$$

which can be simplified as:

$$\text{sgn}(h_n)\bar{b}_n = |h_n|\bar{b}_n \bar{h}_n^{-1} \quad (16)$$

and considering that  $|h_n|h_n^{-1} = |h_n|^{-1}h_n$ , equation (14) can be rewritten as follows:

$$u_n = \begin{cases} \bar{b}_n|h_n|^{-1}h_n & \text{if } |h_n| > d_n \\ \bar{b}_n \bar{d}_n^{-1} h_n & \text{if } |h_n| \leq d_n \end{cases} \quad (17)$$

Consequently, the control law (10) can be rewritten as follows:

$$\tau_{NLPID1} = u_1 + u_2 + u_3 = k_{p1}(\cdot)e_1(t) + k_{i1}(\cdot) \int_0^t e_1(s)ds + k_{d1}(\cdot)\dot{e}_1(t) \quad (18)$$

with

$$k_{p1}(\cdot) = \begin{cases} \bar{b}_{p1}|e(t)|^{-1} & \text{if } |e_1(t)| > d_{p1} \\ \bar{b}_{p1}\bar{d}_{p1}^{-1} & \text{if } |e_1(t)| \leq d_{p1} \end{cases} \quad (19)$$

$$k_{i1}(\cdot) = \begin{cases} \bar{b}_{i1}|\int_0^t e_1(s)|^{-1}ds & \text{if } |\int_0^t e_1(s)|ds > d_{i1} \\ \bar{b}_{i1}\bar{d}_{i1}^{-1} & \text{if } |\int_0^t e_1(s)|ds \leq d_{i1} \end{cases} \quad (20)$$

$$k_{d1}(\cdot) = \begin{cases} \bar{b}_{d1}|\dot{e}_1(t)|^{-1} & \text{if } |\dot{e}_1(t)| > d_{d1} \\ \bar{b}_{d1}\bar{d}_{d1}^{-1} & \text{if } |\dot{e}_1(t)| \leq d_{d1} \end{cases} \quad (21)$$

The advantage of this formulation is that the forces and torques are bounded by the saturation parameters  $\bar{b}_{p1}$ ,  $\bar{b}_{i1}$  and  $\bar{b}_{d1}$ . Consequently, the saturation of the control input is guaranteed. However, some cases may require slightly larger forces and torques to correct the system errors, that is why we propose to change the saturation value  $\bar{b}_n$  in equation (18) as follows:

$$\bar{b}_n = \begin{cases} b_n|h_n|^{\mu_n} & \text{if } |h_n| > d_n \\ b_n|d_n|^{\mu_n} & \text{if } |h_n| \leq d_n \end{cases} \quad (22)$$

$b_n$  being a positive constant, and  $\mu_n \in [0, 1]$ . Now, introducing equations (22) into (17), leads to:

$$u_n = \begin{cases} \bar{b}_n|h_n|^{\mu_n}|h_n|^{-1}h_n & \text{if } |h_n| > d_n \\ \bar{b}_n|d_n|^{\mu_n}\bar{d}_n^{-1}h_n & \text{if } |h_n| \leq d_n \end{cases} \quad (23)$$

Note that the shape of the function  $u_n$  depends on the selected parameter value  $\mu_n$  as illustrated in Figure 2. Consequently, the nonlinear PID control law based on saturation functions with variable parameters can be expressed as:

$$\tau_{NLPIDj} = k_{pj}(\cdot)e_j(t) + k_{ij}(\cdot)\int_0^t e_j(s)ds + k_{dj}(\cdot)\dot{e}_j(t) \quad (24)$$

