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Efficient Incremental Computation of Aggregations over Sliding Windows

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ABSTRACT
Computing aggregation over sliding windows, i.e., finite subsets of an unbounded stream, is a core operation in streaming analytics. We propose PBA (Parallel Boundary Aggregator), a novel parallel algorithm that groups continuous slices of streaming values into chunks and exploits two buffers, cumulative slice aggregations and left cumulative slice aggregations, to compute sliding window aggregations efficiently. PBA runs in $O(1)$ time, performing at most 3 merging operations per slide while consuming $O(n)$ space for windows with $n$ partial aggregations. Our empirical experiments demonstrate that PBA can improve throughput up to 4x while reducing latency, compared to state-of-the-art algorithms.

CCS CONCEPTS
• Information systems → Data streaming.

KEYWORDS
Data Stream; Streaming Algorithm; Sliding Window Aggregation

ACM Reference Format:

1 INTRODUCTION
Nowadays, we are witnessing the production of large volumes of continuous or real-time data in many application domains like traffic monitoring, medical monitoring, social networks, weather forecasting, network monitoring, etc. For example, every day around one trillion messages are processed through Uber data analytics infrastructure\(^1\) while more than 500 million tweets are posted on Twitter [11]. Efficient streaming algorithms are needed for analyzing data streams in such applications. In particular, aggregations [23], having the inherent property of summarizing information from data, constitute a fundamental operator to compute real-time statistics in this context. In the streaming setting, aggregations are typically computed over finite subsets of a stream, called windows. In particular, Sliding-Window Aggregation (SWAG) [20, 21, 26, 28] continuously computes a summary of the most recent data items in a given range $r$ (aka window size) and using a given slide $s$. If the range and slide parameters are given in time units (e.g., seconds), then the sliding window is time-based, otherwise, i.e., if these parameters are given as the number of values, it is count-based. Fig. 1 presents an example of computing sum over the count-based sliding window with a range of 10 values and a slide of 2 values.

Stream processing systems (SPSs) [2, 6, 19, 30, 32] are ubiquitous for analyzing continuously unbounded data. However, one of the challenges faced by SPSs is to efficiently compute aggregations over sliding windows. This requires the ability of such systems to incrementally aggregate moving data, i.e., inserting new data items and evicting old data items when a window is sliding without re-computing the aggregation from scratch. High throughput and low latency are essential requirements as SPSs are typically designed for real-time applications [13].

Two orthogonal techniques have been proposed to meet such requirements: slicing (aka partial aggregation) [7, 18, 20, 31], and merging (aka incremental final aggregation) [25–28]. Slicing techniques focus on slicing the windows into smaller subsets, called slices, and then computing partial aggregation over slices, called slice aggregations. The benefit of the slicing technique is that slice aggregations (i.e., partial aggregations over slices) can be shared by different window instances. For example, in Fig. 1, a slice aggregation over a slice of 2 values can be shared by 5 windows. On the basis of a slicing technique, final aggregations over sliding windows are computed by merging slice aggregations, e.g., in Fig. 1, SWAGs are computed by merging 5 slice aggregations. During the merging phase, each insertion or eviction is processed over a slice aggregation rather than a value. In modern SPSs, practical sliding windows can be very large [28], thereby making the merging phase non-trivial. To efficiently merge slice aggregation, incremental computation is necessary because an approach that recalculate slice aggregations from scratch (hereafter called Recal) is very inefficient [20, 21, 26, 28].

The difficulty of incremental merging depends on the considered class of aggregations: invertible or non-invertible. An aggregation is invertible if the merging function for its partial aggregations has an inverse function. For example, sum is clearly invertible, because it has the arithmetical subtraction as the inverse function. Similarly, avg and std are invertible because they use addition as merging function. Partial aggregations of invertible aggregations can be

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Figure 1: Example of computing sum over a count-based sliding window with a range of 10 values and a slide of 2 values.

Figure 2: Example of merging slice aggregations for computing SWAGs.
An aggregation is invertible if its combine function is invertible. Let \( x, y \) be any values from the domain of a combine function \( \oplus \). Then \( \oplus \) is invertible if there exists an operation \( \ominus \), such that \( x \oplus y \ominus y = x \), e.g., the combine function of geometric mean is invertible as its inverse function is a pair of division and subtraction.