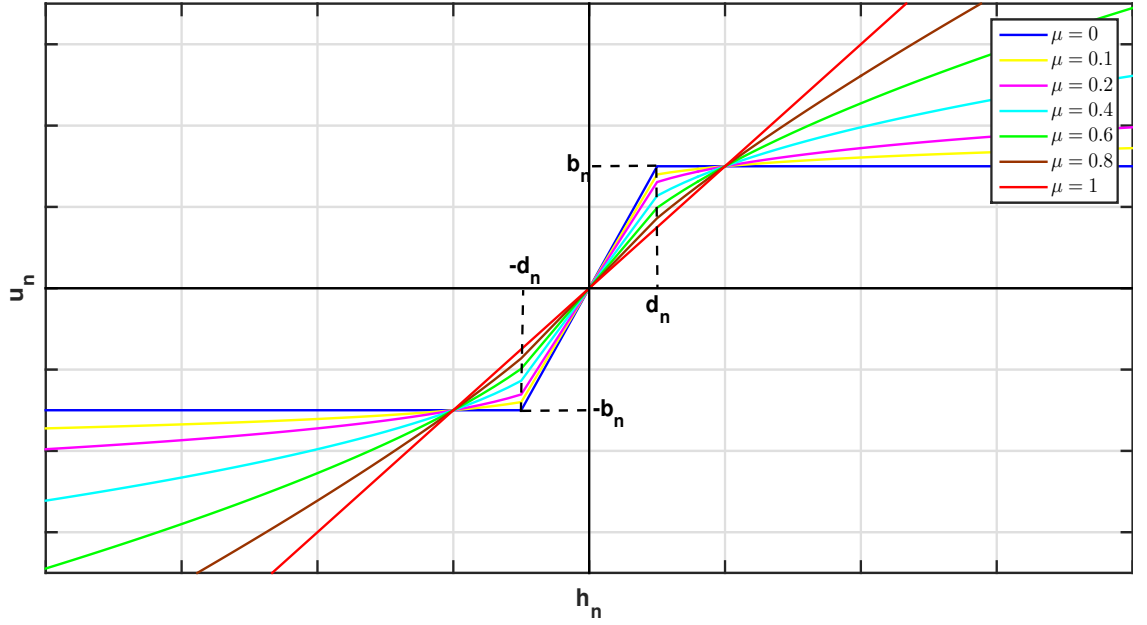


Figure 2: Illustration of the saturation function  $u_n$  for different values of the parameter  $\mu_n$ .

with:

$$k_{pj}(\cdot) = \begin{cases} \bar{b}_{pj} |e_j(t)|^{(\mu_{pj}-1)} & \text{if } |e_j(t)| > d_{pj} \\ \bar{b}_{pj} \bar{d}_{pj}^{(\mu_{pj}-1)} & \text{if } |e_j(t)| \leq d_{pj} \end{cases} \quad (25)$$

$$k_{ij}(\cdot) = \begin{cases} \bar{b}_{ij} |\int_0^t e_j(s)|^{(\mu_{ij}-1)} ds & \text{if } |\int_0^t e_j(s)| ds > d_{ij} \\ \bar{b}_{ij} \bar{d}_{ij}^{(\mu_{ij}-1)} & \text{if } |\int_0^t e_j(s)| ds \leq d_{ij} \end{cases} \quad (26)$$

$$k_{dj}(\cdot) = \begin{cases} \bar{b}_{dj} |\dot{e}_j(t)|^{(\mu_{dj}-1)} & \text{if } |\dot{e}_j(t)| > d_{dj} \\ \bar{b}_{dj} \bar{d}_{dj}^{(\mu_{dj}-1)} & \text{if } |\dot{e}_j(t)| \leq d_{dj} \end{cases} \quad (27)$$

$$\forall \mu_{pj}, \mu_{ij}, \mu_{dj} \in [0, 1]$$

### 3.1. Stability Analysis

Let us consider the nonlinear PID controller given as (24) and define the gain matrices as follows:

$$K'_p(\cdot) = K_p(\cdot) - \frac{1}{\alpha} K_i(\cdot) \quad (28)$$

$$K'_i(\cdot) = \frac{1}{\alpha} K_i(\cdot) \quad (29)$$

$$\zeta = \int_0^t [\alpha e(s) + \dot{e}(s)] ds \quad (30)$$

with  $K_p(\cdot) = \text{diag}(k_{p1}(\cdot), k_{p2}(\cdot), k_{p3}(\cdot), k_{p4}(\cdot), k_{p5}(\cdot), k_{p6}(\cdot)) > 0$  and  $K_i(\cdot) = \text{diag}(k_{i1}(\cdot), k_{i2}(\cdot), k_{i3}(\cdot), k_{i4}(\cdot), k_{i5}(\cdot), k_{i6}(\cdot)) > 0$ .

The complete control law (3) taking into account the nonlinear PID (24), can be rewritten in the following form:

$$\tau = J^T(\eta) \left[ M_\eta(\eta) \ddot{\eta}_d + C_\eta(\nu, \eta) \dot{\eta}_d + D_\eta(\nu, \eta) \dot{\eta}_d + g(\eta) - K'_p(\cdot) e - K_d(\cdot) \dot{e} - K'_i(\cdot) \zeta \right] \quad (31)$$

with  $K_d(\cdot) = \text{diag}(k_{d1}(\cdot), k_{d2}(\cdot), k_{d3}(\cdot), k_{d4}(\cdot), k_{d5}(\cdot), k_{d6}(\cdot)) > 0$ .

Injecting the PID control (31) into dynamic system (2), leads to the following closed loop system:

$$\ddot{e} = M_\eta(\eta)^{-1} \left[ -C_\eta(\nu, \eta) \dot{e} - D_\eta(\nu, \eta) \dot{e} - K'_p(\cdot) e - K'_i(\cdot) \zeta - K_d(\cdot) \dot{e} \right] \quad (32)$$

which can be rewritten in an augmented state form as follows:

$$\frac{d}{dt} \begin{bmatrix} e \\ \dot{e} \\ \zeta \end{bmatrix} = \begin{bmatrix} \dot{e} \\ M_\eta(\eta)^{-1} \left[ -C_\eta(\nu, \eta) \dot{e} - D_\eta(\nu, \eta) \dot{e} - K'_p(\cdot) e - K'_i(\cdot) \zeta - K_d(\cdot) \dot{e} \right] \\ \alpha e + \dot{e} \end{bmatrix} \quad (33)$$

**Remark 1.** *Note that the origin of the state space model is a unique equilibrium point.*

180 **Remark 2.** *The main challenge is to find a Lyapunov candidate function that will allow us to take into account the auxiliary state variable  $\zeta$  as it appears in Eq. (33). As we will see below, this is not a trivial extension of the PD controller case, see [14].*

Consider the following Lyapunov Candidate Function:

$$\begin{aligned} V(e, \dot{e}, \zeta) = & \frac{1}{2} \dot{e}^T M_\eta(\eta) \dot{e} + \alpha e^T M_\eta(\eta) \dot{e} + \frac{\alpha}{2} e^T D_\eta e \\ & + \int_0^e \xi^T K_p'(\xi) d\xi + \int_0^\zeta \xi^T K_i'(\xi) d\xi + \alpha \int_0^e \xi^T K_d(\xi) d\xi \end{aligned} \quad (34)$$

which can be rewritten as follows:

$$\begin{aligned} V(e, \dot{e}, \zeta) = & \frac{1}{2} [\dot{e} + \alpha e]^T M_\eta(\eta) [\dot{e} + \alpha e] + \frac{\alpha}{2} e^T [D_\eta - \alpha M_\eta(\eta)] e + \\ & + \int_0^e \xi^T K_p'(\xi) d\xi + \int_0^\zeta \xi^T K_i'(\xi) d\xi + \alpha \int_0^e \xi^T K_d(\xi) d\xi \end{aligned} \quad (35)$$

To prove that the Lyapunov candidate function is a positive definite and radially unbounded, let us consider the following:

$$\begin{aligned} \int_0^e \xi^T K_p(\xi) d\xi = & \int_0^{e_1} \xi_1 k_{p1}(\xi_1) d\xi_1 + \int_0^{e_2} \xi_2 k_{p2}(\xi_2) d\xi_2 + \\ & + \int_0^{e_3} \xi_3 k_{p3}(\xi_3) d\xi_3 + \cdots + \int_0^{e_n} \xi_n k_{pn}(\xi_n) d\xi_n \end{aligned}$$

where the inequality

$$e_j k_{pj}(\cdot) \geq \alpha_j (|e_j|) \quad (36)$$

is satisfied with class- $K$  functions

$$\alpha_j(|e_j|) = \begin{cases} \frac{b_j |e_j|^{\mu_{pj}} e_j}{a + |e_j|} & \text{if } |e_j| > d_j \\ \frac{b_j |d_j|^{\mu_{pj}} e_j}{a + d_j} & \text{if } |e_j| \leq d_j \end{cases} \quad (37)$$

with  $b_{pj} > b_j$ ,  $a > 0$  and  $d_{pj} < d_j$ . Then, according to Lemma 2 from [8], we can deduce that:

$$\int_0^e \xi^T K_p(\xi) d\xi > 0 \quad \forall e \neq 0 \in \mathbb{R}^n \quad (38)$$

and

$$\int_0^e \xi^T K_p(\xi) d\xi \rightarrow \infty \quad \text{as } \|e\| \rightarrow \infty \quad (39)$$

Note that **by** following the same arguments, we can conclude that the next conditions are accomplished:

$$\int_0^\zeta \xi^T K_i(\xi) d\xi > 0 \quad \forall \zeta \neq 0 \in \mathbb{R}^n \quad (40)$$

$$\int_0^e \xi^T K_d(\xi) d\xi > 0 \quad \forall e \neq 0 \in \mathbb{R}^n \quad (41)$$

and

$$\int_0^\zeta \xi^T K_i(\xi) d\xi \rightarrow \infty \quad \text{as} \quad \|\zeta\| \rightarrow \infty \quad (42)$$

$$\int_0^e \xi^T K_d(\xi) d\xi \rightarrow \infty \quad \text{as} \quad \|e\| \rightarrow \infty \quad (43)$$

The term  $1/2[\dot{e} + \alpha e]^T M_\eta(\eta)[\dot{e} + \alpha e]$  is positive definite because the matrix  $M_\eta(\eta)$  is positive definite. Finally, the matrix  $D_\eta - \alpha M_\eta(\eta)$  is positive definite since:

$$\frac{D_{\eta i}}{\sum_{j=1}^n \max_\eta |M_{\eta ij}(\eta)|} > \alpha \quad (44)$$

where  $M_{\eta ij}(\eta)$  stands for the element of matrix  $M_\eta(\eta)$  placed at row  $i$  and column  $j$ . Therefore, the Lyapunov function candidate  $V(e, \dot{e}, \zeta)$  is positive definite and radially unbounded.