Aggregations can also be classified in distributive, algebraic and holistic [10]. Distributive aggregations, e.g., sum and max, have an identical constant size for both partial and final aggregation. Algebraic aggregations have a bounded size for partial aggregation, e.g., average and geometric mean. The other aggregations are holistic, which have an unbounded size for partial aggregations, e.g., median and percentile. In this paper, we consider non-invertible aggregations that are distributive or algebraic. Note that, such consideration is consistent with state-of-the-art works [25–27].

3 STATE OF THE ART

This section reviews state-of-the-art algorithms devoted to merging slice aggregations, and discusses slicing techniques and parallelization in SPSS. A more broad vision on SWAG can be found in [13] while existing surveys review various facets of SPSSs [8, 12, 14].

3.1 Incremental Merging of Slice Aggregations

To merge slice aggregations for non-invertible aggregations, efficient algorithms are needed. The performance of such algorithms can impact the overall aggregation time, because latency caused by computing SWAG has the nature of propagation towards computations over the following ones. To our best knowledge, TwoStack [27], DABA [27], FlatFIT [25], SlickDeque (Non-Inv) [26] and SlideSide (Non-Inv) [29] are the most efficient state-of-the-art algorithms for computing non-invertible aggregations over FIFO windows. Consider each instance of a sliding window that requires merging \( n \) slice (partial) aggregations. In Table 1, we present the algorithmic complexities of the state-of-the-art algorithms computed originally in [26, 29], and also our algorithm PBA (see Section 4.4 for explanation). TwoStack pushes pairs of a partial aggregation and a streaming value into a back stack and pops such pairs from a front stack. Computing an aggregation over a sliding window instance only needs to peek and merge partial aggregations from the front and back stack. However, when the front stack is empty, TwoStack flips all items in the back stack onto the front stack requiring \( O(n) \) time. DABA [27] leverages TwoStack to gradually perform the flipping operation of TwoStack which amortizes its time to \( O(1) \). As a consequence, DABA is in \( O(1) \) worst-case time. FlatFIT [25] only recalculates window aggregation one time per \( n + 1 \) slides. Intermediate aggregation results are maintained in an appropriate index structure and reused to avoid redundant computations. Hence, on average, each of \( n + 1 \) slides can be computed by 3 merging steps. SlickDeque (Non-Inv) uses a deque to store streaming values, and not every streaming value will be added into the deque. For example, when computing \( \max \) over sliding windows, SlickDeque continuously replaces the end of a deque \( v' \) using a new value \( v \) if \( v > v' \). Adding a value \( v \) will depend on the rank of \( v \) w.r.t the number of values in the deque which could be \( n \). The worst time complexity of SlickDeque is \( O(n) \) while its amortized time is less than 2 because a new value will never be compared more than twice. SlideSide (Non-Inv) uses two stacks to store partial aggregations, like TwoStack, but shares values between them. While, an operation similar to the flipping in TwoStack is still required, resulting in \( O(n) \) worst-case time.

As shown in Table 1, which contains complexity analysis of PBA described in Section 4.4, PBA is the best for time and space complexity, except the comparison with SlickDeque in amortized time. However, unlike SlickDeque, PBA runs in constant time, which is also experimentally demonstrated in Section 5.1.1. Such a feature of PBA guarantees its performance in the worst case. Note that amortized and worst-case time determine throughput and latency, respectively.

In addition to its low time and space complexities, one of the main advantages of PBA compared to the state-of-the-art algorithms, e.g., TwoStack [27], DABA [27], FlatFIT [25], SlickDeque (Non-Inv) [26] and SlideSide (Non-Inv) [29], is that the latter algorithms cannot use additional threads to get performance gains, i.e., computing intermediate results in parallel. For instance, in TwoStack, the two stacks are interdependent. In SlickDeque, the deque needs to be traversed in the worst case. However, the lcs and csa buffers used for computing SWAGs in PBA are completely independent of each other, allowing their incremental computation to be done in parallel.

3.2 Combining Slicing and Merging

Various slicing techniques have been proposed in the literature, among which we could mention Pairs [20], Pairs [18], Cutty [7], and Scootty [31]. The main goal is to determine sizes of intervals over the stream called slices which are then used to split each window into several slices in order to allow sharing the aggregations computed over slices. Slicing techniques can improve throughput by amortizing the total time of merging evenly over each stream value in each slice. However, having only a slicing technique cannot reduce latency caused by merging slice aggregations, which is especially important for a continuous stream-processing model.