The time derivative of the Lyapunov candidate function, step by step, is given **as**:

$$\begin{aligned} \dot{V}(e, \dot{e}, \zeta) &= \dot{e}^T M_\eta \ddot{e} + \frac{1}{2} \dot{e}^T \dot{M}_\eta \dot{e} + \alpha \dot{e}^T M_\eta \dot{e} + \alpha e^T \dot{M}_\eta \dot{e} + \alpha e^T M_\eta \ddot{e} \\ &\quad + \alpha e^T K_d(\cdot) \dot{e} + e^T K'_p(\cdot) \dot{e} + \zeta^T K'_i(\cdot) \dot{\zeta} + \alpha e^T D_\eta \dot{e} \\ &= \frac{1}{2} \dot{e}^T [\dot{M}_\eta - 2C_\eta] \dot{e} - \dot{e}^T D_\eta \dot{e} - \dot{e}^T K_d(\cdot) \dot{e} + \alpha \dot{e}^T M_\eta \dot{e} + \alpha e^T \dot{M}_\eta \dot{e} \\ &\quad - \alpha e^T C_\eta \dot{e} - \alpha e^T K'_p(\cdot) e \end{aligned}$$

From the assumption that the vehicle is moving at low speed, we can assume that  $\dot{M}_\eta = 0$ ,  $C_\eta(\nu, \eta)$  is skew symmetric and  $D(\nu, \eta) > 0$ , then:

$$\dot{V}(e, \dot{e}) = -\dot{e}^T [K_d(\cdot) + D_\eta - \alpha M_\eta] \dot{e} - \alpha e^T K'_p(\cdot) e \quad (45)$$

From (45) it is possible to observe that the term on the right hand side is negative because  $\alpha > 0$  and  $K'_p(\cdot) > 0$ . The first term  $K_d(\cdot) + D_\eta - \alpha M_\eta$  will



be positive if condition (44) is satisfied. Finally, we can conclude that  $\dot{V}$  is  
190 negative semidefinite and based on the LaSalle invariance principle it is possible  
to ensure asymptotic stability.

#### 4. Real-Time Experimental Results

To demonstrate the feasibility and efficiency of our proposed control solution,  
we applied the control algorithm to *Leonard* (Figure 3), an underwater vehicle  
195 developed at the LIRMM (CNRS/University of Montpellier, France). *Leonard*  
is a tethered underwater vehicle that measures  $75 \times 55 \times 45$  cm and weighs 28  
kg. The propulsion system of this vehicle consists of six thrusters to obtain a  
fully actuated system.

The underwater robot is controlled by a laptop computer, with CPU Intel  
200 Core i7-3520M 2.9 GHz, 8GB of RAM memory. The computer runs under  
Windows 7 operating system and the control software is developed using Visual  
C++ 2010. The computer receives the data from the robot's sensors (depth,  
IMU), computes the control laws and sends input signals to the propellers.  
These actuators are controlled by Syren 25 Motor Drivers. The main features  
205 of this vehicle are summarized in Table 1. It is worth noting that this vehicle  
has two operation modes, we can use it as a ROV for sea exploration missions  
or we can program tasks to be performed autonomously. In our paper, we focus  
in the latter case. All the trajectory tracking tests were performed as an AUV.  
The control algorithm was experimentally tested in the  $4 \times 4 \times 1.2$  m pool of the  
210 LIRMM. Although, the proposed control law given by (24) is designed for the  
whole system of six degrees of freedom, the real-time experiments conducted  
in this work concern only depth and yaw. The main objective of the designed  
control law is to robustly track a desired reference trajectory in depth and yaw  
in presence of parameter uncertainties and/or external disturbances. Real-time  
215 experiments can be seen at <https://www.youtube.com/watch?v=lkiYr0v7H7c>.

Table 1: Main Features of the underwater vehicle

Mass	28 kg
Buoyancy	9 N
Dimensions	75 × 55 × 45 cm
Maximal depth	100 m
Thrusters	6 Seabotix BTD150
Power	48V - 600 W
Attitude Sensor	Sparkfun Arduimu V3 Invensense MPU-6000 MEMS 3-axis gyro and accelerometer 3-axis I2C magnetometer HMC-5883L Atmega328 microprocessor
Camera	Pacific Co. VPC-895A CCD1/3 PAL-25-fps
Depth sensor	Pressure Sensor MS5803-14BA
Sampling period	40 ms
Surface computer	Dell Latitude E6230- Intel Core i7 -2.9 GHz Windows 7 Professional 64 bits Microsoft Visual C++ 2010
Tether length	150 m

#### 4.1. Proposed Experimental Scenarios

To test the robustness of the proposed control scheme, four different scenarios have been performed, namely:

- (i) Scenario 1: Nominal case.

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In this scenario the underwater vehicle follows a predefined desired trajectory in depth and yaw in the absence of external disturbances. During this test, the controller's feedback gains are adjusted to obtain the best tracking. These gains remain unchanged during the rest of the experiments.

Table 2: Control gains used in real-time experiments

Depth	$b_{p3} = 20$	$d_{p3} = 0.05$	$u_{p3} = 0.1$
	$b_{i3} = 15$	$d_{i3} = 0.25$	$u_{i3} = 0.2$
	$b_{d3} = 13$	$d_{d3} = 0.25$	$u_{d3} = 0.2$
Yaw	$b_{p6} = 4.5$	$d_{p6} = 0.015$	$u_{p6} = 0.2$
	$b_{i6} = 1$	$d_{i6} = 0.015$	$u_{i6} = 0.2$
	$b_{d6} = 0.2$	$d_{d6} = 0.15$	$u_{d6} = 0.2$

225 (ii) Scenario 2: Robustness towards parametric uncertainties

In this test the buoyancy and damping of the vehicle are modified to test the effectiveness of the controller and its robustness towards parametric uncertainties.

(iii) Scenario 3: External disturbances rejection.

230 This test is inspired by a more realistic scenario, where the vehicle has the task of loading an object and when it reaches a certain depth, it drops that object. In this test we can observe a sudden change in the vehicle's weight and we can see how it affects the **controller's** performance.

(iv) Scenario 4: Comparison with other controllers.

235 In this **test**, the performance of the NLPID controller is compared with the classical PD controller and the NLPD control in parametric robustness tests.

#### 4.2. Tuning the nonlinear PID controller

240 The gains of the proposed controller have been tuned heuristically and following sequentially the steps below:

- $d_{pj}$  is chosen, taking into account that the interval  $[-d_{pj}, d_{pj}]$  is the linear region of the proposed controller.
- Considering  $b_{dj} = b_{ij} = 0$  and  $\mu_{pj} = 0$ ;  $b_{pj}$  is increased until the closed-loop system oscillates.

- 245 •  $d_{ij}$  is chosen equal or bigger than  $d_{pj}$  , and  $\mu_{ij} = 0$  .
- Then  $b_{ij}$  is increased until the system oscillations decrease.
- $d_{dj}$  is chosen bigger than  $d_{pj}$  , and  $\mu_{dj} = 0$  .
- $b_{dj}$  is increased until the system oscillations decrease.
- $\mu_{pj}$ ,  $\mu_{dj}$  and  $\mu_{ij}$  are adjusted to improve the system behavior, considering
- 250  $\mu_{pj} \leq \mu_{dj}$  and  $\mu_{pj} \leq \mu_{ij}$  .

Finally, the control gains used through **out** the whole set of real-time experiments are summarized in Table 2.

#### 4.3. Scenario 1: Control in nominal conditions

The upper plot of Figure 5 shows the depth and yaw controller performance  
 255 of the robot during the first **scenario**. In this experiment, the vehicle follows a predefined trajectory in depth going from the surface to a maximal depth of 30 cm, where the vehicle remains stable in that position for 20 seconds and finally emerges to 20 cm and hovers until the trial ends. For the yaw motion, the vehicle turns from its initial position **of** 60 degrees in 6 seconds. Then, it  
 260 remains stable in that position for 20 seconds. Finally, the robot goes to -60 degrees and **stays** there until the test ends. It can be **observed** that the controller **has** a short lapse of time to converge to the reference trajectory with a slight tracking error, as seen in the error plot **in** the middle of Figure 5. This can be confirmed through numerical data **from** the Root Mean Square Error (RMSE),  
 265 which is **shown** in Table 3. It is worth **noting** that oscillations (of an amplitude smaller than 1 cm) that are perceived in the depth trajectory tracking, could be a consequence of the depth sensor's accuracy. Finally, the evolution of the control inputs is displayed at the bottom of Figure 5.

#### 4.4. Scenario 2: Robustness towards parameter's uncertainties

270 In order to evaluate the robustness of the proposed controller against parametric uncertainties, we changed the buoyancy of the vehicle by attaching buoys

on both sides of the vehicle, thus increasing the floatability by 200%. To modify the damping of the submarine, we attached a large rigid plastic sheet ( $45 \times 10$  cm) on one side of the submarine, thus increasing the rotational damping along  
275 z-axis by approximately 90% (see illustration in Figure 3).

The tracking trajectory for depth and yaw motion is shown on the top of Figure 6. The NLPID takes a short lapse of time to converge to the reference depth trajectory, it is due to the fact that the vehicle needs more energy to overcome the added buoyant force. Despite the big persistent disturbance, the  
280 controller is able to maintain a performance as good as in the nominal case. However, the yaw tracking trajectory is reduced when the vehicle turns, but maintains a good steady-state performance. The RMSE for both scenarios is given in Table 3, it can be noted that the values are very close to the ones observed in the nominal case. The tracking errors are shown in the middle of  
285 Figure 6. In this figure, we can see the impact of the disturbances, the error increases when the vehicle submerges, emerges or turns. Finally, in the bottom of Figure 6, we can examine the evolution of the control inputs versus time. For example, for depth following, we can observe that the force increases almost twice as much when compared to the nominal case. This suggests that there is  
290 a strong compromise between the controller's ability to reject disturbances and the increase in energy that is demanded from the actuators.