A merging technique on top of a slicing one can deal with the latency issues, and additionally improves the throughput. First of all, latency can be reduced, as demonstrated in Cutty and Scooty through combining their slicing techniques with the FlatFIT [28] merging algorithm. Eager slicing of Scooty (using FlatFIT for merging) shows up to two orders of magnitudes reduction of latency, compared to lazy slicing (with Recal as the merging algorithm). In addition, an advanced merging algorithm can also improve throughput. Specifically, [27] shows that TwoStack outperforms Recal, except in the case of very small window sizes, and TwoStack is always faster, up to \( 6x \), than FlatFIT. In this paper, we adopt the Cutty slicing technique and design a constant-time merging algorithm to

Table 1: Algorithmic Complexities (Non-Invertible SWAG).

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Time (amortized)</th>
<th>Time (worst)</th>
<th>Space</th>
</tr>
</thead>
<tbody>
<tr>
<td>TwoStack</td>
<td>3</td>
<td>( n )</td>
<td>2( n )</td>
</tr>
<tr>
<td>DABA</td>
<td>5</td>
<td>8</td>
<td>2( n )</td>
</tr>
<tr>
<td>FlatFIT</td>
<td>3</td>
<td>( n )</td>
<td>2( n )</td>
</tr>
<tr>
<td>SlickDeque</td>
<td>(&lt; 2)</td>
<td>( n )</td>
<td>2( n )</td>
</tr>
<tr>
<td>SlideSide</td>
<td>3</td>
<td>( n )</td>
<td>2( n )</td>
</tr>
<tr>
<td>PBA</td>
<td>(&lt; 3)</td>
<td>3</td>
<td>( 3( n )+13 )/2</td>
</tr>
</tbody>
</table>
reduce latency and improve throughput. It is worth noting that our merging approach remains independent from slicing techniques.

3.3 Parallelization in SPSs

Parallelization in SPSs is an active research area. A large piece of work in this field focuses on inter-operator parallelism with a clear dominance of key-based splitting techniques [24] in shared nothing cluster architecture. Regarding intra-operator parallelism, [22] presents parallel patterns to handle generic stateful operators (e.g., sorting, join, grouping, ...). PBA fits into the category of exploiting intra-operator parallelism to incrementally compute SWAGs.

Novel SPSs are designed to exploit multi-core processors to process streams in parallel [17, 34]. In this line of work, SABER [17] processes fixed-size batches in parallel using a hybrid architecture of CPUs and GPGPUs (i.e., modern GPUs), and merges local results of batches to produce the final result. The parallelism of SABER is suitable for the micro-batch model, giving the opportunity to process each micro batch by separate tasks (one task for each batch [17]). PBA is designed for the continuous processing model. In addition, PBA merges at most 3 sub-aggregations to produce the final aggregation for arbitrary cases, i.e., requiring only constant time for merging, which is achieved by using the optimal chunk size computed based on the range and slide parameters in a continuous aggregate query.

Modern distributed SPSs [2–4, 19, 30, 32] compute SWAGs over a stream of key-value pairs in parallel. For example, in Apache Flink [3, 6], one can transform a DataStream into a KeyedStream with disjoint partitions, where a key will be assigned to a specific partition. SWAGs over different partitions can be computed in parallel using multiple cores of nodes in a cluster. The parallel computation in PBA is orthogonal to such distributed SPSs, since PBA computes SWAGs over values with the same key in parallel, which makes PBA suitable to extend partition-oriented parallelism in distributed SPSs.

4 Parallel Boundary Aggregator

In PBA, a stream is considered as a sequence of chunks having an identical number of slices. Non-invertible aggregations over window instances are computed by merging two buffers of cumulative aggregations over slice aggregations in chunks. To efficiently compute SWAG, buffers are computed in parallel using two threads. As SPSs are usually running on modern CPUs [33], in PBA we assume that the system is equipped with at least two cores allowing to run two tasks in parallel.

4.1 Main Ideas

Let us consider a query with the non-invertible aggregation \( \max \) over a range of 10 values and a slide of 2 values, i.e., \( W[10, 2] \). Slices of 2 values can be created, and thus each window instance needs to merge 5 slice aggregations. In general, the final aggregation needs to merge \( [r/s] \) slice aggregations for each instance of \( W[r,s] \).