#### 4.5. Scenario 3: Robustness towards external disturbances

In some applications, underwater vehicles are equipped with robotic manipulators which allow them to carry or manipulate objects and take them to a  
295 specific location or pick them up from the ocean floor to transport them to the surface. This scenario is inspired by this practical case. To simulate this the robot carries a load, a metallic block of 1 kg has been attached to the submarine with a 20 cm-long length of rope. In this scenario, the maximal depth of the reference trajectory has been set to 40 cm. As the maximum depth of the pool  
300 is 50 cm, the robot will be suddenly disturbed when it will reach 30 centimeters, because the metallic block will touch the floor, thus suddenly canceling its

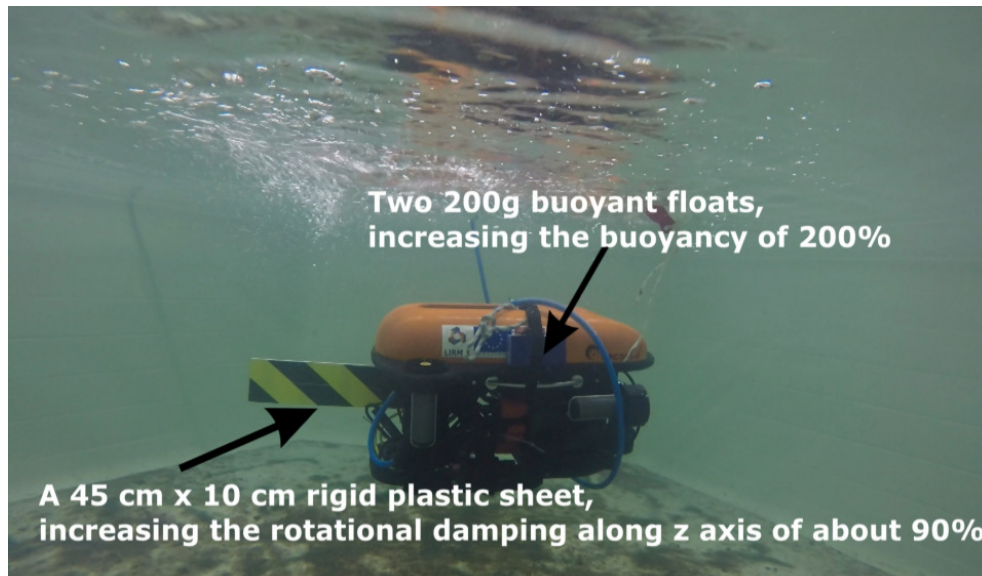


Figure 3: *Leonard* underwater vehicle with the **two additional** buoyant floats and a rigid plastic sheet, which increase the buoyancy and the damping along **the** z axis

weight. The disturbance will remain until the robot will **move** up and reach 30 cm, where the extra weight will act again (Figure 4). This simulates both the sudden release and the recovery of a load by the robot.

305 The obtained results for this scenario are depicted in Figure 7. At the top of the graph, we can see the influence of the extra weight because it changes the initial position of the submarine to 30 cm deep. When the test begins, the robot converges to the desired trajectory in about 5 seconds. Two seconds later, the weight of the vehicle suddenly changes and the NLPID control compensates

310 the **effects** of the disturbance some seconds later thanks to the integral term of the controller. When the vehicle **moves** up, the extra weight acts again on the submarine and **reduces** the trajectory tracking. Again, the NLPID controller compensates **this** disturbance as **we** can **observe** at the end of the graph. The error plots are displayed **in** the middle of Figure 7, while the numerical value of

315 the RMSE is given in Table 3. The evolution of the control input is displayed at the bottom of Figure 7.

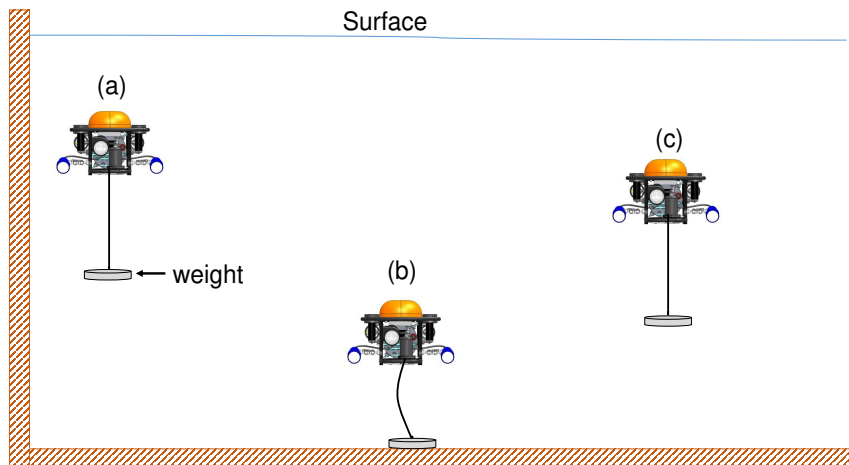


Figure 4: Description of controller robustness towards external disturbances test. A plate weighing 1 kg is attached to the robot as shown in (a). When the robot reaches 30 cm, the influence of the weight disappears (b). Finally, when the robot moves towards the surface, the influence of the weight acts on the robot again (c).

Table 3: Root Mean Square Error for NLPID controller for trajectory tracking .

Case	$RMSE_z(m)$	$RMSE_\psi(deg)$
Nominal	0.0009	0.0265
Parametric uncertainties	0.0017	0.4269
External disturbances	0.0030	0.0605

#### 4.6. Scenario 4: Comparison to other controllers

To highlight the improvements of our proposed NLPID controller over standard methods, the NLPID is compared to the well-known PD with buoyancy compensation and also with the NLPD algorithm proposed in [15]. The PD controller was chosen because it is a popular, simple and efficient algorithm to control the position and attitude of these kind of vehicles. The NLPD proposed in [15] is chosen for comparison because of its demonstrated robustness and fast convergence.

Firstly, we test the robustness of the whole set of controllers under parametric uncertainties. Then, we repeat the experiment described in section 4.3, introducing persistent disturbances in depth and yaw dynamics. The comparison between both controllers is displayed in Figure 8.

The trajectory tracking of depth and yaw is shown in the upper part of Figure 8. From tracking in depth, we can observe that the PD controller is not robust enough to compensate the effect of the disturbance. The NLPD shows improved behavior under perturbations than the PD, but its performance is insufficient to achieve good tracking when compared with the NLPID which succeeded in compensating for this disturbance. However, the yaw tracking test shows that all controllers are able to manage the introduced damping parametric disturbance.

In the middle of Figure 8, the plot of errors are depicted and the improvement of each controller is visually obvious and can be confirmed numerically through the RMSE in Table 4. Finally, the control inputs are displayed at the bottom of Figure 8. It is worth noting that at the beginning of the test, the NLPID



demands more energy than the other controllers, but this energy **reduces quickly** as the NLPID reaches the reference trajectory.

Table 4: Root Mean Square Error comparison for PD, NLPD and NLPID controllers.

Controller	$RMSE_z(m)$	$RMSE_\psi(deg)$
PD	0.0789	0.5500
NLPD	0.0374	0.3371
NLPID	0.0017	0.4269

## 5. Conclusion

In this paper, a decoupled nonlinear PID (NLPID) control has been developed for trajectory tracking control of an underwater vehicle. The NLPID controller has been improved through the introduction of a whole **range** of nonlinear functions to replace the constant feedback gains. Then, a Lyapunov design has been proposed to prove the stability of the closed-loop system. The main advantages of the proposed control law are: 1) it improves robustness with respect to classical PID controllers by introducing varying nonlinear gains that are adapted as functions of the tracking error, 2) it improves NLPD saturated control laws as it eliminates the undesirable gap when regulating the depth of the vehicle for **example**. The proposed controller has been implemented for trajectory tracking in depth and yaw motions on the *Leonard* underwater vehicle. The obtained real-time experimental results demonstrate the effectiveness and robustness of **our** proposed controller towards external disturbances and persistent parametric uncertainties. Finally, the proposed controller was compared to **a** nonlinear PD control. Based on the real-time experimental results, the NLPID shows better tracking performance and better robustness than the NLPD control proposed in our previous work. **For** future work, the NLPID will be compared with more advanced controllers, such as Active Disturbance Rejection Controllers (ADCR), for **example**.

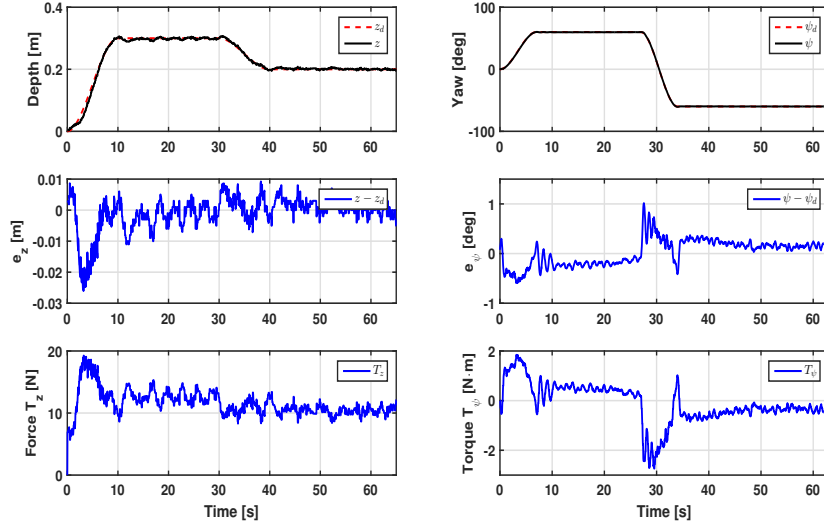


Figure 5: Performance of the NLPID controller nominal design. (Upper) Trajectory tracking in depth and yaw in absence of disturbances. (Middle) Plots of the error signal. (Lower) Evolution of the control inputs.

## Acknowledgment

This work was supported by Conacyt, grant 490978. The *Leonard* underwater vehicle has been financed by the European Union (FEDER grant n° 49793) and the Region Occitanie (ARPE Pilot Plus project). The authors would like to express their gratitude to the anonymous reviewers for their comments for the improvement of the manuscript.