PBA is an \( O(1) \) time solution for \( W[r,s] \), which is achieved by maintaining two buffers: \( csa \) (cumulative slice aggregations) and \( lcs \) (left cumulative slice aggregations). Generally, a \( csa \) buffer is computed through accumulating slice aggregations from left to right inside a \( chunk \) (an array of slices), and a \( lcs \) buffer from right to

![Figure 2: Example of computing the count-based \( W[10, 2] \) with the aggregation \( \max \) over a stream using PBA with a chunk size of 5 slices.](image-url)
accumulating streaming values inside each slice to have a final aggregation, and the other for processing the task of computing SWAGs. Thus, PBA can keep receiving new streaming values after the end of \( w_1 \), i.e., whether PBA needs to wait for the result of \( lcs_0 \) to compute \( \max(w_1) \). Such an issue is dealt with in Section 4.3, where we identify the optimal chunk size minimizing the waiting time.

### 4.2 PBA Model

In PBA, a stream is considered as a sequence of non-overlapping chunks of slices. Each chunk has an identical number of slices and starts at a specific time denoted as boundary:

- \( b_1 \) (boundary): the start of the chunks, e.g., \( b_1 \) in Fig. 2;
- \( c_1 \) (chunk size): a sequence of slices from \( b_1 \) to \( b_1 + c_0 \), e.g., \( c_0 \) in Fig. 2;
- \( b \) (chunk size): the number of slices in a chunk, e.g., 5 in Fig. 2.

We incrementally compute partial aggregations for every chunk and the other for processing the task of computing SWAGs. To compute \( lcs \), PBA adopts a two-level incremental computation inside each chunk:

1. (i) accumulating streaming values inside each slice to have a slice aggregation, and (ii) accumulating slice aggregations inside each chunk to have a chunk aggregation. To compute \( lcs \), PBA maintains intermediate results during accumulating slice aggregations from right to left in a slice aggregation array \( \text{sa}_i \).

**Dividing SWAG into Sub-Aggregations:** As the window instances, whose starts coincide with boundaries in every chunk, are trivial cases requiring only \( csa \) elements, e.g., \( w_0 \) in Fig. 2, we focus on the other cases in the sequel. To illustrate the PBA model, we first define \( k = \lceil \frac{\mu(s)}{\mu(u)} \rceil \), which denotes the number of chunks a window instance can fully cover, e.g., \( k = \lceil \frac{10}{2} \rceil = 1 \) in Fig. 2. In the PBA model, we use boundaries to divide a window instance \( W[r,s] \) into several sub-parts and merge partial aggregations of sub-parts to have a final aggregation of \( w \). The number of sub-parts can be \( k + 1 \) or \( k + 2 \), depending on \( W[r,s] \) and the used chunk size. We denote a partial aggregation of each sub-part as a sub-aggregation, and all sub-aggregations of \( w \) as \( (\text{sa}_0,\text{sa}_1,\ldots) \), i.e., \( \text{sa}_0 \) is the first one (see Fig. 3 for an example). Then the first sub-aggregation is an element in \( lcs \), and the last one in \( csa \). Each of the others is a chunk aggregation, i.e., the last element in a \( csa \) buffer. An example of \( k = 1 \) is shown in Fig. 2, where each window instance is divided into 2 sub-parts and SWAGs are computed by merging 2 sub-aggregations. To illustrate the case of \( k > 1 \), Fig. 3 presents the example of computing a count-based \( W[16,1] \) with a chunk size of 4, where we have \( k = 4 \) and each window instance is divided into 5 sub-parts, e.g., \( \max(w_1) = \max(lcs_0[1],c_0,c_1,c_2,c_3) \).

**Efficient Computation of \( lcs \):** In the final aggregation stage, since \( lcs \) and \( csa \) buffers used for merging are computed over completely independent \( \text{sa}_i \) arrays, we compute \( lcs \) and \( csa \) buffers in parallel, i.e., two tasks run simultaneously and each task focus on computing a single buffer. Specifically, we maintain two threads in PBA. The main thread is used to compute \( csa \) and the final aggregation, and the other for processing the task of computing \( lcs \).

![Figure 3: Example of using a chunk size of 4 to compute \( \max \) a count-based \( W[16,1] \), which leads to \( k = \lceil \frac{16}{1} \rceil = 4 \) and the window instance \( w_1 \) is divided into 5 sub-parts.](image)

### 4.3 Optimal Chunk Size in PBA

The chunk size is crucial for PBA. Specifically, a carelessly selected chunk size can cause delay to compute final aggregations. For instance, consider the example in Fig. 2, and let \( T_u \) be the time required to execute \( \oplus \), i.e., a merging function or a combine function. Although the two tasks for computing \( lcs_0 \) and \( csa_1 \) are simultaneously started at the boundary \( b_1 \), \( lcs_0[1] \) cannot be obtained earlier than \( csa_1[0] \) because computing \( lcs_0[1] \) (3 \( T_u \)) requires two more \( T_u \) than computing \( csa_1[0] \) (1 \( T_u \)). Thus, PBA needs to wait for 2 \( T_u \) to use \( lcs_0[1] \) and \( csa_1[0] \) to compute \( \max(w_1) \).