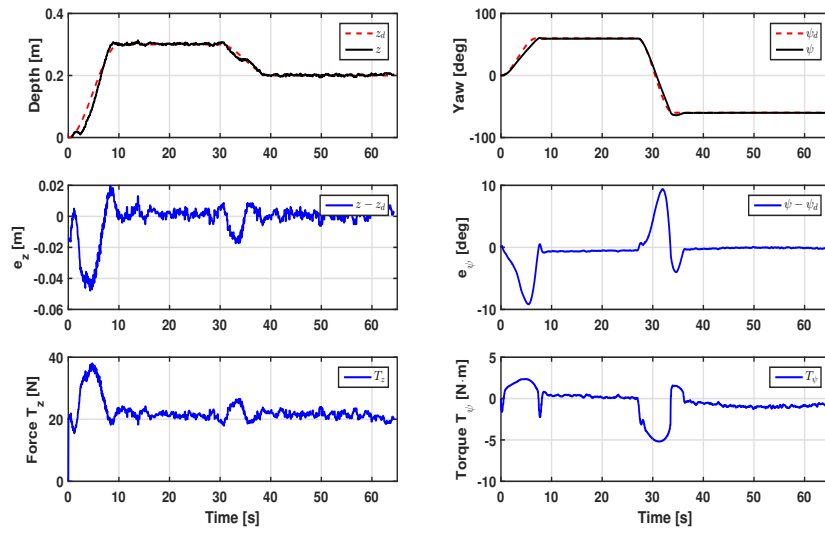


Figure 6: Robustness NLPID controller performance towards parametric uncertainties. The floatability of the submarine was increased by 200% while the damping along the z-axis was modified by up to 90% when compared to the nominal case.

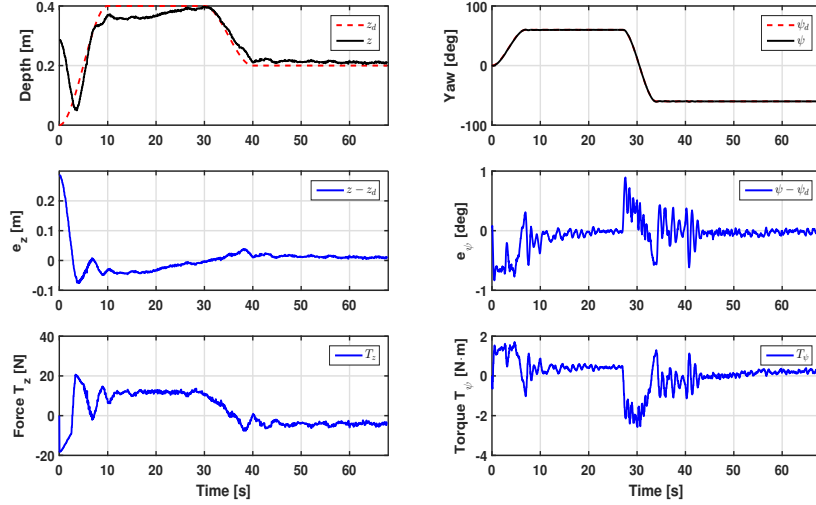


Figure 7: NLPID controller performance under external disturbance test. A 1 kg weight is attached to the robot and when the vehicle reaches a depth of 30 cm the influence of the weight disappears. Finally, when the robot moves towards the surface, the action of the weight disturbs the robots dynamics again.

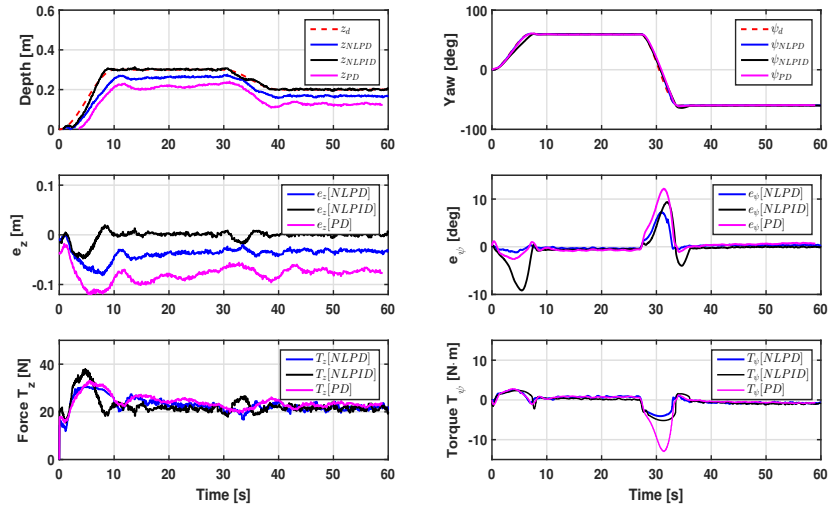


Figure 8: NLPID, NLPD and PD controller performance comparison towards parametric uncertainties. The floatability of the submarine was increased by 200% while the damping along the z-axis was modified by up to 90% when compared to the nominal case.

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