The following two theorems identify the optimal chunk size, denoted as \( b^* \), for count-based windows and time-based window, respectively. The corresponding proofs are provided in our technical report, which is available online [1].

**Theorem 1.** Given a count-based sliding window window \( W[r,s] \), the optimal chunk size \( b^* \) in PBA can be obtained as follows:

- if \( r/s \leq s + (r \mod s) + 1 \), then \( b^* = r/s \);
- otherwise \( b^* = \lceil \frac{(r/(s + 1)) + r \mod s + 1}{b + 1} \rceil \).

With \( b^* \), we have \( k = \lceil \frac{r/s}{b^*} \rceil = 1 \).

**Theorem 2.** Given a time-based sliding window window \( W[r,s] \), the optimal chunk size \( b^* \) in PBA can be obtained as follows:

- if \( r/s \leq \frac{r + s + 2T_u + C}{s + 2T_u} \), then \( b^* = r/s \);
- otherwise \( b^* = \lceil \frac{r/s + s + 2T_u + C}{s + 2T_u} \rceil \).

where \( C = 0 \) if \( r \mod s = 0 \), otherwise \( C = s(r \mod s + 1) + T_u \). With \( b^* \), we have \( k = \lceil \frac{s}{b^*} \rceil = 1 \).

The optimal chunk size ensures that (i) each \( lcs \) buffer can be obtained without waiting, and (ii) \( k = 1 \) which leads to the minimum number of merging operations to compute final aggregations.

### 4.4 Complexity Analysis

As previous works [25–27, 29] present complexities by computing a count-based \( W[n,1] \) with a range of \( n \) and a slice of 1, i.e., merging
n slice aggregations for each window instance, we also rest on such a scenario to discuss complexities of PBA.

Given a sliding window \( W[n, t] \), as PBA is used with the optimal chunk size \( b^* \), we have \( b^* = \left\lfloor \frac{n}{k+1} \right\rfloor \) and \( k = \left\lfloor \frac{1/s}{b} \right\rfloor = 1 \) according to Theorem 1. Thus, a window instance will be divided into either \( k + 1 = 2 \) or \( k + 2 = 3 \) sub-parts, i.e., spanning 2 or 3 chunks. Based on this, we discuss the time and space complexity of PBA below.

Time Complexity: In the final aggregation stage, merging 2 or 3 sub-aggregations of sub-parts needs 1 or 2 merging operations. Considering that the last streaming value of a window will be merged with \( cs_a \), the total number of merging operations by PBA is 2 or 3. Therefore, the worst-case time is 3, and the amortized time is less than 3.

Space Complexity: As a window instance can span at most 3 chunks, \( l \) o.g, we denote the three chunks as \( c_{i-2}, c_{i-1}, c_i \), and consider the current streaming value is arriving at a slice of \( c_i \). Thus, 3 \( sa_a \) arrays of size \( b^* \) are needed. Note that the \( lcs \) arrays of the three chunks will be computed over \( sa_a \) arrays and do not require extra space. In addition, PBA only needs the \( ca_{i-1} \) array of the current chunk \( c_i \), i.e., \( cs_{ai} \), and maintains one element in \( cs_{ai} \), the current one, rather than the entire \( cs_{ai} \) array. For windows spanning 3 chunks, the chunk aggregation \( cs_{ai-1} \) of chunk \( c_{i-1} \) is also needed. Thus, the total space required by PBA is: \( 3b^* + 2 = 3\left\lfloor \frac{n}{k+2} \right\rfloor + 2 \leq \frac{3n+13}{2} \).

5 EXPERIMENTAL EVALUATION

In this section, we evaluate the performance of PBA against the state-of-the-art algorithms for computing non-invertible aggregations over sliding windows with FIFO semantics. Moreover, we integrate PBA into Apache Flink and present the corresponding improvement in local and cluster modes, respectively.

5.1 PBA Compared to Alternatives

State-of-the-Art Algorithms: In our experimental evaluation we compare PBA to the two best state-of-the-art algorithms: SlickDeque [26] and TwoStack [27]. SlickDeque shows the best performance in terms of throughput and latency [26] while TwoStack is slightly worse than SlickDeque but behaves better than the others [26, 27, 29]. Note that, although DABA [27] has a constant time complexity in the worst case, it does not show a better performance result compared to SlickDeque in terms of throughput and latency [26], or TwoStack in terms of throughput [27]. We also consider the naïve algorithm and call it Recal (recalculate). As the sliding window moves, it calculates an aggregation from scratch. To study the performance of our algorithm in the case of single-core machines, we implemented a sequential version of PBA, denoted as SBA (sequential boundary aggregator), which uses only one thread to compute SWAG. SBA follows the same procedure as PBA, except that the task of computing \( lcs \) in SBA is done in the same thread as the one that computes \( ca_{ai} \) buffer (SBA uses only one thread). In order to slice a data stream, we set each slice size to be equal to the slide size (as described in Section 2.2 for details). Notice that this is the underlying slice solution for all algorithms tested in our evaluation. We implemented PBA and SBA using Java 8, and the state-of-the-art algorithms based on the pseudo-codes in [27] and [26]. The source codes of PBA, SBA, and the implementation of state-of-the-art algorithms are available online [1].

Datasets: We use two datasets, a real-world and a synthetic one, for throughput experiment. The real-world dataset is the DEBS12 Grand Challenge Manufacturing Equipment Dataset [15], which is also used by SlickDeque [26]. This dataset contains energy consumption recorded by sensors of manufacturing equipment with the frequency of 100 records per second, and each tuple is associated with a timestamp, which we will use in our time-based experiments. The original dataset contains 32 million tuples, which we made into 130 million tuples, i.e., 4 copies. The synthetic dataset contains 200 million values generated using the uniform distribution. Note that in our experiments we observed the same tendency for PBA with different datasets, this is why we have not used more than two test datasets. For the latency experiments, we used the synthetic dataset and tested latency results for 1 million window instances.

In our experiments, as aggregation function we use \( max \) commonly used in related works [25, 26, 28, 29] as the representative of non-invertible aggregations. We first evaluate throughput for count-based windows with a fixed slide while varying the ranges. Then we evaluate the case with a fixed range while varying the slides. Similarly, we evaluate the throughput for time-based windows in both settings (i.e., with a fixed slide and varying ranges, and then with a fixed range and varying slides). We test latency for both count-based and time-based windows. To further study the latency of different algorithms, we also test a more complex aggregation, MomentSketch = \((min, max, sum, count, \sum x_i, \ldots, \sum x_i^2, \sum log x_i, \ldots, \sum (log x_i)^2)\) [9] with \( l = 10 \), which can approximate percentiles.

Experiment Setup: We run the throughput and latency experiments at a server with Ubuntu 16.01.3 LTS, 6 virtual CPUs of Intel(R) Xeon(R) 2.40GHz, and 16GB main memory, where the heap size of JVM is configured to 4GB.

5.1.1 Throughput Experiments. The workload for evaluating \( max \) over count-based windows is as follows: 1) range from \( 2^2 \) to \( 2^{20} \) with the slide size set to one; 2) slide from 1 to 10 with a range of \( 2^{17} \). For the time-based windows the workload is as follows: 1) range from 6 to 60 minutes with a slide of 10 milliseconds; 2) slide from 10 milliseconds to 100 milliseconds with a range of 1 hour. We do not test for larger slide sizes as the overall throughput will be amortized by the time of computing slice aggregations, such that the differences between merging algorithms cannot be observed (see Section 3.2 for detailed discussion). We run the workload 20 times and report the median of all evaluation results. We stop reporting the throughput of the Recal algorithm when the corresponding throughput is too small. Our experimental results are presented in Fig. 4, Fig. 5, and Fig 6. We discuss the results in the sequel.

Count-based windows with a fixed slide. Our throughput results for this case are shown in Fig. 4. PBA shows the best throughput with large window sizes, and SBA (the sequential version of PBA) shows a higher throughput than TwoStack and SlickDeque, even for small window sizes. More precisely, the throughput of PBA increases w.r.t to the increase of window size \( r \) when \( r < 2^{15} \), and keeps consistent when \( r \geq 2^{15} \). When \( r \geq 2^{25} \), the throughput of PBA is \( 2.5 \times \) higher than that of TwoStack and \( 4 \times \) higher than that of SlickDeque. Note that, the throughput of PBA increases w.r.t to the
window size \( r \) when \( r < 2^{15} \), because a smaller window size will lead to a smaller optimal chunk size in PBA. Thus, the parallel task in PBA, i.e., computing \( fcs \), will consequently require less time but will be launched more frequently, compared to a case with a larger window size. In such a case, the constant overhead for launching a parallel task will be relatively more obvious. For example, when \( r = 2^{5} \), the optimal chunk size of PBA is 17. Then, the corresponding parallel computation for each chunk in PBA requires applying only 15 times of the \( \max \) operation over 2 elements, and this cost is much less than the cost of launching a parallel task. But, if \( r = 2^{20} \), the optimal chunk size is 5242884, which requires 5242882 times of \( \max \) over 2 elements. In the latter case, launching a parallel task can bring significant benefits.

**Count-based windows with various slide sizes.** Our throughput results for this case are shown in Fig. 5. We observe that, with a larger slide size, combining slicing with merging can improve throughput. PBA shows better throughput with a small slide shown in Fig. 5, because \( \text{range} \) is still large in such cases, which means there are still a large number of slice aggregations that need to be merged. Then, as the slide size is getting larger, the throughput of different algorithms are getting closer. There are mainly two reasons that explain such a behavior. The first reason comes from the fact that the ratio \( \frac{\text{range}}{\text{slide}} \) is smaller in these cases, which leads to less slice aggregations to be merged for each window instance. Thus, the required computations are not enough to exploit the full capacity of PBA. The second reason is that the overall difference between various algorithms will be amortized by the cost of computing partial aggregations over each slice (this is due to the large number of \( \oplus \) operations performed in each slice).

**Time-based windows with various range and slide sizes.** Our throughput results of this case are shown in Fig. 6. PBA shows the overall best throughput with large window sizes, and SBA (the sequential version of PBA) shows a higher throughput than TwoStack and SlickDeque. The corresponding reasons are identical to the case of count-based windows. Note that, in Fig. 6 (a), PBA outperforms the others because \( \text{range} \) is large even for the case of \( \text{range} = 6 \) minutes.

5.1.2 Latency Experiments. The workload consists in: (i) computing the aggregation \( \text{Max} \) over count-based windows with a slide of 1 and ranges of \( 2^{13} \) and \( 2^{14} \) respectively, and (ii) computing the aggregation \( \text{MS} \) (MomentSketch) over time-based windows with a slide of 1 second (containing around 100 streaming values) and ranges of 1 and 2 hours respectively. In this experiment, we compare TwoStack, SlickDeque, SBA and PBA. We capture the computation time in nanoseconds, corresponding to the time required by an algorithm to compute the aggregation over each window when the ends of windows are reached. We run the experiments for 1 million windows, and report the latency for the last 970 thousand ones.

Our latency results are presented in Fig. 7. In Table 2 and Table 3, we present 7 statistical summaries for the latency experiments, i.e., Min (minimum), Max (maximum), Avg (average), Std (standard deviation), LQ (lower quartile, i.e., 25% percentile), Med (median), HQ (higher quartile, i.e., 75% percentile). On the whole, we observe that both SlickDeque and PBA do not have latency spikes, and PBA performs better than SlickDeque. We discuss detailed results of all tested algorithms in the sequel.

As it can be observed, PBA has the overall best latency results in terms of all statistical summaries, especially for the Max and Std metrics shown in Table 2 and 3, which corresponds to the worst case

![Figure 4: Throughput for count-based windows by varying the window size and with a fixed slide size.](image)

![Figure 5: Throughput for count-based windows by varying the slide size and with a fixed range.](image)

![Figure 6: Throughput for time-based windows.](image)
time complexity of PBA shown in Table 1. Moreover, PBA shows better latency results with a larger window size, shown in Fig. 7, and Table 2 and 3 (the reason has been discussed in Section 5.1.1). SBA shows similar results as PBA except for Max and Std in Table 2 and 3. SBA computes a $lcs$ buffer at each boundary, which postpones the computation of a $csa$ buffer until the computation of $lcs$ has been completed. Therefore, SBA has a high latency periodically, e.g., in Fig. 2, at boundary $b_1$, SBA needs to firstly compute $lcs_0$, and then $csa_1$, and this incurs high latency for $w_1$. Such a high latency of SBA can be observed in Fig. 7. Note that, PBA does not have high latency due to computing $lcs$ and $csa$ in parallel.

SlickDeque has almost the same latency as TwoStack for Avg, but much better than TwoStack for Max and Std. As shown in Fig. 7, TwoStack has latency spikes periodically, and thus TwoStack does not perform well in terms of Max and Std. Such latency spikes become larger when the window size increases. TwoStack requires moving all elements of one stack to another one periodically, and the corresponding cost is linearly increasing w.r.t to the window size. This is why the periodical red spike of TwoStack for the case of 16384 is higher than the corresponding one for the case of 8192, and similar for time-based window with a range of 2 hours compared to the range of 1 hour.

We also observe that, as aggregation getting more complex, the latency is also getting higher, which can be observed in Table 2 and Table 3. As an aggregation defined in the LCL framework can have an arbitrarily complex $\oplus$ operation, the difference in the latency caused by using a different merging algorithm can be more obvious.

### 5.2 Apache Flink Integration

We integrate PBA into Apache Flink [3, 6], denoted as FPBA. PBA is integrated into Flink through KeyedProcessFunction, i.e., a low-level operator in Flink. To support parallel tasks of PBA, a thread pool for each task slot in Flink is launched, which will be used to compute the $lcs$ buffers for all key-value pairs associated with the corresponding task slot. Our goal in this subsection is to show that PBA can be easily integrated into modern distributed and parallel SPSSs, and to evaluate FPBA in both local and cluster modes. In this experiment, we consider 2$^{10}$ as the representative of large windows. We compute max over count-based sliding windows with a slide of 1 and a window size of 2$^{10}$, and capture the throughput of Flink and FPBA by using a different degree of parallelism in local mode, and a different number of nodes in cluster mode.

**Datasets:** We use the DEBS14 Grand Challenge Smart Home Dataset [16], which contains recordings from smart plugs in private households. Each tuple of this dataset includes a power consumption and a plugin ID. The first 10 million tuples contain 14 plugin IDs with a slight data skew, which we made into different sizes with the identical distribution in our experiments, i.e., 60 million tuples with 84 plugin IDs for local execution, and 240 million tuples with 336 plugin IDs for cluster execution.

**Experiment Setup:** We run the cluster experiment at a Flink cluster having 1 master node and 6 worker nodes running Ubuntu server 16.01.3 LTS. The master node has 6 virtual CPU cores of Intel XEON 3GHz, and 16GB main memory, and the job manager of Flink is configured with 6GB of memory. Every worker node has 4 virtual CPU cores of Intel XEON 3GHz, and 8GB main memory.
and the task manager of Flink is configured with 6GB of memory. We run the local experiment only at the master node of the Flink cluster. We run both local and cluster experiments 10 times, where we consider the first 3 runs as warm-ups, and we repeat the whole execution 3 times. We report the median throughput for Flink and FPBA. We use Flink 1.10.0 and Java 8 in this experiment.

We present the results in Fig. 8. In Fig. 8 (a), we observe the throughput of FPBA or Flink linearly increases up to 3 parallel instances (called parallelism in Flink). Each parallel instance of the execution pipeline of Flink, or FPBA, contains 2 tasks, i.e., reading data and computing SWAG. Therefore, up to 3 parallel instances, the task for computing SWAG can run on a dedicated CPU core at a machine with 6 cores. For more parallel instances, the throughput growth becomes less linear compared to the first phase. In Fig. 8 (b), we observe the throughput of FPBA and Flink linearly scale up w.r.t more nodes used in a cluster.

6 CONCLUSION

In this paper, we presented PBA, a novel algorithm that calculates incremental aggregations in parallel for efficiently computing SWAGs, and also its sequential version SBA. We also proposed an approach to optimize the chunk size, which guarantees the minimum latency for PBA. Our experimental results demonstrate that SBA has higher throughput than state-of-the-art algorithms irrespective of window sizes, and PBA shows best performance for large windows (i.e., improving throughput up to 4x while reducing latency). Thus, a simple strategy for obtaining high performance can be using SBA for small windows and PBA for larger ones. In addition, FPBA, an integration of PBA into Apache Flink, shows significant improvement in both local mode and cluster mode.

As future works, we plan to extend PBA to support both multi-query processing and out-of-order streams. The idea is to replace the array structure of lcs buffers with a tree structure, where each leaf node stores a slice aggregation and any intermediate node stores partial aggregation of all its children (e.g., in the spirit of the array-based binary heap implementation of FlatFAT). In such a scenario, the major benefit of using PBA model is that any updates caused by late values can be processed only over lcs buffers in parallel, such that the computation for accumulating streaming values will not be delayed. One technical challenge underlying the development of such an approach lies in optimizing the chunk size that ensures the overall minimum latency, while taking into account watermarks and multiple combinations of ranges and slides.

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